

## Problem 1

The answer can be got from inspection as in the following two tables.

| $i$ | $j$     | Printing # |
|-----|---------|------------|
| 1   | 1 to 4  | 4          |
| 2   | 2 to 7  | 6          |
| 3   | 3 to 10 | 8          |
| ... | ...     | ...        |

| $n$ | $i$    | Printing # |
|-----|--------|------------|
| 1   | 1 to 1 | 4          |
| 2   | 1 to 2 | 10         |
| 3   | 1 to 3 | 18         |
| ... | ...    | ...        |

But you must offer some concrete “evidence” to say the answer is something. Inspection is not good enough for such a kind course. (Algorithm)

The inner loop is only a print statement, so the constant execution time is needed. You can use a “c” or “k” to denote the constant, or just using 1 (unity). Either is  $O(1)$ .

Take a look at your textbook pp.1058-1060 for some concepts about summations, and don't been fooled by the index term ( $k$  in the following example) and the summed term ( $b$  in the following example).

$$\sum_{k=a}^{a+2} b = \underset{k=a}{b} + \underset{k=a+1}{b} + \underset{k=a+1}{b} = 3b$$

In the above example, the exact value of  $a$  is NOT important, as long as it won't change during summation. The same idea applies to professors' solution. When doing

$$\sum_{j=i}^{3i+1} 1 = \underset{j=i}{1} + \underset{j=i+1}{1} + \dots + \underset{j=3i+1}{1} = (3i+1) - (i) + 1 = 2i + 2$$

$i$  won't change during the summation, which can be known by inspecting the code. The second equal sign can be got from a simple counting. I (TA) learned it when I was 10 years old.

**Problem 2**

Read the English again if you failed to catch the meaning of “minimize the maximum sum of a pair”. For example, if the input is  $\{1,9,5,3\}$ , one partition is  $\{1,9\}$  and  $\{5,3\}$ , and the maximum sum is  $\max(1+9, 5+3) = 10$ . Other partitions exist also, like  $\{1,5\}$  and  $\{9,3\}$ , whose output is  $\max(1+5, 9+3) = 12$ . The question asks, “How to pair to get the minimize  $\max(\dots)$  ? ”Once you grasp the meaning of questions, it's not hard to guess the correct answer.

**Problem 3(a)**

Sorting, a topic will be covered in the near future, needs some time. In fact, there is a lower bound,  $\Omega(n \log n)$ , for comparison-based sorting, which is covered on your textbook pp. 165-167. Namely, if you want to do something via sorting, the worse-case running time is at least  $O(n \log n)$ .

**Problem 4**

Don't forget the base case ( $n = 1$ ) in induction. If you know something about strong induction and weak induction, weak one is enough in this question. If not, ignore the previous sentence.