Lecture slides for Automated Planning: Theory and Practice

### Chapter 14 Temporal Planning

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# **Temporal Planning**

• Motivation: want to do planning in situations where actions

- have nonzero duration
- may overlap in time
- Need an explicit representation of time
- In Chapter 10 we studied a "temporal" logic
  - Its notion of time is too simple: a sequence of discrete events
  - Many real-world applications require continuous time
  - How to get this?

# **Temporal Planning**

• The book presents two equivalent approaches:

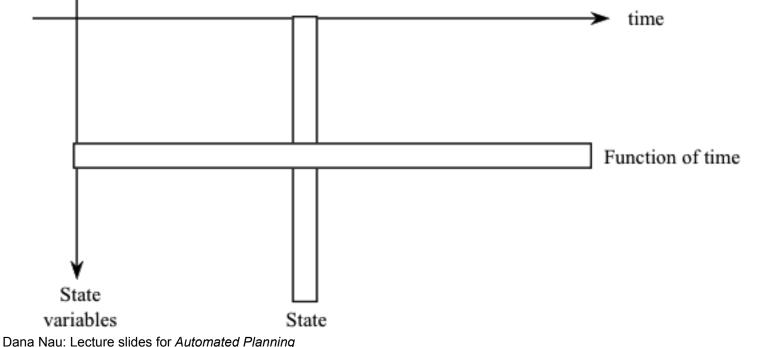
- 1. Use logical atoms, and extend the usual planning operators to include temporal conditions on those atoms
  - » Chapter 14 calls this the "state-oriented view"
- 2. Use state variables, and specify change and persistence constraints on the state variables

» Chapter 14 calls this the "time-oriented view"

• In each case, the chapter gives a planning algorithm that's like a temporal-planning version of PSP

# **The Time-Oriented View**

- We'll concentrate on the "time-oriented view": Sections 14.3.1–14.3.3
  - It produces a simpler representation
  - State variables seem better suited for the task
- States not defined explicitly
  - Instead, can compute a state for any time point, from the values of the state variables at that time

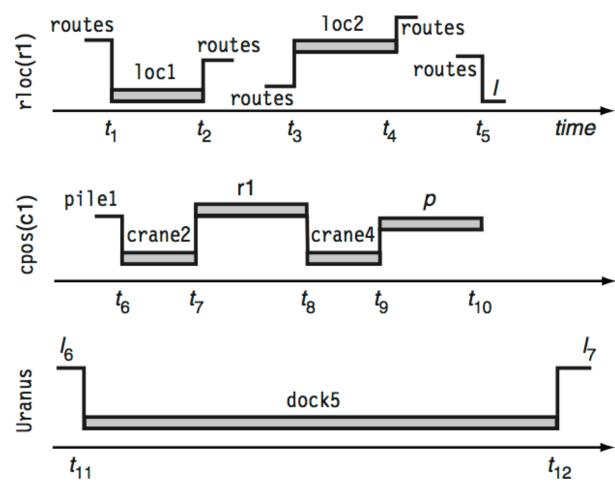


### **State Variables**

- A state variable is a partially specified function telling what is true at some time *t* 
  - cpos(c1) : time  $\rightarrow$  containers U cranes U robots
    - » Tells what c1 is on at time t
  - rloc(r1) : time  $\rightarrow$  locations
    - » Tells where r1 is at time t
- Might not ever specify the entire function
- cpos(c) refers to a collection of state variables
  - But we'll be sloppy and just call it a state variable

# **DWR Example**

- robot r1
  - in loc1 at time  $t_1$
  - leaves loc1 at time  $t_2$
  - enters loc2 at time  $t_3$
  - leaves loc2 at time  $t_4$
  - enters l at time  $t_5$
- container c1
  - in pile1 until time  $t_6$
  - held by crane2 until  $t_7$
  - sits on r1 until  $t_8$
  - held by crane4 until  $t_9$
  - sits on p until  $t_{10}$  (or later)
- ship Uranus
  - stays at dock5 from  $t_{11}$  to  $t_{12}$



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## **Temporal Assertions**

- Temporal assertion:
  - *Event*: an expression of the form  $x@t: (v_1, v_2)$ 
    - » At time *t*, *x* changes from  $v_1$  to  $v_2 \neq v_1$
  - *Persistence condition*:  $x@[t_1,t_2) : v$ 
    - » x = v throughout the interval  $[t_1, t_2)$

where

- »  $t, t_1, t_2$  are constants or temporal variables
- »  $v, v_1, v_2$  are constants or object variables
- Note that the time intervals are semi-open

• Why?

