

Lecture slides for
Automated Planning: Theory and Practice

Chapter 14

Temporal Planning

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Temporal Planning

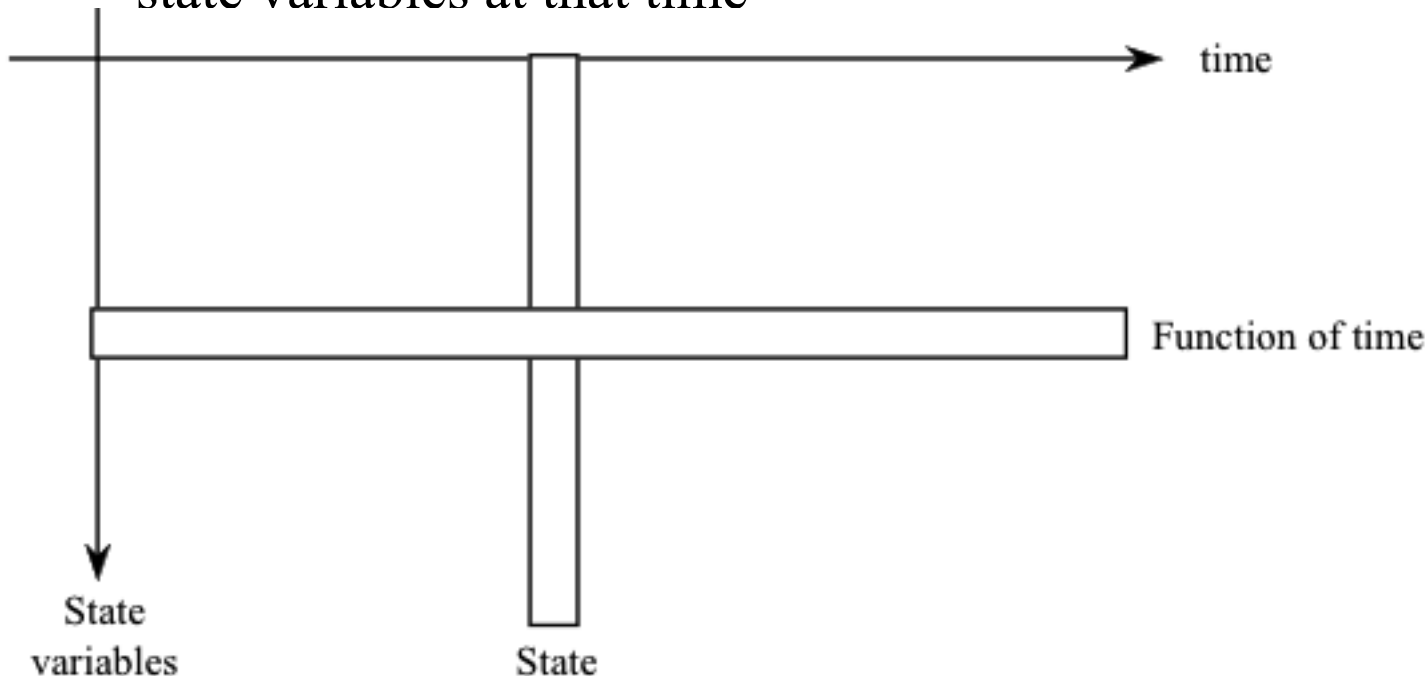
- Motivation: want to do planning in situations where actions
 - ◆ have nonzero duration
 - ◆ may overlap in time
- Need an explicit representation of time
- In Chapter 10 we studied a “temporal” logic
 - ◆ Its notion of time is too simple: a sequence of discrete events
 - ◆ Many real-world applications require continuous time
 - ◆ How to get this?

Temporal Planning

- The book presents two equivalent approaches:
 1. Use logical atoms, and extend the usual planning operators to include temporal conditions on those atoms
 - » Chapter 14 calls this the “state-oriented view”
 2. Use state variables, and specify change and persistence constraints on the state variables
 - » Chapter 14 calls this the “time-oriented view”
- In each case, the chapter gives a planning algorithm that’s like a temporal-planning version of PSP

The Time-Oriented View

- We'll concentrate on the “time-oriented view”: Sections 14.3.1–14.3.3
 - ◆ It produces a simpler representation
 - ◆ State variables seem better suited for the task
- States not defined explicitly
 - ◆ Instead, can compute a state for any time point, from the values of the state variables at that time

