Due in class: Complete by Apr 18.

- (1) Give an f-approximate algorithm for the set cover problem in which each element belongs to at most f sets.
- (2) Prove that Integer Programming is NP-hard.
- (3) Jerry runs a tent rental company. People make requests for reserving tents. Request i has three parameters the profit p_i gained if the request is satisfied, the start time s_i and the end time e_i . Assume that n requests are known in advance. Jerry would like to maximize his profit.
 - (a) Design an efficient algorithm for the case when Jerry has one tent, and would like to maximize his profit. Note that if Jerry agrees to rent the tent to a set of people, then the time intervals during which they wish to have the tent should not overlap. (No proof required.) Faster algorithms will receive more points.
 - (b) If Jerry has k tents, how would you reduce this problem to an instance of min-cost flow? (No proof required.)
- (4) Consider the following approximation algorithm for unweighted vertex cover. Run DFS in the graph (assume it is connected) to obtain a DFS tree T. Now pick all the non-leaf vertices in the vertex cover. Prove that this is a 2-approximation. Why does this form a vertex cover? (Hint: Any matching in G is a lower bound on the size of a vertex cover.)
- (5) Show that there is always an optimal solution to the vertex cover LP whose optimal solutions only have the values $\{0, \frac{1}{2}, 1\}$. (If you look up the proof, I would like you to describe it in your own words.)