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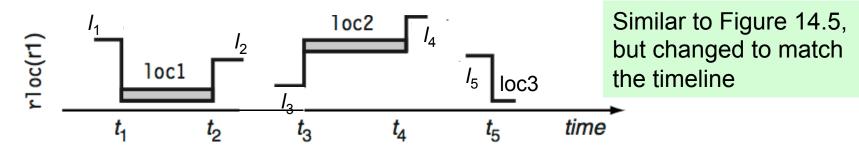
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- »  $v, v_1, v_2$  are constants or object variables
- Note that the time intervals are semi-open
  - Why?
  - To prevent potential confusion about *x*'s value at the endpoints

# Chronicles

- *Chronicle*: a pair  $\Phi = (F, C)$ 
  - *F* is a finite set of temporal assertions
  - *C* is a finite set of constraints
    - » temporal constraints and object constraints
  - *C* must be consistent
    - » i.e., there must exist variable assignments that satisfy it
- *Timeline*: a chronicle for a single state variable
- The book writes *F* and *C* in a calligraphic font
  - Sometimes I will, more often I'll just use italics

## Example



• Timeline for rloc(r1), from Example 14.9 of the book

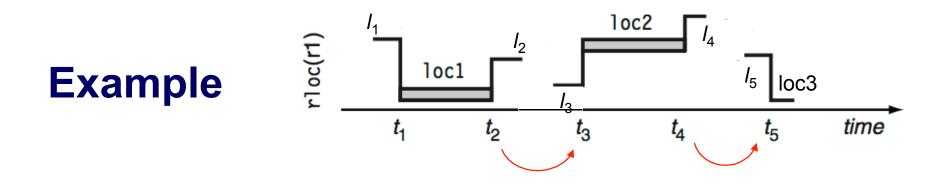
$$\begin{array}{ll} (\{ & \mathsf{rloc}(\mathsf{r1})@t_1:(l_1,\mathsf{loc1}), \\ & \mathsf{rloc}(\mathsf{r1})@[t_1,t_2):\mathsf{loc1}, \\ & \mathsf{rloc}(\mathsf{r1})@t_2:(\mathsf{loc1},l_2), \\ & \mathsf{rloc}(\mathsf{r1})@t_3:(l_3,\mathsf{loc2}), \\ & \mathsf{rloc}(\mathsf{r1})@[t_3,t_4):\mathsf{loc2}, \\ & \mathsf{rloc}(\mathsf{r1})@t_4:(\mathsf{loc2},l_4), \\ & \mathsf{rloc}(\mathsf{r1})@t_5:(l_5,\mathsf{loc3}) \ \ \}, \\ \{ & \mathsf{adjacent}(l_1,\mathsf{loc1}),\mathsf{adjacent}(\mathsf{loc1},l_2), \\ & \mathsf{adjacent}(l_3,\mathsf{loc2}), \mathsf{adjacent}(\mathsf{loc2},l_4), \mathsf{adjacent}(l_5,\mathsf{loc3}), \\ & t_1 < t_2 < t_3 < t_4 < t_5 \ \} \ ). \end{array}$$

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## **C-consistency**

- A timeline (*F*,*C*) is *c*-consistent (chronicle-consistent) if
  - $\bullet$  *C* is consistent, and
  - Every pair of assertions in *F* are either disjoint or they refer to the same value and/or time points:
    - » If *F* contains both  $x@[t_1,t_2):v_1$  and  $x@[t_3,t_4):v_2$ , then *C* must entail  $\{t_2 \le t_3\}, \{t_4 \le t_1\}, \text{ or } \{v_1 = v_2\}$
    - » If *F* contains both  $x@t:(v_1,v_2)$  and  $x@[t_1,t_2):v$ , then *C* must entail  $\{t < t_1\}, \{t_2 < t\}, \{v = v_2, t_1 = t\}, \text{ or } \{t_2 = t, v = v_1\}$
    - » If *F* contains both  $x@t:(v_1,v_2)$  and  $x@t':(v'_1,v'_2)$ , then *C* must entail  $\{t \neq t'\}$  or  $\{v_1 = v'_1, v_2 = v'_2\}$
- (F,C) is c-consistent iff every timeline in (F,C) is c-consistent
- The book calls this consistency, not c-consistency
  - But it's a stronger requirement than ordinary mathematical consistency
- Mathematical consistency: *C* doesn't contradict the separation constraints
- c-consistency: *C* must actually entail the separation constraints
  - It's sort of like saying that (*F*,*C*) contains no threats