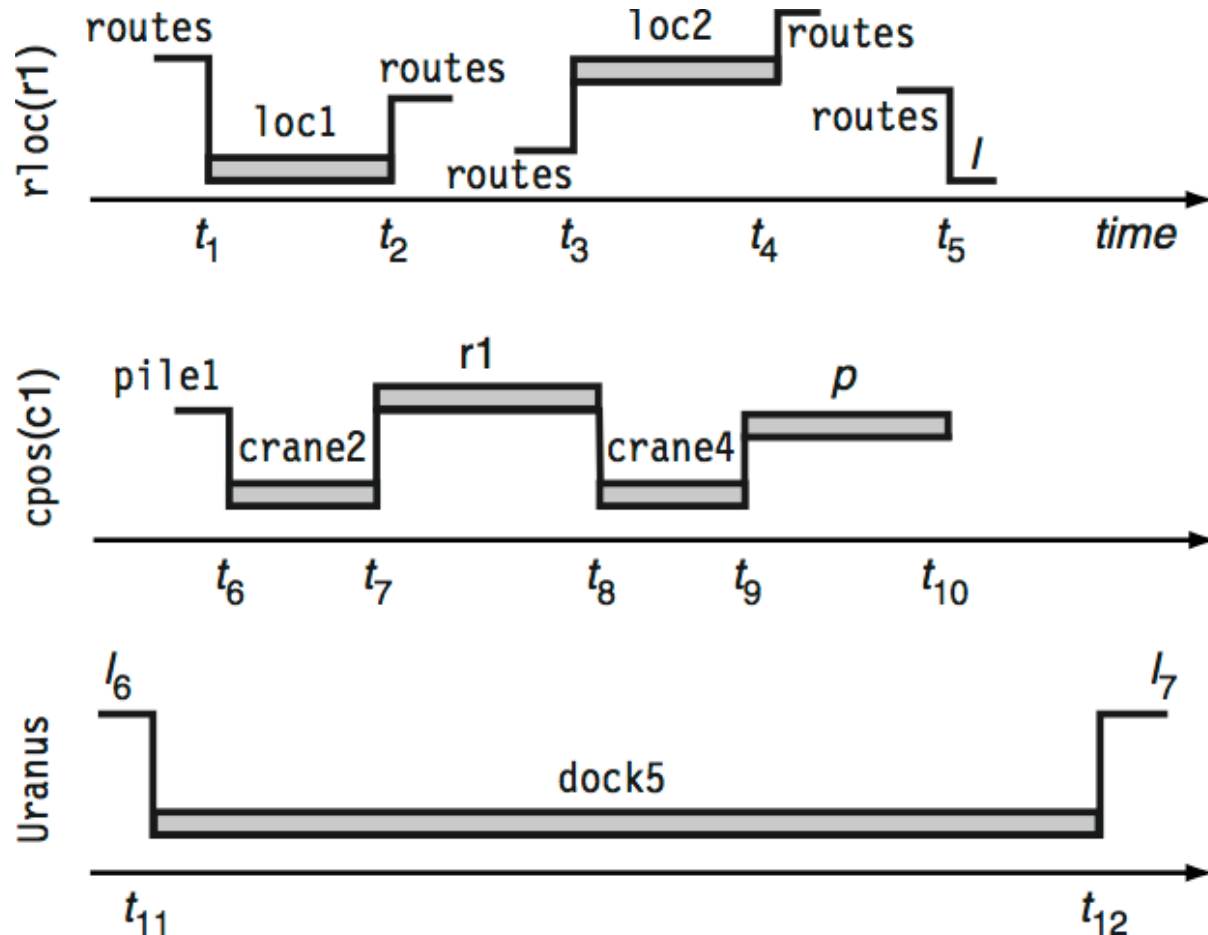


State Variables

- A **state variable** is a partially specified function telling what is true at some time t
 - ◆ $\text{cpos}(c1) : \text{time} \rightarrow \text{containers} \cup \text{cranes} \cup \text{robots}$
 - » Tells what $c1$ is on at time t
 - ◆ $\text{rloc}(r1) : \text{time} \rightarrow \text{locations}$
 - » Tells where $r1$ is at time t
- Might not ever specify the entire function
- $\text{cpos}(c)$ refers to a collection of state variables
 - ◆ But we'll be sloppy and just call it a state variable

DWR Example

- robot r1
 - ◆ in loc1 at time t_1
 - ◆ leaves loc1 at time t_2
 - ◆ enters loc2 at time t_3
 - ◆ leaves loc2 at time t_4
 - ◆ enters l at time t_5
- container c1
 - ◆ in pile1 until time t_6
 - ◆ held by crane2 until t_7
 - ◆ sits on r1 until t_8
 - ◆ held by crane4 until t_9
 - ◆ sits on p until t_{10}
(or later)
- ship Uranus
 - ◆ stays at dock5
from t_{11} to t_{12}



Temporal Assertions

- Temporal assertion:
 - ◆ *Event*: an expression of the form $x@t : (v_1, v_2)$
 - » At time t , x changes from v_1 to $v_2 \neq v_1$
 - ◆ *Persistence condition*: $x@[t_1, t_2) : v$
 - » $x = v$ throughout the interval $[t_1, t_2)$
 - ◆ where
 - » t, t_1, t_2 are constants or temporal variables
 - » v, v_1, v_2 are constants or object variables
- Note that the time intervals are semi-open
 - ◆ Why?

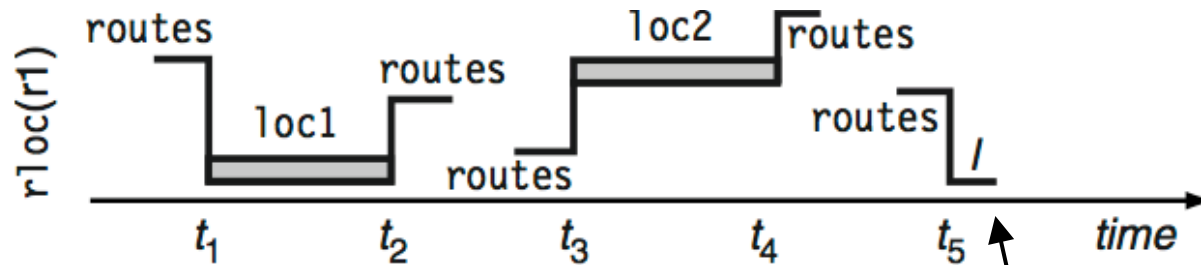
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- Note that the time intervals are semi-open
 - ◆ Why?
 - ◆ To prevent potential confusion about x 's value at the endpoints

Chronicles

- *Chronicle*: a pair $\Phi = (F, C)$
 - ◆ F is a finite set of temporal assertions
 - ◆ C is a finite set of constraints
 - » temporal constraints and object constraints
 - ◆ C must be consistent
 - » i.e., there must exist variable assignments that satisfy it
- *Timeline*: a chronicle for a single state variable
- The book writes F and C in a calligraphic font
 - ◆ Sometimes I will, more often I'll just use italics

Example



- Timeline for $rloc(r1)$:

```
({
  rloc(r1)@t1 : (l1, loc1),
  rloc(r1)@[t1, t2) : loc1,
  rloc(r1)@t2 : (loc1, l2),
  rloc(r1)@t3 : (l3, loc2),
  rloc(r1)@[t3, t4) : loc2,
  rloc(r1)@t4 : (loc2, l4),
  rloc(r1)@t5 : (l5, loc3)
},
```

