

Candidate Course Project Topics (CMSC 657)

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Abstract

This document is meant to provide some useful guideline and references for finding projects in the field of quantum information and computation. The selection is *not comprehensive* and subject to the author's personal knowledge on the topics (mistakes are possible). Each topic comes with a brief description and a few representative references.

It is totally fine to pursue project topics beyond this document. However, please do identify your topic and relevant references in your proposal. Please feel free to contact me if you have difficulty identifying a project topic.

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1 Quantum Information & Foundation

1. Understanding of quantum time-space and casual structure.
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 - A. Ambainis, Quantum walks and their algorithmic applications. arXiv: quant-ph/0403120
 - F. Magniez, A. Nayak, J. Roland, and M. Santha, Search via Quantum Walk. arXiv: quant-ph/0608026
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 - Quantum linear systems algorithm with exponentially improved dependence on precision by Andrew M. Childs, Robin Kothari, Rolando D. Somma, QIP 2016. arXiv:1511.02306
 - Quantum Algorithms for Approximating the Effective Resistances in Electrical Networks by Guoming Wang. arXiv:1311.1851.
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- A subexponential-time quantum algorithm for the dihedral hidden subgroup problem by Greg Kuperberg, SIAM Journal on Computing, Volume 35 Issue 1, 2005, Pages 170-188. arXiv:quant-ph/0302112
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4 Quantum Complexity

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5 Quantum Cryptography

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- Anand Natarajan, Thomas Vidick. Robust self-testing of many-qubit states. STOC 2017. arXiv:1610.03574.

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- Using Simon's Algorithm to Attack Symmetric-Key Cryptographic Primitives by Thomas Santoli, Christian Schaffner. arXiv:1603.07856.

6 Quantum Programming Languages

1. Foundations of Quantum Programming Languages.

- Quantum lambda calculus. Book chapter by Benoit Valiron and Peter Selinger. In Simon Gay and Ian Mackie, editors, Semantic Techniques in Quantum Computation, Cambridge University Press, pp. 135–172, 2009.

- Programming the quantum future by Benoit Valiron, Neil J. Ross, Peter Selinger, D. Scott Alexander, and Jonathan M. Smith. *Communications of the ACM* Vol. 58 No. 8, pages 52–61, 2015.
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 - Floyd–hoare logic for quantum programs by Mingsheng Ying. *ACM Transactions on Programming Languages and Systems (TOPLAS)*, Vol 33, Issue 6, pages 16.
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 - Model-Checking Linear-Time Properties of Quantum Systems by M. S. Ying, Y. J. Li, N. K. Yu, and Y. Feng. *ACM Transactions on Computational Logic*, 15(3) (2014), 22:1-22:31.
 - Invariants of quantum programs: characterisations and generation by Mingsheng Ying, Shenggang Ying, Xiaodi Wu. *POPL* 2017.
 - QWIRE: A Core Language for Quantum Circuits by Jennifer Paykin, Robert Rand, Steve Zdancewic. *POPL* 2017.

7 Fault-tolerant Quantum Computation

1. Fault-tolerant Quantum Computation.
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8 Near-term Quantum Devices

1. Establishing quantum supremacy, in theory or close-to-practical scenarios.
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- Average-case complexity versus approximate simulation of commuting quantum computations by Michael J. Bremner, Ashley Montanaro, Dan J. Shepherd. QIP 2016. arXiv:1504.07999.
 - Complexity-Theoretic Foundations of Quantum Supremacy Experiments by Scott Aaronson, Lijie Chen, arXiv:1612.05903. (CCC 2017)
 - Quantum computational supremacy by Aram W. Harrow, Ashley Montanaro. Nature 549, 203–209 (14 September 2017).
2. Architecture of quantum hardware.
 - An experimental microarchitecture for a superconducting quantum processor by X. Fu et al. Proceeding MICRO-50 '17 Proceedings of the 50th Annual IEEE/ACM International Symposium on Microarchitecture Pages 813-825. arXiv: 1708.07677.
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 - Taming the instruction bandwidth of quantum computers via hardware-managed error correction by S. Tannu. Proceeding MICRO-50 '17 Proceedings of the 50th Annual IEEE/ACM International Symposium on Microarchitecture Pages 679-691.
 3. Better classical algorithms to simulate quantum applications.
 - Classical boson sampling algorithms with superior performance to near-term experiments by A. Neville et al. Nature Physics (2017) arXiv:1705.00686.
 - The Classical Complexity of Boson Sampling by Peter Clifford and Raphael Clifford. SODA 2018. arXiv:1706.01260.

9 Explorative topics

Topics in this section have almost no research result yet. (Please do correct me if I am wrong.)

1. Implement a quantum algorithm with the publicly accessible quantum machines (or simulators), e.g., IBM Q Experience, Microsoft Q#, and so on. Design some measures to compare them.
2. Survey the hardware specifications of publicly accessible quantum machines. Think of any practical method to verify the real quantum machines against their claimed specifications.
3. Please tell me if you have any idea along this line.