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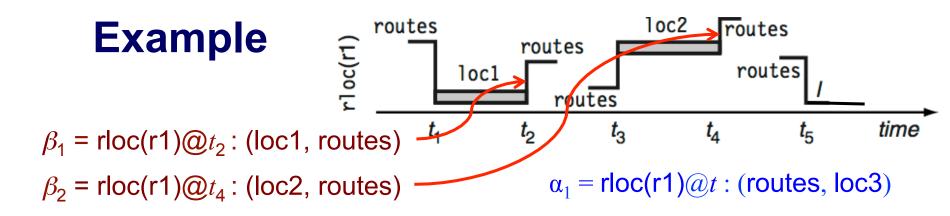
- Let (F,C) be the timeline given earlier for r1
- (F,C) is not c-consistent
  - To ensure that  $rloc(r1)@[t_1,t_2)$ :loc1 and  $rloc(r1)@t_3:(l_3,loc2)$  don't conflict, need  $t_2 < t_3$  or  $t_3 < t_1$
  - To ensure that  $rloc(r1)@[t_1,t_2)$ :loc1 and  $rloc(r1)@[t_3,t_4)$ :loc2 don't conflict, need  $t_2 < t_3$  or  $t_4 < t_1$
  - Etc.
- If we add some additional time constraints, (*F*,*C*) will be consistent:
  - e.g.,  $t_2 < t_3$  and  $t_4 < t_5$

# **Support and Enablers**

- Let  $\alpha$  be either x@t:(v,v') or x@[t,t'):v
  - Note that  $\alpha$  requires x = v either at *t* or just before *t*
- Intuitively, a chronicle  $\Phi = (F, C)$  supports  $\alpha$  if
  - *F* contains an assertion  $\beta$  that we can use to establish x = v at some time s < t,
    - »  $\beta$  is called *the support for*  $\alpha$
  - and if it's consistent with  $\Phi$  for v to persist over [s,t) and for  $\alpha$  be true
- Formally,  $\Phi = (F, C)$  supports  $\alpha$  if
  - *F* contains an assertion  $\beta$  of the form  $\beta = x@s:(w',w)$  or  $\beta = x@[s',s):w$ , and
  - A separation constraints C' such that the following chronicle is c-consistent:
    » (F ∪ {x@[s,t):v, α}, C ∪ C' ∪ {w=v, s < t})</li>
  - C' can either be absent from  $\Phi$  or already in  $\Phi$
- The chronicle  $\delta = (\{x @ [s,t]:v, \alpha\}, C' \cup \{w=v, s < t\})$  is an *enabler* for  $\alpha$

Analogous to a causal link in PSP

• Just as there could be more than one possible causal link in PSP, there can be more than one possible enabler



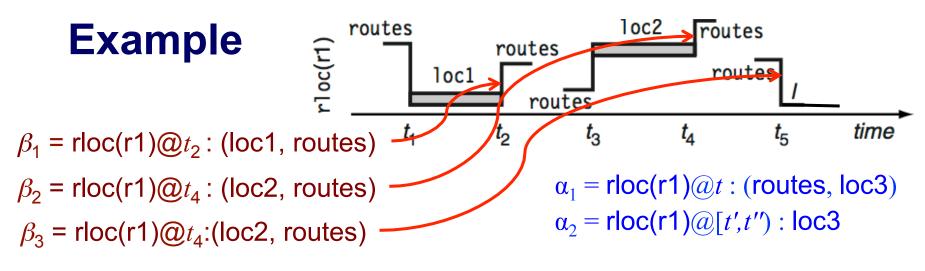
### • $\Phi$ supports $\alpha_1$ in two different ways:

- $\beta_1$  establishes rloc(r1) = routes at time  $t_2$ 
  - » this can support  $\alpha_1$  if we constrain  $t_2 < t < t_3$
  - » enabler is  $\delta_1 = (\{ \mathsf{rloc}(\mathsf{r1}) @ [t_2, t] : \mathsf{routes}, \alpha_1 \}, \{ t_2 \le t \le t_3 \}$
- $\beta_2$  establishes rloc(r1) = routes at time  $t_4$ 
  - » this can support  $\alpha_1$  if we constrain  $t_4 < t < t_5$
  - » enabler is  $\delta_2 = (\{ \mathsf{rloc}(\mathsf{r1}) @ [t_4, t] : \mathsf{routes}, \alpha_1 \}, \{ t_4 < t < t_5 \}$

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## **Enabling Several Assertions at Once**

- $\Phi = (F, C)$  supports a set of assertions  $E = \{\alpha_1, ..., \alpha_k\}$  if both of the following are true
  - $F \cup E$  contains a support  $\beta_i$  for  $\alpha_i$  other than  $\alpha_i$  itself
  - There are enablers δ<sub>1</sub>, ..., δ<sub>k</sub> for α<sub>1</sub>, ..., α<sub>k</sub> such that the chronicle Φ ∪ δ<sub>1</sub> ∪ ... ∪ δ<sub>k</sub> is c-consistent
- Note that some of the assertions in *E* may support each other!
- $\phi = \{\delta_1, ..., \delta_k\}$  is an *enabler* for *E*



- $δ_1 = (\{ \mathsf{rloc}(\mathsf{r1})@[t_2,t):\mathsf{routes}, α_1 \}, \{t_2 < t < t_3 \}$  $δ_2 = (\{ \mathsf{rloc}(\mathsf{r1})@[t_4,t):\mathsf{routes}, α_1 \}, \{t_4 < t < t_5 \}$
- $\Phi$  supports { $\alpha_1, \alpha_2$ } in four different ways:
  - As before, for  $\alpha_1$  we can use either  $\beta_1$  and  $\delta_1$  or  $\beta_2$  and  $\delta_2$
  - We can support  $\alpha_2$  with  $\beta_3$ 
    - » Enabler is  $\delta_3 = (\{ \mathsf{rloc}(\mathsf{r1}) @ [t_5, t'] : \mathsf{loc3}, \alpha_2 \}, \{ l = \mathsf{loc3}, t_5 < t' \} )$
  - Or we can support  $\alpha_2$  with  $\alpha_1$ 
    - » If used  $\beta_1$  and  $\delta_1$  for  $\alpha_1$ ,
      - Then  $\alpha_2$ 's enabler is  $\delta_4 = (\{ \mathsf{rloc}(\mathsf{r1}) @ [t,t') : \mathsf{loc3}, \alpha_2 \}, \{ t \le t' \le t_3 \})$
    - » If we used  $\beta_1$  and  $\delta_2$  for  $\alpha_1$ , then replace  $t_3$  with  $t_5$  in  $\delta_4$

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# **One Chronicle Supporting Another**

