

CMSC 430 Practice Midterm Solutions

In grammars, capital letters represent nonterminals,
lower case letters represent terminals.
One sentence answers are sufficient for the “essay” questions.

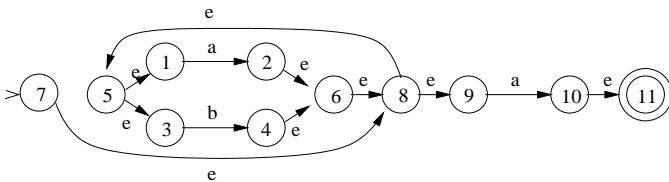
1. (6 points) Compiler front end.

- (a) What is the primary function of the scanner and what computational mechanism is used to accomplish it?
Break the input stream up into tokens using deterministic finite automata (DFA).
- (b) What is the primary function of the parser and what computational mechanism is used to accomplish it?
Provide syntactic structure to token stream using push-down automata (PDA = DFA + stack).
- (c) How do you decide what should be handled by the scanner versus the parser? (Hint: think of the complexity of languages)
Scanner handles simple constructs that can be easily described by regular expressions, parser handles more complicated syntax described by context-free grammars.

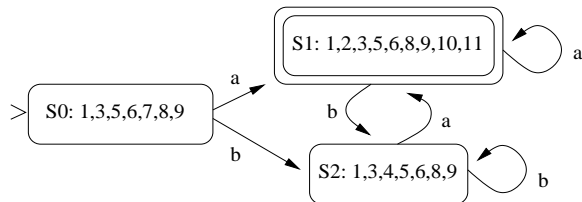
2. (20 points) Scanner construction.

- (a) Construct a regular expression for recognizing all non-empty strings composed of the letters a and b that do not end in b.
 $(a | b)^* a$

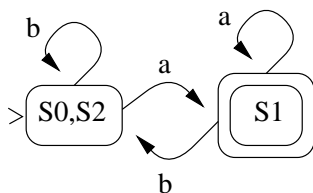
- (b) Convert the regular expression to an NFA using Thompson's construction algorithm.



- (c) Convert the NFA to a DFA (show the sets of NFA states for each DFA state).



- (d) Minimize the DFA (show the sets of DFA states for each minimized DFA state).



3. (16 points) Consider the following grammar:

$$E \rightarrow E + E | a$$

- (a) When is a grammar ambiguous?
When there are multiple left-most (or right-most) derivations of the same string.

- (b) Show that the grammar is ambiguous for the string $a + a + a$

<p><i>(leftmost derivation 1)</i></p> $E \Rightarrow E + E$ $\Rightarrow a + E$ $\Rightarrow a + E + E$ $\Rightarrow a + a + E$ $\Rightarrow a + a + a$	<p><i>(rightmost derivation 1)</i></p> $E \Rightarrow E + E$ $\Rightarrow E + a$ $\Rightarrow E + E + a$ $\Rightarrow E + a + a$ $\Rightarrow a + a + a$
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<p><i>(leftmost derivation 2)</i></p> $E \Rightarrow E + E$ $\Rightarrow E + E + E$ $\Rightarrow a + E + E$ $\Rightarrow a + a + E$ $\Rightarrow a + a + a$	<p><i>(rightmost derivation 2)</i></p> $E \Rightarrow E + E$ $\Rightarrow E + E + E$ $\Rightarrow E + E + a$ $\Rightarrow E + a + a$ $\Rightarrow a + a + a$
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- (c) What happens if you write a recursive-descent parser for this grammar?
May infinite loop trying to match E.
- (d) Fix the grammar to avoid this problem.

$$E \rightarrow a E'$$

$$E' \rightarrow + E E' | \epsilon$$

4. (16 points) Consider the following grammar:

$$S \rightarrow AB$$

$$A \rightarrow a | \epsilon$$

$$B \rightarrow b | \epsilon$$

- (a) Calculate FIRST for S, A, B:
- (b) Calculate FOLLOW for S, A, B:

Nonterminals	FIRST	FOLLOW
S	{ ϵ , a, b }	{ \$ }
A	{ ϵ , a }	{ b, \$ }
B	{ ϵ , b }	{ \$ }

