1. (50 points) Prove the following identity:

\[ n! = \int_0^1 (-\ln x)^n \, dx. \]

2. (50 points) Prove that for all \( n \geq 0 \), 2304 divides \( 7^{2n} - 48n - 1 \).