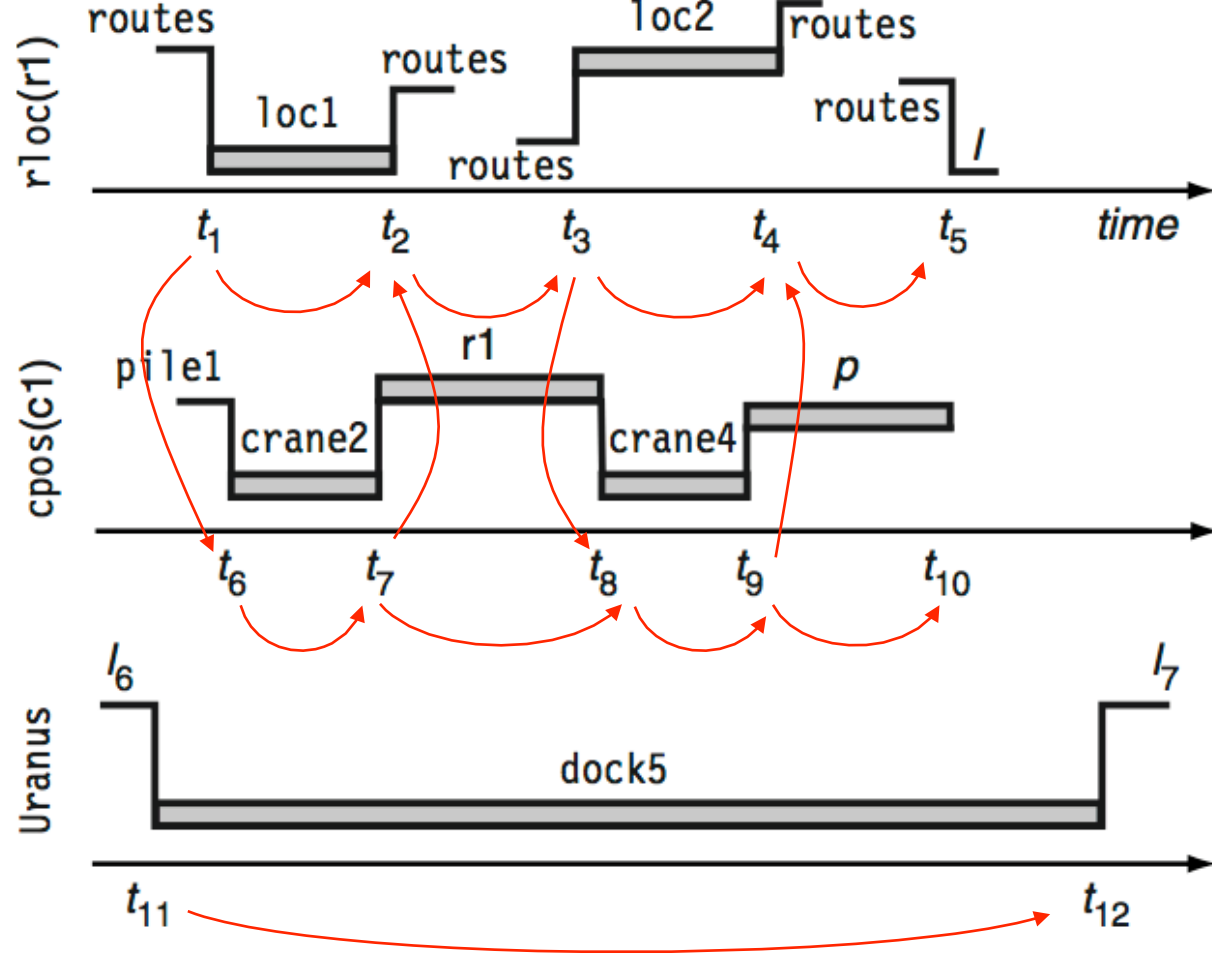
```
{
  adjacent(l1, loc1), adjacent(loc1, l2),
  adjacent(l3, loc2), adjacent(loc2, l4), adjacent(l5, loc3),
  t1 < t2 < t3 < t4 < t5
} ).
```

Inconsistency in the book
between Figure 14.5
and Example 14.9

C-consistency

- A timeline (F, C) is *c-consistent* (chronicle-consistent) if
 - ◆ C is consistent, and
 - ◆ Every pair of assertions in F are either disjoint or they refer to the same value and/or time points:
 - » If F contains both $x@[t_1, t_2]:v_1$ and $x@[t_3, t_4]:v_2$, then C must entail $\{t_2 \leq t_3\}$, $\{t_4 \leq t_1\}$, or $\{v_1 = v_2\}$
 - » If F contains both $x@t:(v_1, v_2)$ and $x@[t_1, t_2]:v$, then C must entail $\{t < t_1\}$, $\{t_2 < t\}$, $\{v = v_2, t_1 = t\}$, or $\{t_2 = t, v = v_1\}$
 - » If F contains both $x@t:(v_1, v_2)$ and $x@t':(v'_1, v'_2)$, then C must entail $\{t \neq t'\}$ or $\{v_1 = v'_1, v_2 = v'_2\}$
- (F, C) is c-consistent iff every timeline in (F, C) is c-consistent
- The book calls this consistency, not c-consistency
 - ◆ But it's a stronger requirement than ordinary mathematical consistency
- Mathematical consistency: C doesn't contradict the separation constraints
- c-consistency: C must actually entail the separation constraints
 - ◆ It's sort of like saying that (F, C) contains no threats

Example



- Let (F, C) include the timelines given earlier, plus some additional constraints:
 - ◆ $t_1 \leq t_6$, $t_7 < t_2$, $t_3 \leq t_8$, $t_9 < t_4$, $\text{attached}(p, \text{loc2})$
- Above, I've drawn the entire set of time constraints
- (F, C) is c-consistent