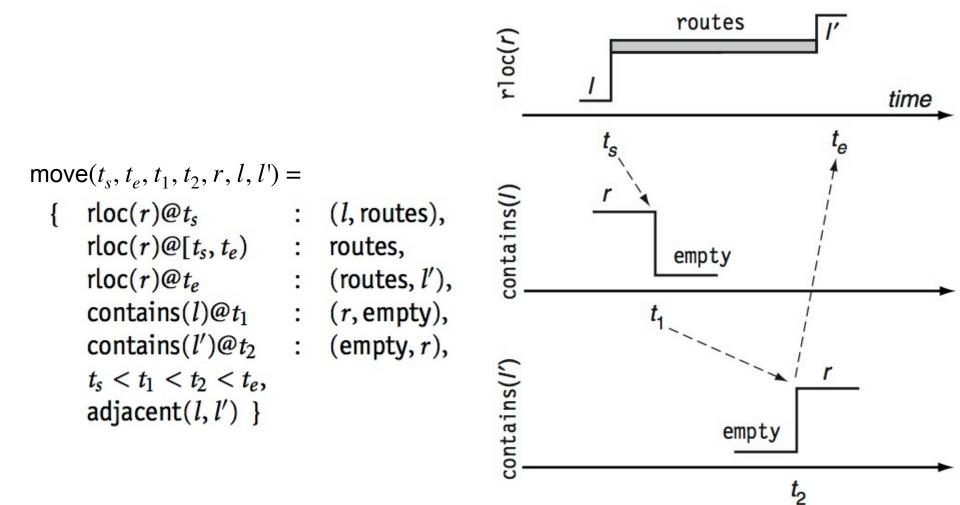
- Let  $\Phi' = (F', C')$  be a chronicle
- Suppose  $\Phi = (F, C)$  supports F'.
- Let  $\delta_1, \ldots, \delta_k$  be all the possible enablers of  $\Phi'$ 
  - For each  $\delta_i$ , let  $\delta'_i = \delta_1 \cup C'$
- If there is a  $\delta'_i$  such that  $\Phi \cup \delta'_i$  is c-consistent,
  - Then  $\Phi$  supports  $\Phi'$ , and  $\delta'_i$  is an enabler for  $\Phi'$
  - If  $\delta'_i \subseteq \Phi$ , then  $\Phi$  entails  $\Phi'$

• The set of all enablers for  $\Phi'$  is  $\theta(\Phi/\Phi') = \{\delta'_i : \Phi \cup \delta'_i \text{ is c-consistent}\}$ 

## **Chronicles as Planning Operators**

- Chronicle planning operator: a pair o = (name(o), (F(o), C(o))), where
  - name(*o*) is an expression of the form  $o(t_s, t_e, ..., v_1, v_2, ...)$ 
    - » *o* is an operator symbol
    - »  $t_s, t_e, ..., v_1, v_2, ...$  are all the temporal and object variables in o
  - (F(o), C(o)) is a chronicle
- Action: a (partially) instantiated operator, *a*
- If a chronicle  $\Phi$  supports (*F*(*a*),*C*(*a*)), then *a* is *applicable* to  $\Phi$ 
  - *a* may be applicable in several ways, so the result is a set of chronicles
    - »  $\gamma(\Phi,a) = \{ \Phi \cup \phi \mid \phi \in \theta(a/\Phi) \}$

### **Example: Operator for Moving a Robot**



# Applying a Set of Actions

- Just like several temporal assertions can support each other, several actions can also support each other
  - Let  $\pi = \{a_1, ..., a_k\}$  be a set of actions
  - Let  $\Phi_{\pi} = \bigcup_i (F(a_i), C(a_i))$
  - If  $\Phi$  supports  $\Phi_{\pi}$  then  $\pi$  is applicable to  $\Phi$

 $a_1$ 

 $a_2$ 

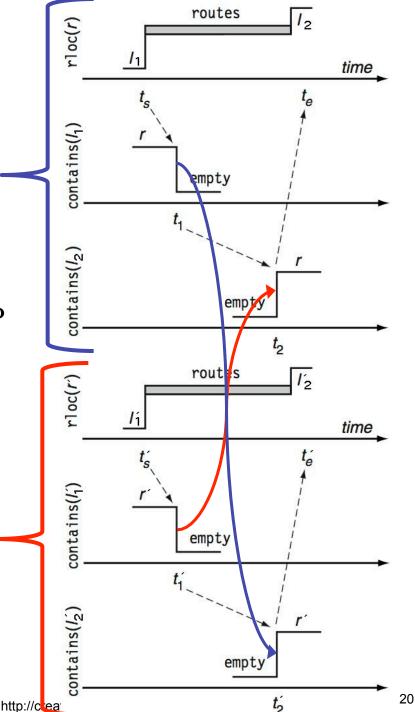
• Result is a *set* of chronicles  $\gamma(\Phi,\pi) = \{ \Phi \cup \phi \mid \phi \in \theta(\Phi_{\pi}/\Phi) \}$ 

• Example:

- Suppose Φ asserts that at time t<sub>0</sub>, robots r1 and r2 are at adjacent locations loc1 and loc2
- Let  $a_1$  and  $a_2$  be as shown

