CMSC 132: OBJECT-ORIENTED PROGRAMMING II

Sorting

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Sorting

• Goal
  • Arrange elements in **predetermined** order
  • Based on **key** for each element
  • Derived from ability to **compare** two keys by size

• Properties
  • Stable $\Rightarrow$ relative order of **equal** keys unchanged
    • Stable: $3, 1, 4, 3, 3, 2 \rightarrow 1, 2, 3, 3, 3, 4$
    • Unstable: $3, 1, 4, 3, 3, 2 \rightarrow 1, 2, 3, 3, 3, 4$
  • In-place $\Rightarrow$ uses only constant additional space
  • External $\Rightarrow$ can efficiently sort large # of keys
Type of Sorting Algorithms

- Comparison-based and Linear Algorithms
- Comparison-based Algorithms
  - Only uses pairwise key comparisons
  - Proven lower bound of $O(n \log(n))$
  - Examples
    - $O(n^2)$ → Bubblesort, Selection sort, Insertion sort
    - $O(n \log(n))$ → Treesort, Heapsort, Quicksort, Mergesort
- Linear Algorithms - Uses additional properties of keys
  - Counting sort
  - Bucket (bin) sort
  - Radix sort
Bubble Sort

- Approach
  - Iteratively sweep through shrinking portions of list
  - Swap element $x$ with its right neighbor if $x$ is larger

- Performance
  - $O(n^2)$ average / worst case
Bubble Sort Example

Sweep 1

Sweep 2

Sweep 3

Sweep 4
Bubble Sort Code

```c
void bubbleSort(int[ ] a) {
    int outer, inner;
    for (outer = a.length - 1; outer > 0; outer--)
        for (inner = 0; inner < outer; inner++)
            if (a[inner] > a[inner + 1])
                swap(a, inner, inner+1);
}

void swap(int a[ ], int x, int y) {
    int temp = a[x];
    a[x] = a[y];
    a[y] = temp;
}
```

Swap with right neighbor if larger
Selection Sort

- **Approach**
  1. Iteratively sweep through shrinking portions of list
  2. Select smallest element found in each sweep
  3. Swap smallest element with front of current list

- **Performance**
  - $O(n^2)$ average / worst case
void selectionSort(int[] a) {
    int outer, inner, min;
    for (outer = 0; outer < a.length - 1; outer++) {
        min = outer;
        for (inner = outer + 1; inner < a.length; inner++) {
            if (a[inner] < a[min]) {
                min = inner;
            }
        }
        swap(a, outer, min);
    }
}
Tree Sort

- Approach
  - Insert elements in binary search tree
  - List elements using *inorder* traversal
- Performance
  - Binary search tree
    - $\mathcal{O}( n \log(n) )$ average case
    - $\mathcal{O}( n^2 )$ worst case
  - Balanced binary search tree
    - $\mathcal{O}( n \log(n) )$ average / worst case

```
{ 7, 2, 8, 5, 4 }
```
Heap Sort

• Approach
  1. Insert elements in heap
  2. Remove smallest element in heap, repeat
  3. List elements in order of removal from heap

• Performance
  • $O(n \log(n))$ average / worst case
Quick Sort

• Approach
  1. Select pivot value (near median of list)
  2. Partition elements (into 2 lists) using pivot value
  3. Recursively sort both resulting lists
  4. Concatenate resulting lists
  5. For efficiency pivot needs to partition list evenly

• Performance
  • $O(n \log(n))$ average case
  • $O(n^2)$ worst case
Quick Sort Algorithm

1. If list below size K
   • Sort w/ other algorithm
2. Else pick pivot \( x \) and partition S into
   • L elements < \( x \)
   • E elements = \( x \)
   • G elements > \( x \)
3. Quicksort L & G
4. Concatenate L, E & G
   • If not sorting in place
Quick Sort Example