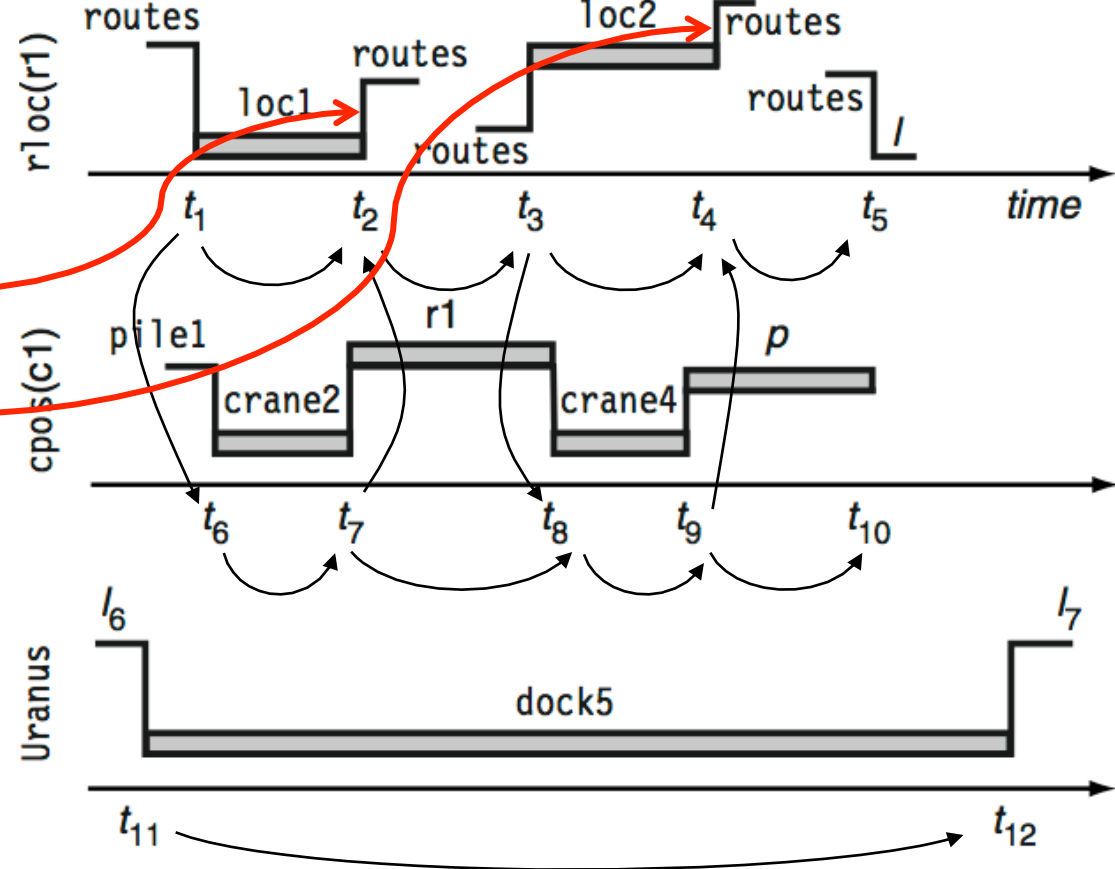
Support and Enablers

- Let α be either $x@t:(v,v')$ or $x@[t,t'):v$
 - ◆ Note that α requires $x = v$ either at t or just before t
- Intuitively, a chronicle $\Phi = (F,C)$ *supports* α if
 - ◆ F contains an assertion β that we can use to establish $x = v$ at some time $s < t$,
 - » β is called *the support for α*
 - ◆ and if it's consistent with Φ for v to persist over $[s,t)$ and for α be true
- Formally, $\Phi = (F,C)$ supports α if
 - ◆ F contains an assertion β of the form $\beta = x@s:(w',w)$ or $\beta = x@[s',s):w$, and
 - ◆ \exists separation constraints C' such that the following chronicle is c-consistent:
 - » $(F \cup \{x@[s,t):v, \alpha\}, C \cup C' \cup \{w=v, s < t\})$
 - ◆ C' can either be absent from Φ or already in Φ
- The chronicle $\delta = (\{x@[s,t):v, \alpha\}, C' \cup \{w=v, s < t\})$ is an *enabler* for α
 - ◆ *Analogous to a causal link in PSP*
- Just as there could be more than one possible causal link in PSP, there can be more than one possible enabler

Example

$$\beta_1 = \text{rloc}(r1)@t_2:(\text{loc1}, \text{routes})$$

$$\beta_2 = \text{rloc}(r1)@t_4:(\text{loc2}, \text{routes})$$



- Let Φ be as shown

- Then Φ supports

$$\alpha_1 = \text{rloc}(r1)@t:(\text{routes}, \text{loc3})$$

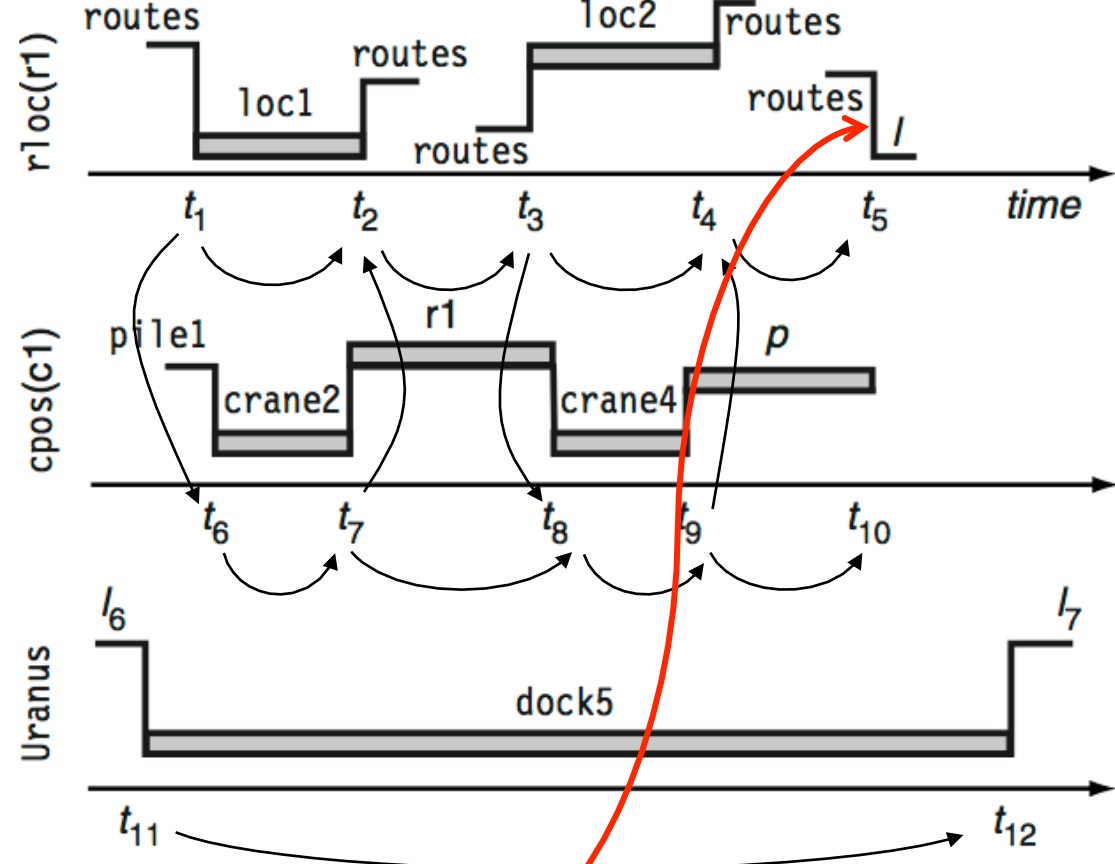
in two different ways:

