Memory Management
Memory Management

• Background
• Swapping
• Contiguous Memory Allocation
• Segmentation
• Paging
• Structure of the Page Table
CPU and Memory

- Basic architecture of a computer system requires the CPU and the main memory.
- All programs and data accessed by the CPU during the execution of instructions is either in the registers or in the main memory.
  - For the discussion here we are going to ignore the presence of Cache Memory which many CPUs have today and whose presence is managed by the hardware transparently.
- For executing an instruction:
  - Instruction has to be fetched from the memory.
  - Operand(s) have to be fetched from the memory – if so required.
  - Results may have to be stored in memory – if so required.
- CPU may make multiple memory accesses for each instruction.
Background

• Program must be brought (from disk) into memory and placed within a process for it to be run
• Main memory and registers are only storage CPU can access directly
• Memory unit only sees a stream of addresses + read requests, or address + data and write requests
• Register access in one CPU clock (or less)
• Main memory can take many cycles, causing a stall
• Cache sits between main memory and CPU registers
• Protection of memory required to ensure correct operation
View of the memory

• An array of cells
• Each cell can store several bits (cell width)
  • 8- Byte
  • 16 – Half Word
  • 32 – Word
  • ..
• Cells are organized as a linear array with each cell having a unique address
• A memory cell is accessed by the CPU by presenting the address of the cell to the memory controller
Address Space

• The address of a cell consists of say $n$ bits. This gives $2^n$ unique addresses, from 0 to $(2^n - 1)$

• We can view this address space in *any logical organization* we desire, treating any number of contiguous cells as a group.

• When the number of such cells in a group is a power of 2 then the address can be decomposed easily into the group number and the cell within the group.
Mapping of Address Spaces

• We can map any address space, “A” into any other address space “B” as long as we can get a unique address for one given as address for the other.
  • Map one address to the other
  • Address spaces do not have to be of the same size. (Size defined by the number of bits required to specify a unique address.
  • Usually, the cell sizes are same but if they are not, a mapping there is required also.
    • One organized with cell size of one byte while the other with cell size of a word – 4 bytes

• How to map???
Mapping of address spaces

• How to map (Going from “A” to “B”)
  • Lookup table
    • Organized by cells
      • Each address in A has an entry for the address in B
      • Use A as an index in the array which as the corresponding address B
Desirable Features

• Very large address space
• Ability to execute partially loaded programs
• Dynamic Relocatability
• Sharing
• Protection

• Achieving these features require a variety of hardware and software support
Binding and Multiple Mappings

• Binding
  • Associating an address to a location in an address space

• Mapping
  • Translating one address to another address
  • Each address is defined in an address space
  • Mapping one address space to another address space

• Mapping is never done on Byte by Byte
  • A contagious portion is mapped on to a contagious portion
Address Binding

• Programs on disk, ready to be brought into memory to execute form an **input queue**
  • Without support, must be loaded into address 0000
• Inconvenient to have first user process physical address always at 0000
  • How can it not be?
• Further, addresses represented in different ways at different stages of a program’s life
  • Source code addresses usually symbolic
  • Compiled code addresses **bind** to relocatable addresses
    • i.e. “14 bytes from beginning of this module”
  • Linker or loader will bind relocatable addresses to absolute addresses
    • i.e. 74014
  • Each binding maps one address space to another
Binding of Instructions and Data to Memory

• Address binding of instructions and data to memory addresses can happen at three different stages
  • **Compile time**: If memory location known a priori, absolute code can be generated; must recompile code if starting location changes
  • **Load time**: Must generate relocatable code if memory location is not known at compile time
  • **Execution time**: Binding delayed until run time if the process can be moved during its execution from one memory segment to another
    • Need hardware support for address maps (e.g., base and limit registers)
Multistep Processing of a User Program
Dynamic Linking