• Then 
$$\Phi$$
 supports  $\{a_1, a_2\}$  with  
 $l_1 = \text{loc1}, l_2 = \text{loc2}, l'_1 = \text{loc2}, l'_2 = \text{loc1},$   
 $t_0 < t_s < t_1 < t'_2, t_0 < t'_s < t'_1 < t_2$ 

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# **Domains and Problems**

- Temporal planning *domain*:
  - A pair  $\boldsymbol{D} = (\Lambda_{\Phi}, O)$ 
    - »  $O = \{$ all chronicle planning operators in the domain $\}$
    - »  $\Lambda_{\Phi} = \{ all chronicles allowed in the domain \}$
- Temporal planning *problem* on **D**:
  - A triple  $\boldsymbol{P} = (\boldsymbol{D}, \Phi_0, \Phi_g)$ 
    - » **D** is the domain
    - »  $\Phi_0$  and  $\Phi_g$  are initial chronicle and goal chronicle
    - » O is the set of chronicle planning operators
- Statement of the problem *P*:
  - A triple  $P = (O, \Phi_{0}, \Phi_{g})$ 
    - » O is the set of chronicle planning operators
    - »  $\Phi_0$  and  $\Phi_g$  are initial chronicle and goal chronicle
- Solution plan:
  - A set of actions  $\pi = \{a_1, ..., a_n\}$  such that at least one chronicle in  $\gamma(\Phi_0, \pi)$  entails  $\Phi_g$

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As in plan-space planning, there are two set of open goals (*tqes*) kinds of flaws: / \_ set of sets of enablers • Open goal: a *tqe* that isn't yet enabled  $CP(\Phi, G, \mathcal{K}, \pi)$ Threat: an enabler that hasn't yet been incorporated into  $\Phi$ if  $G = \mathcal{K} = \emptyset$  then return $(\pi)$ perform the two following steps in any order if  $G \neq \emptyset$  then do select any  $\alpha \in G$ if  $\theta(\alpha/\Phi) \neq \emptyset$  then return(CP( $\Phi, G - \{\alpha\}, \mathcal{K} \cup \{\theta(\alpha/\Phi)\}, \pi$ )) else do *relevant*  $\leftarrow$  {*a* | *a* contains a support for  $\alpha$ } if *relevant* =  $\emptyset$  then return(failure) nondeterministically choose  $a \in relevant$ return(CP( $\Phi \cup (\mathcal{F}(a), \mathcal{C}(a)), G \cup \mathcal{F}(a), \mathcal{K} \cup \{\theta(a/\Phi)\}, \pi \cup \{a\}$ )) if  $\mathcal{K} \neq \emptyset$  then do select any  $C \in \mathcal{K}$ threat-resolvers  $\leftarrow \{ \phi \in C \mid \phi \text{ consistent with } \Phi \}$ if *threat-resolvers* =  $\emptyset$  then return(failure) nondeterministically choose  $\phi \in threat$ -resolvers return(CP( $\Phi \cup \phi, G, \mathcal{K} - C, \pi$ ))