- ◆ β_1 establishes $\text{rloc}(r1) = \text{routes}$ at time t_2
 - » this can support α_1 if we constrain $t_2 < t < t_3$
 - » enabler is $\delta_1 = (\{\text{rloc}(r1)@[t_2, t]: \text{routes}, \alpha_1\}, \{t_2 < t < t_3\})$
- ◆ β_2 establishes $\text{rloc}(r1) = \text{routes}$ at time t_4
 - » this can support α_1 if we constrain $t_4 < t < t_5$
 - » enabler is $\delta_2 = (\{\text{rloc}(r1)@[t_4, t]: \text{routes}, \alpha_1\}, \{t_4 < t < t_5\})$

Enabling Several Assertions at Once

- $\Phi = (F, C)$ supports a set of assertions $E = \{\alpha_1, \dots, \alpha_k\}$ if both of the following are true
 - ◆ $F \cup E$ contains a support β_i for α_i other than α_i itself
 - ◆ There are enablers $\delta_1, \dots, \delta_k$ for $\alpha_1, \dots, \alpha_k$ such that the chronicle $\Phi \cup \delta_1 \cup \dots \cup \delta_k$ is c-consistent
- Note that some of the assertions in E may support each other!
- $\phi = \{\delta_1, \dots, \delta_k\}$ is an *enabler* for E

Example



- Let Φ be as shown
- Let α_1 be the same as before:
 $\alpha_1 = \text{rloc}(r1)@t:(\text{routes}, \text{loc3})$
- Let $\alpha_2 = \text{rloc}(r1)@[t', t'']:\text{loc3}$
- Then Φ supports $\{\alpha_1, \alpha_2\}$ in four different ways:
 - ◆ As before, for α_1 we can use either β_1 and δ_1 or β_2 and δ_2
 - ◆ We can support α_2 with $\beta_3 = \text{rloc}(r1)@t_5:(\text{routes}, l)$
 - » Enabler is $\delta_3 = (\{\text{rloc}(r1)@[t_5, t']:\text{loc3}, \alpha_2\}, \{l = \text{loc3}, t_5 < t'\})$
 - ◆ Or we can support α_2 with α_1
 - » If we supported α_1 with β_1 and enabled it with δ_1 , the enabler for α_2 is $\delta_4 = (\{\text{rloc}(r1)@[t, t']:\text{loc3}, \alpha_2\}, \{t < t' < t_3\})$
 - » If we supported α_1 with β_1 and enabled it with δ_2 , then replace t_3 with t_5 in δ_4

One Chronicle Supporting Another

- Let $\Phi' = (F', C')$ be a chronicle, and suppose $\Phi = (F, C)$ supports F' .
- Let $\delta_1, \dots, \delta_k$ be all the possible enablers of Φ'
 - ◆ For each δ_i , let $\delta'_i = \delta_i \cup C'$
- If there is a δ'_i such that $\Phi \cup \delta'_i$ is c-consistent,
 - ◆ Then Φ *supports* Φ' , and δ'_i is an *enabler* for Φ'
 - ◆ If $\delta'_i \subseteq \Phi$, then Φ *entails* Φ'
- The set of all enablers for Φ' is $\theta(\Phi/\Phi') = \{\delta'_i : \Phi \cup \delta'_i \text{ is c-consistent}\}$

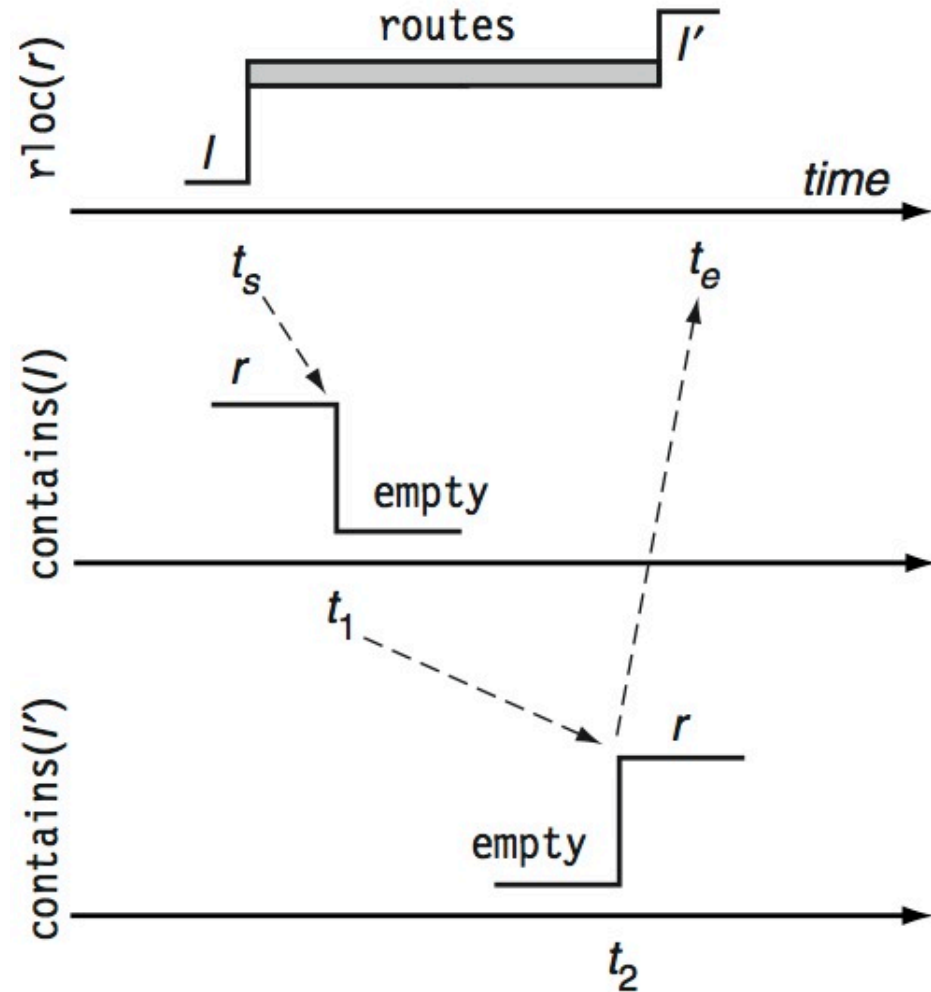
Chronicles as Planning Operators

- Chronicle planning operator: a pair $o = (\text{name}(o), (F(o), C(o)))$, where
 - ◆ $\text{name}(o)$ is an expression of the form $o(t_s, t_e, \dots, v_1, v_2, \dots)$
 - » o is an operator symbol
 - » $t_s, t_e, \dots, v_1, v_2, \dots$ are all the temporal and object variables in o
 - ◆ $(F(o), C(o))$ is a chronicle
- Action: a (partially) instantiated operator, a
- If a chronicle Φ supports $(F(a), C(a))$, then a is *applicable* to Φ
 - ◆ a may be applicable in several ways, so the result is a set of chronicles
 - » $\gamma(\Phi, a) = \{\Phi \cup \phi \mid \phi \in \theta(a/\Phi)\}$