- (c) Construct its recursive-descent parser (with lookahead), given the following functions:

```

tok; // current token

match(x) { // matches token
    if (tok != x) // if wrong token
        error(); // exit with error
    tok = getToken(); // get new token
}

parser() {
    tok = getToken(); // initialize
    S( ); // start symbol
    match("$"); // match EOF
}

```

Answer

```

S() {
  A(); B();
}
A() {
  if (tok == "a") // FIRST(b)
    match("a");
  else if ((tok == "b" || // FOLLOW(A)
           (tok == "$"))
           ;
  else
    error();
}
B() {
  if (tok == "b") // FIRST(b)
    match("b");
  else if (tok == "$") // FOLLOW(B)
    ;
  else
    error();
}

```

(b) Derive the canonical sets of LR(1) items

- State 0: [S → • E , { \$ }]
 [E → • E + E , { \$, + }]
 [E → • a , { \$, + }]
- State 1: [S → E • , { \$ }]
 [E → E • + E , { \$, + }]
- State 2: [E → a • , { \$, + }]
- State 3: [E → E + • E , { \$, + }]
 [E → • E + E , { \$, + }]
 [E → • a , { \$, + }]
- State 4: [E → E + E • , { \$, + }]
 [E → E • + E , { \$, + }]
- GOTO(0, E) = 1 GOTO(3, a) = 2
 GOTO(0, a) = 2 GOTO(3, E) = 4
 GOTO(1, +) = 3 GOTO(4, +) = 3

5. (6 points) Consider the following ACTION/GOTO tables:

State	Action		Goto	
	a	\$	A	B
0	shift 1	reduce B → ε	2	3
1	shift 3	reduce A → a	0	
2		accept	3	0
3	shift 1	accept		1

Show the contents of the stack and input buffer for the shift-reduce parse of "a", assuming State 0 is the start state:

Stack	Input	Action
\$ 0	a \$	shift 1
\$ 0 a 1	\$	reduce A → a
\$ 0 A	\$	goto[0,A] = 2
\$ 0 A 2	\$	accept

(c) Build the LR(1) parse table

State	Action			Goto E
	a	+	\$	
0	shift 2			1
1		shift 3	accept	
2		reduce P3 (E → a)	reduce P3 (E → a)	
3	shift 2			4
4		shift 3 reduce P2 (E → E + E)	reduce P2 (E → E + E)	

(d) For each shift/reduce or reduce/reduce conflict you find (if any), describe what would happen for the different ways to resolve the conflict(s).

For the shift/reduce conflict in state 4 with lookahead +, resolving the conflict in favor of reduce would make + left-associative; resolving it in favor of shift would make + right-associative.

6. (20 points) Consider the following augmented grammar:

P1	S	→	E
P2	E	→	E + E
P3			a

(a) Derive the canonical sets of LR(0) items

- State 0: [S → • E]
 [E → • E + E]
 [E → • a]
- State 1: [S → E •]
 [E → E • + E]
- State 2: [E → a •]
- State 3: [E → E + • E]
 [E → • E + E]
 [E → • a]
- State 4: [E → E + E •]
 [E → E • + E]
- GOTO(0, E) = 1 GOTO(3, a) = 2
 GOTO(0, a) = 2 GOTO(3, E) = 4
 GOTO(1, +) = 3 GOTO(4, +) = 3

7. (16 points) Consider the following sets of LR(1) items in the states of a LR(1) parser:

- State 0: [A → • a , b]
 [A → a • , c]
 [B → a • , b]
- State 2: [A → • a , c]
 [A → a • , b]
 [B → a • , a]
- State 1: [A → • a , a]
 [A → • a , b]
 [B → a • , b]
- State 3: [A → • a , b]
 [B → • a , b]

(a) Find all conflicts, listing state, pair of LR(1) items, and lookahead(s) causing conflict.

State 2, shift/reduce conflict on lookahead=a between [A → • a , c] and [B → a • , a]

(b) List states that would be merged in a LALR(1) parser.
 State 0 and 2

(c) List additional conflicts in the LALR(1) parser, if any.
 State 0&2, reduce/reduce conflict on lookahead=b between [A → a • , b] and [B → a • , b]

(d) What are the advantages of LALR over LR parsers?
 Smaller number of DFA states.