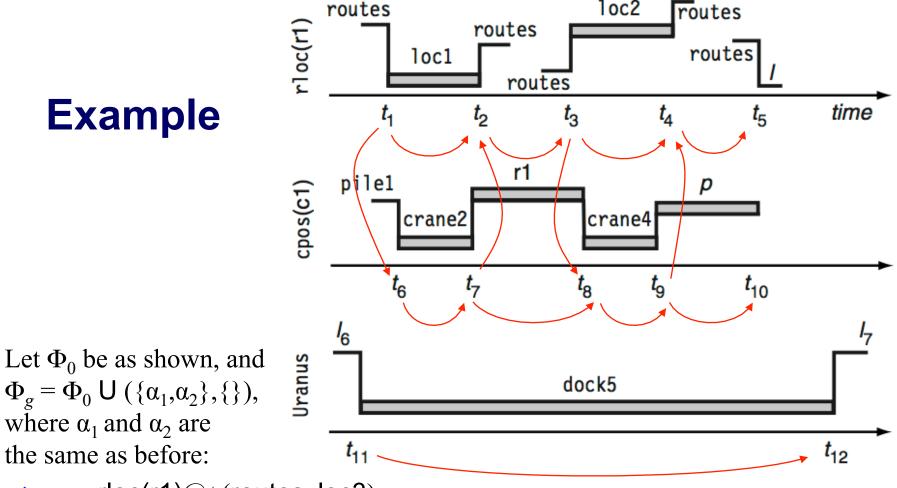
# **Resolving Open Goals**

- Let  $\alpha \in G$  be an open goal
- Case 1:  $\Phi$  supports  $\alpha$ 
  - Resolver: any enabler for  $\alpha$  that's consistent with  $\Phi$
  - Refinement:
    - »  $G \leftarrow G \{\alpha\}$
    - »  $K \leftarrow K \cup \theta(\alpha/\Phi)$
- Case 2:  $\Phi$  doesn't support  $\alpha$ 
  - Resolver: an action a = (F(a), C(a)) that supports  $\alpha$ 
    - » We don't yet require a to be supported by  $\Phi$
  - Refinement:
    - »  $\pi \leftarrow \pi \cup \{a\}$
    - »  $\Phi \leftarrow \Phi \cup (F(a), C(a))$
    - »  $G \leftarrow G \cup F(a)$  Don't remove  $\alpha$  yet: we haven't chosen an enabler for it
      - We'll choose one in a later call to CP, in Case 1 above
    - »  $K \leftarrow K \cup \theta(a/\Phi)$  put *a*'s set of enablers into *K*

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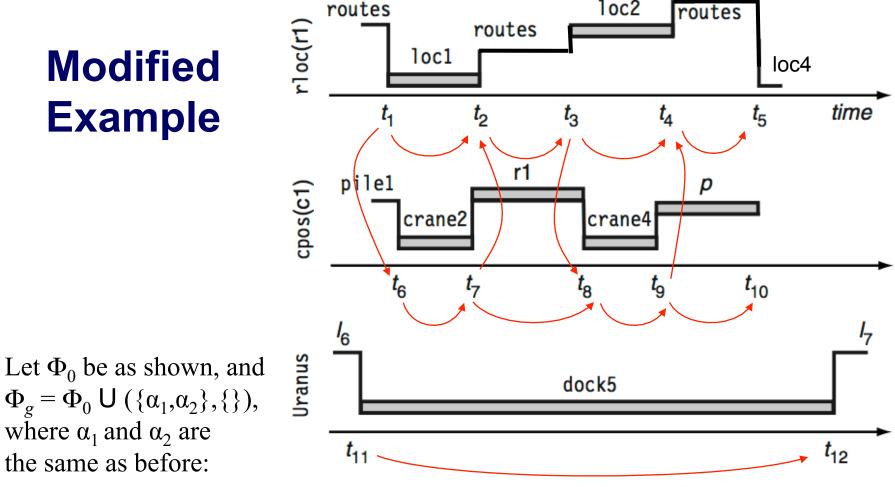
# **Resolving Threats**

- *Threat*: each enabler in *K* that isn't yet entailed by  $\Phi$  is threatened
  - For each C in K, we need only one of the enablers in C
    - » They're alternative ways to achieve the same thing
  - "Threat" means something different here than in PSP, because we won't try to entail *all* of the enablers
    - » Just the one we select
  - Resolver: any enabler  $\phi$  in *C* that is consistent with  $\Phi$
  - Refinement:
    - »  $K \leftarrow K C$
    - »  $\Phi \leftarrow \Phi \cup \phi$



- $\alpha_1 = rloc(r1)@t:(routes, loc3)$
- $\alpha_2 = \operatorname{rloc}(r1)@[t',t''):loc3$
- As we saw earlier, we can support  $\{\alpha_1, \alpha_2\}$  from  $\Phi_0$ 
  - Thus CP won't add any actions
  - It will return a modified version of  $\Phi_0$  that includes the enablers for  $\{\alpha_1, \alpha_2\}$

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- $\alpha_1 = rloc(r1)@t:(routes, loc3)$
- $\alpha_2 = \operatorname{rloc}(r1)@[t',t''):loc3$
- This time, CP will need to insert an action  $move(t_s, t_e, t_1, t_2, r1, loc4, loc3)$ 
  - » with  $t_5 < t_s < t_1 < t_2 < t_e$

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