Example: Operator for Moving a Robot

$\text{move}(t_s, t_e, t_1, t_2, r, l, l') =$
 {

- $\text{rloc}(r)@t_s$: (l, routes) ,
- $\text{rloc}(r)@[t_s, t_e]$: routes ,
- $\text{rloc}(r)@t_e$: (routes, l') ,
- $\text{contains}(l)@t_1$: (r, empty) ,
- $\text{contains}(l')@t_2$: (empty, r) ,
- $t_s < t_1 < t_2 < t_e$,
- $\text{adjacent}(l, l')$ }

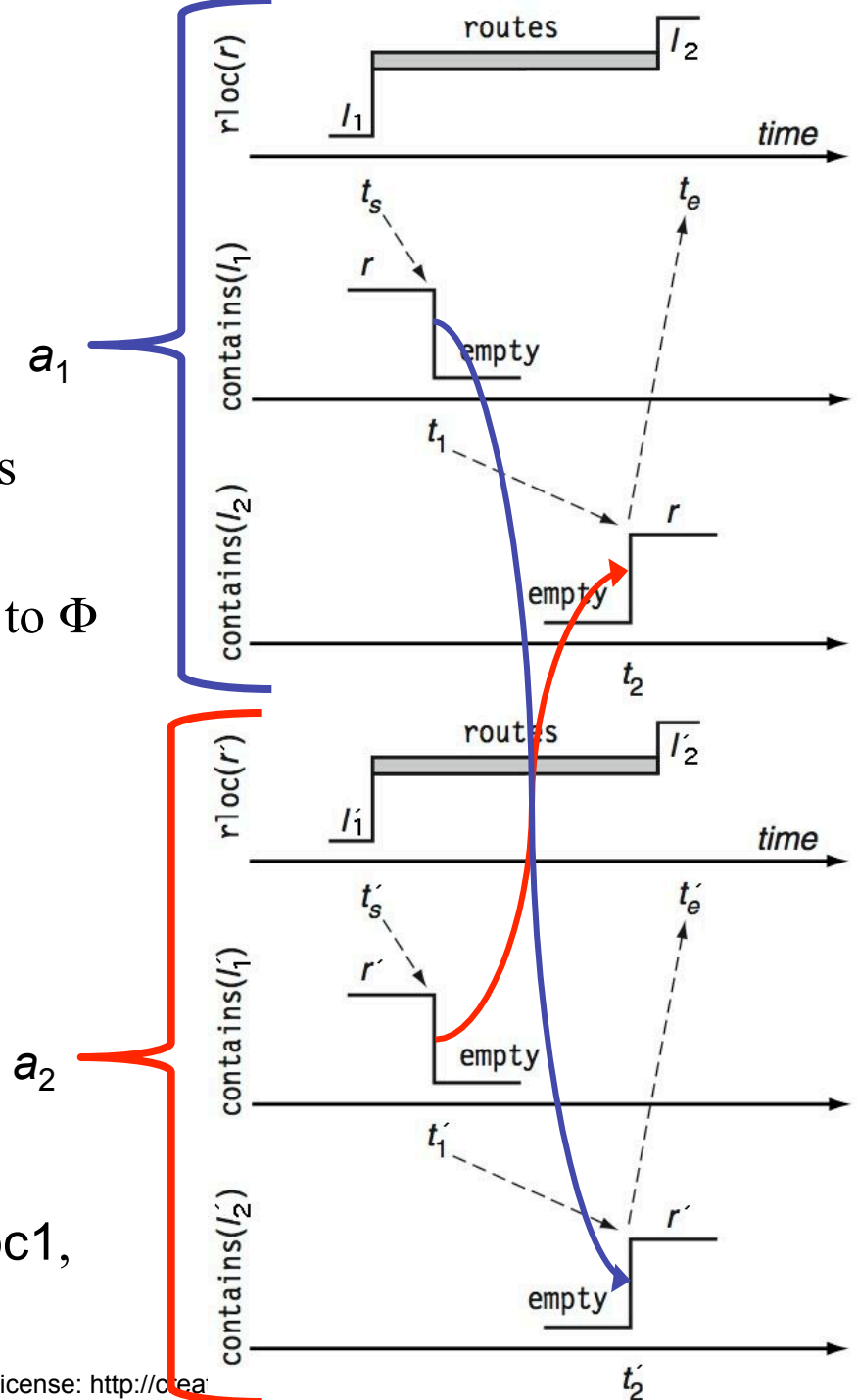


Applying a Set of Actions

- Just like several temporal assertions can support each other, several actions can also support each other
 - Let $\pi = \{a_1, \dots, a_k\}$ be a set of actions
 - Let $\Phi_\pi = \cup_i (F(a_i), C(a_i))$
 - If Φ supports Φ_π then π is applicable to Φ
 - Result is a *set* of chronicles
 - $\gamma(\Phi, \pi) = \{\Phi \cup \phi \mid \phi \in \theta(\Phi_\pi / \Phi)\}$

- Example:

- Suppose Φ asserts that at time t_0 , robots r_1 and r_2 are at adjacent locations loc_1 and loc_2
- Let a_1 and a_2 be as shown
- Then Φ supports $\{a_1, a_2\}$ with
 - $l_1 = loc_1, l_2 = loc_2, l'_1 = loc_2, l'_2 = loc_1,$
 - $t_0 < t_s < t_1 < t'_2, t_0 < t'_s < t'_1 < t_2$