Partition & Sort

Result
Quick Sort Code

```c
void quickSort(int[] a, int x, int y) {
    int pivotIndex;
    if ((y - x) > 0) {
        pivotIndex = partitionList(a, x, y);
        quickSort(a, x, pivotIndex - 1);
        quickSort(a, pivotIndex + 1, y);
    }
}

int partitionList(int[] a, int first, int last) {
    ... // partitions list and returns index of pivot
}
```
Quick Sort Code

```c
int partitionList(int a[], int first, int last) {
    int i, pivot, border;

    pivot = a[first];
    border = first;
    for (i = first + 1; i <= last; i++) {
        if (a[i] <= pivot) {
            border++;
            border++;
            swap(a, border, i);
        }
    }
    swap(a, first, border);
    return border;
}
```
Merge Sort

• Approach
  1. Partition list of elements into 2 lists
  2. Recursively sort both lists
  3. Given 2 sorted lists, **merge** into 1 sorted list
     • Examine head of both lists
     • Move smaller to end of new list

• Performance
  • O( n \log(n) ) average / worst case

• Used by Collections.sort
Merge Example

```
2 7
4 5 8
2
7
4 5 8
2 4
7
5 8
2 4 5 8
2 4 5
7
8
2 4 5 7
2 4 5 7 8
```
Merge Sort Example

Split

Merge
void mergeSort(int[] a, int x, int y) {
    int mid = (x + y) / 2;
    if (x != y) {
        mergeSort(a, x, mid);
        mergeSort(a, mid + 1, y);
        merge(a, x, y, mid);
    }
}

void merge(int[] a, int x, int y, int mid) {
    ... // merges 2 adjacent sorted lists in array
}
void merge(int[] a, int x, int y, int mid) {
    int j, size = y - x + 1, left = x, right = mid + 1;
    int[] tmp = new int[a.length];

    for (j = 0; j < size; j++)
        if (left > mid)
            tmp[j] = a[right++];
        else
            if (right > y || a[left] < a[right])
                tmp[j] = a[left++];
            else
                tmp[j] = a[right++];

    for (j = 0; j < size; j++)
        a[x + j] = tmp[j];
}
## Sorting Properties

<table>
<thead>
<tr>
<th>Name</th>
<th>Comparison Sort</th>
<th>Avg Case Complexity</th>
<th>Worst Case Complexity</th>
<th>In Place</th>
<th>Can be Stable</th>
</tr>
</thead>
<tbody>
<tr>
<td>Bubble</td>
<td>✓</td>
<td>$O(n^2)$</td>
<td>$O(n^2)$</td>
<td>✓</td>
<td>✓</td>
</tr>
<tr>
<td>Selection</td>
<td>✓</td>
<td>$O(n^2)$</td>
<td>$O(n^2)$</td>
<td>✓</td>
<td>✓</td>
</tr>
<tr>
<td>Tree</td>
<td>✓</td>
<td>$O(n \log(n))$</td>
<td>$O(n^2)$</td>
<td>✓</td>
<td></td>
</tr>
<tr>
<td>Heap</td>
<td>✓</td>
<td>$O(n \log(n))$</td>
<td>$O(n \log(n))$</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Quick</td>
<td>✓</td>
<td>$O(n \log(n))$</td>
<td>$O(n^2)$</td>
<td></td>
<td>✓</td>
</tr>
<tr>
<td>Merge</td>
<td>✓</td>
<td>$O(n \log(n))$</td>
<td>$O(n \log(n))$</td>
<td></td>
<td>✓</td>
</tr>
</tbody>
</table>
The President and Sorting

- [http://www.youtube.com/watch?v=k4RRi_ntQc8](http://www.youtube.com/watch?v=k4RRi_ntQc8)
Links

- Selection vs. Quicksort
  - [http://jtf.acm.org/demos/classroom/SortDemo.html](http://jtf.acm.org/demos/classroom/SortDemo.html)

- What different sorting algorithms sound like
  - [http://www.youtube.com/watch?v=t8g-iYGHpEA](http://www.youtube.com/watch?v=t8g-iYGHpEA)

- Sorting Algorithms
  - [http://maven.smith.edu/~thiebaut/java/sort/demo.html](http://maven.smith.edu/~thiebaut/java/sort/demo.html)