Domains and Problems

- Temporal planning *domain*: a pair $\mathbf{D} = (\Lambda_\Phi, O)$
 - ◆ $O = \{\text{all chronicle planning operators in the domain}\}$
 - ◆ $\Lambda_\Phi = \{\text{all chronicles allowed in the domain}\}$
- Temporal planning *problem* on \mathbf{D} : a triple $\mathbf{P} = (\mathbf{D}, \Phi_0, \Phi_g)$
 - ◆ \mathbf{D} is the domain
 - ◆ Φ_0 and Φ_g are initial chronicle and goal chronicle
 - ◆ O is the set of chronicle planning operators
- Statement of the problem \mathbf{P} : a triple $P = (O, \Phi_0, \Phi_g)$
 - ◆ O is the set of chronicle planning operators
 - ◆ Φ_0 and Φ_g are initial chronicle and goal chronicle
- *Solution plan*: a set of actions $\pi = \{a_1, \dots, a_n\}$ such that at least one chronicle in $\gamma(\Phi_0, \pi)$ entails Φ_g

set of open goals

set of sets of enablers

$CP(\Phi, G, \mathcal{K}, \pi)$

if $G = \mathcal{K} = \emptyset$ then return(π)

perform the two following steps in any order

if $G \neq \emptyset$ then do

select any $\alpha \in G$

if $\theta(\alpha/\Phi) \neq \emptyset$ then return($CP(\Phi, G - \{\alpha\}, \mathcal{K} \cup \{\theta(\alpha/\Phi)\}, \pi)$)

else do

$relevant \leftarrow \{a \mid a \text{ contains a support for } \alpha\}$

if $relevant = \emptyset$ then return(failure)

nondeterministically choose $a \in relevant$

return($CP(\Phi \cup (\mathcal{F}(a), \mathcal{C}(a)), G \cup \mathcal{F}(a), \mathcal{K} \cup \{\theta(a/\Phi)\}, \pi \cup \{a\})$)

if $\mathcal{K} \neq \emptyset$ then do

select any $C \in \mathcal{K}$

threat-resolvers $\leftarrow \{\phi \in C \mid \phi \text{ consistent with } \Phi\}$

if $threat-resolvers = \emptyset$ then return(failure)

nondeterministically choose $\phi \in threat-resolvers$

return($CP(\Phi \cup \phi, G, \mathcal{K} - C, \pi)$)

● As in plan-space planning, there are two kinds of flaws:

◆ Open goal: a *tqe* that isn't yet enabled

◆ Threat: an enabler that hasn't yet been incorporated into Φ

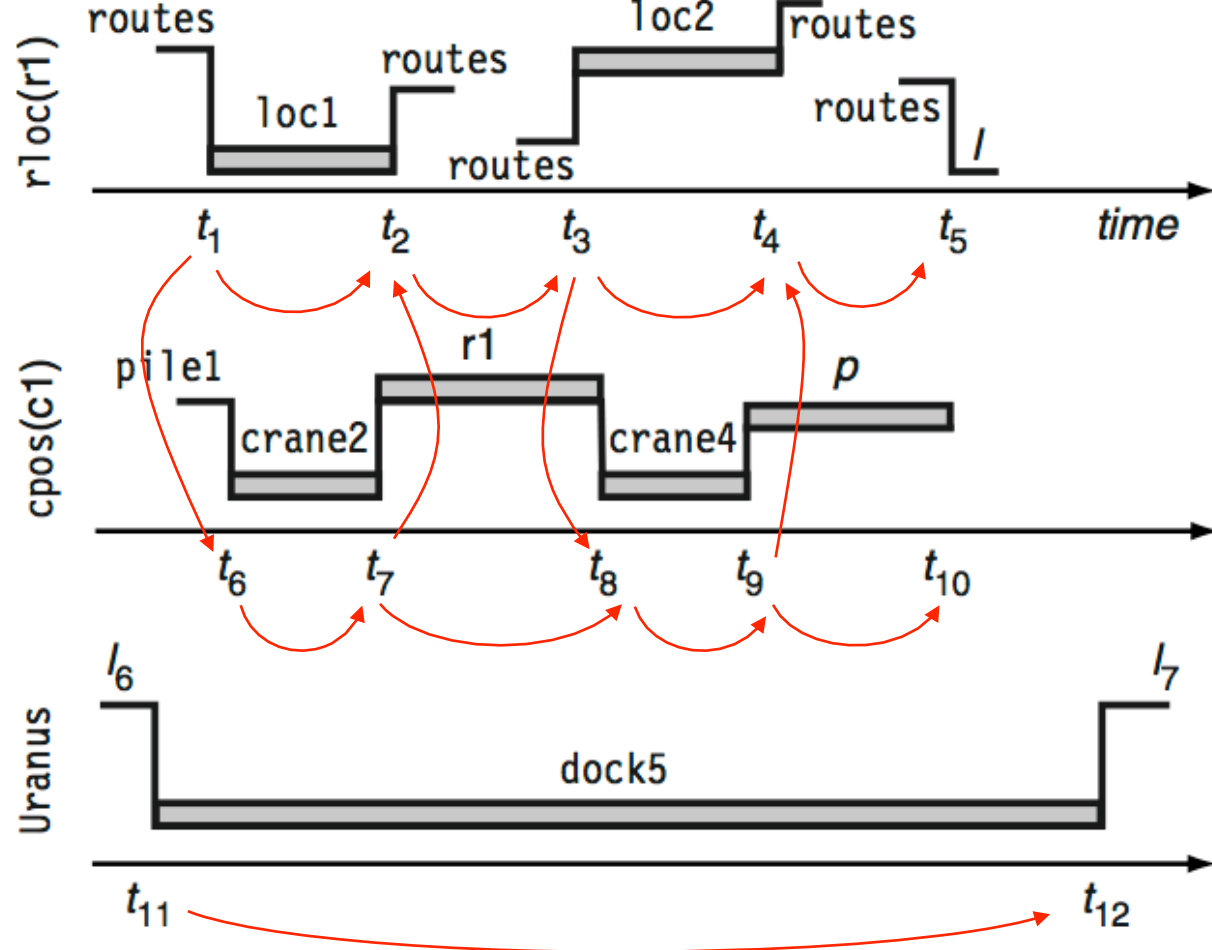
Resolving Open Goals

- Let $\alpha \in G$ be an open goal
- Case 1: Φ supports α
 - ◆ Resolver: any enabler for α that's consistent with Φ
 - ◆ Refinement:
 - » $G \leftarrow G - \{\alpha\}$
 - » $K \leftarrow K \cup \theta(\alpha/\Phi)$
- Case 2: Φ doesn't support α
 - ◆ Resolver: an action $a = (F(a), C(a))$ that supports α
 - » We don't yet require a to be supported by Φ
 - ◆ Refinement:
 - » $\pi \leftarrow \pi \cup \{a\}$
 - » $\Phi \leftarrow \Phi \cup (F(a), C(a))$
 - » $G \leftarrow G \cup F(a)$ Don't remove α yet: we haven't chosen an enabler for it
 - We'll choose one in a later call to CP, in Case 1 above
 - » $K \leftarrow K \cup \theta(a/\Phi)$ put a 's set of enablers into K

Resolving Threats

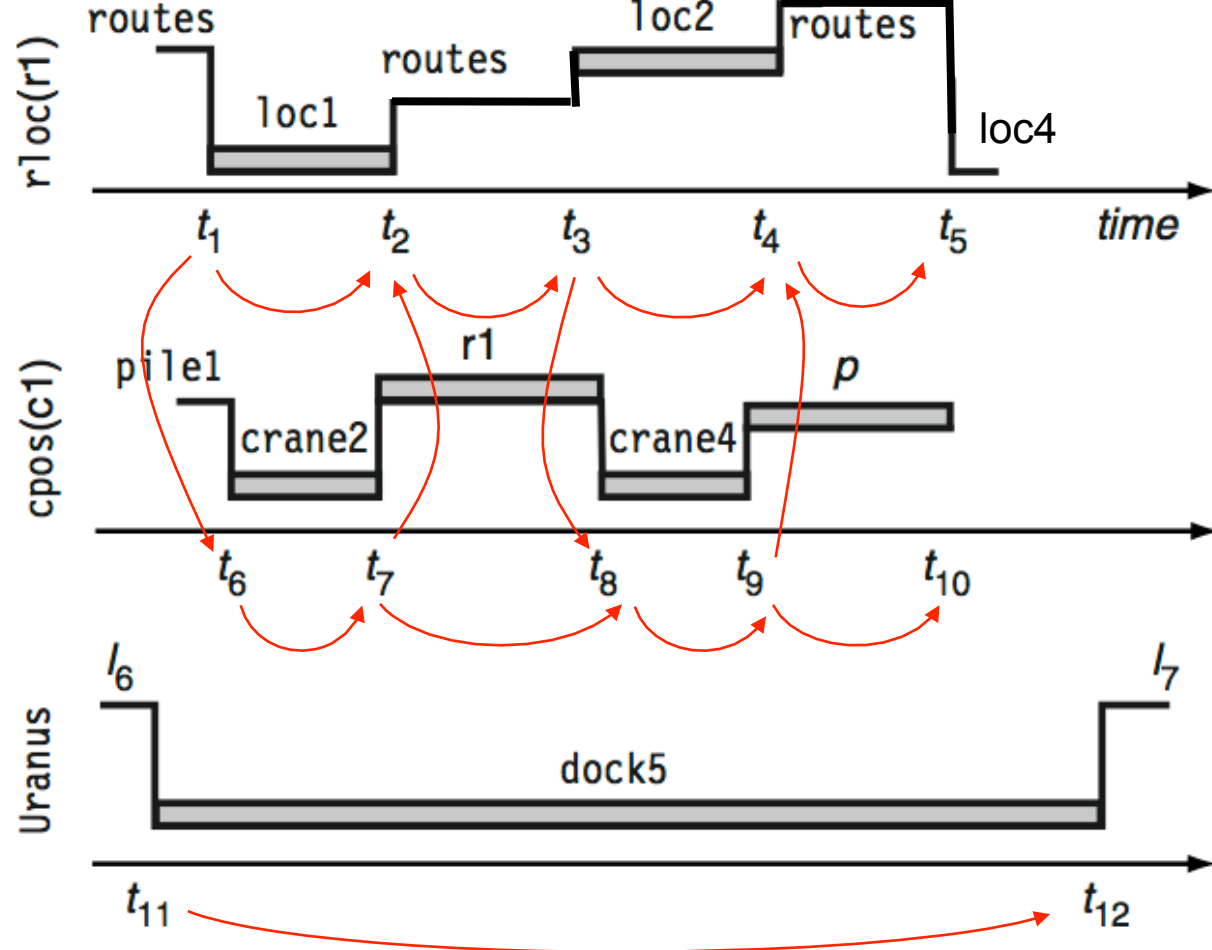
- *Threat*: each enabler in K that isn't yet entailed by Φ is threatened
 - ◆ For each C in K , we need only one of the enablers in C
 - » They're alternative ways to achieve the same thing
 - ◆ “Threat” means something different here than in PSP, because we won't try to entail *all* of the enablers
 - » Just the one we select
 - ◆ Resolver: any enabler ϕ in C that is consistent with Φ
 - ◆ Refinement:
 - » $K \leftarrow K - C$
 - » $\Phi \leftarrow \Phi \cup \phi$

Example



- Let Φ_0 be as shown, and $\Phi_g = \Phi_0 \cup (\{\alpha_1, \alpha_2\}, \{\})$, where α_1 and α_2 are the same as before:
 - ◆ $\alpha_1 = \text{rloc}(r1)@t:(\text{routes}, \text{loc3})$
 - ◆ $\alpha_2 = \text{rloc}(r1)@[t', t'']:\text{loc3}$
- As we saw earlier, we can support $\{\alpha_1, \alpha_2\}$ from Φ_0
 - ◆ Thus CP won't add any actions
 - ◆ It will return a modified version of Φ_0 that includes the enablers for $\{\alpha_1, \alpha_2\}$

Modified Example



- Let Φ_0 be as shown, and $\Phi_g = \Phi_0 \cup (\{\alpha_1, \alpha_2\}, \{\})$, where α_1 and α_2 are the same as before:

- ◆ $\alpha_1 = \text{rloc}(r1)@t:(\text{routes}, \text{loc3})$
- ◆ $\alpha_2 = \text{rloc}(r1)@[t', t'']:\text{loc3}$
- ◆ This time, CP will need to insert an action $\text{move}(t_s, t_e, t_1, t_2, r1, \text{loc4}, \text{loc3})$
 - » with $t_5 < t_s < t_1 < t_2 < t_e$