• **Static linking** – system libraries and program code combined by the loader into the binary program image
• Dynamic linking – linking postponed until execution time
• Small piece of code, **stub**, used to locate the appropriate memory-resident library routine
• Stub replaces itself with the address of the routine, and executes the routine
• Operating system checks if routine is in processes’ memory address
  • If not in address space, add to address space
• Dynamic linking is particularly useful for libraries
• System also known as **shared libraries**
Dynamic Loading

• Routine is not loaded until it is called
• Better memory-space utilization; unused routine is never loaded
• Useful when large amounts of code are needed to handle infrequently occurring cases
• No special support from the operating system is required implemented through program design
Overlays

• Keep in memory only those instructions and data that are needed at any given time

• Needed when process is larger than amount of memory allocated to it

• Implemented by user, no special support needed from operating system, programming design of overlay structure is complex
Logical vs. Physical Address Space

• The concept of a logical address space that is bound to a separate physical address space is central to proper memory management
  • Logical address – generated by the CPU; also referred to as virtual address
  • Physical address – address seen by the memory unit

• Logical and physical addresses are the same in compile-time and load-time address-binding schemes; logical (virtual) and physical addresses differ in execution-time address-binding scheme

• Logical address space is the set of all logical addresses that can be generated by a program

• Physical address space is the set of all physical addresses that can be generated by a program
Memory-Management Unit (MMU)

• Hardware device that at run time maps virtual to physical address
• Many methods possible, covered in the rest of this chapter
• To start, consider simple scheme where the value in the relocation register is added to every address generated by a user process at the time it is sent to memory
  • Base register now called relocation register
  • MS-DOS on Intel 80x86 used 4 relocation registers
• The user program deals with logical addresses; it never sees the real physical addresses
  • Execution-time binding occurs when reference is made to location in memory
  • Logical address bound to physical addresses
Swapping

• A process can be **swapped** temporarily out of memory to a backing store, and then brought back into memory for continued execution
  • Total physical memory space of processes can exceed physical memory

• **Backing store** – fast disk large enough to accommodate copies of all memory images for all users; must provide direct access to these memory images

• **Roll out, roll in** – swapping variant used for priority-based scheduling algorithms; lower-priority process is swapped out so higher-priority process can be loaded and executed

• Major part of swap time is transfer time; total transfer time is directly proportional to the amount of memory swapped

• System maintains a **ready queue** of ready-to-run processes which have memory images on disk
Swapping (Cont.)

• Does the swapped out process need to swap back in to same physical addresses?
• Depends on address binding method
  • Plus consider pending I/O to / from process memory space
• Modified versions of swapping are found on many systems (i.e., UNIX, Linux, and Windows)
  • Swapping normally disabled
  • Started if more than threshold amount of memory allocated
  • Disabled again once memory demand reduced below threshold
Schematic View of Swapping

1. Swap out
2. Swap in
Context Switch Time including Swapping

• If next processes to be put on CPU is not in memory, need to swap out a process and swap in target process
• Context switch time can then be very high
• 100MB process swapping to hard disk with transfer rate of 50MB/sec
  • Swap out time of 2000 ms
  • Plus swap in of same sized process
  • Total context switch swapping component time of 4000ms (4 seconds)
• Can reduce if reduce size of memory swapped – by knowing how much memory really being used
  • System calls to inform OS of memory use via request_memory() and release_memory()
Context Switch Time and Swapping (Cont.)

• Other constraints as well on swapping
  • Pending I/O – can’t swap out as I/O would occur to wrong process
  • Or always transfer I/O to kernel space, then to I/O device
    • Known as double buffering, adds overhead

• Standard swapping not used in modern operating systems
  • But modified version common
    • Swap only when free memory extremely low
Contiguous Allocation

- Main memory must support both OS and user processes
- Limited resource, must allocate efficiently
- Contiguous allocation is one early method
- Main memory usually into two partitions:
  - Resident operating system, usually held in low memory with interrupt vector
  - User processes then held in high memory
  - Each process contained in single contiguous section of memory
Contiguous Allocation (Cont.)

• Relocation registers used to protect user processes from each other, and from changing operating-system code and data
  • Base register contains value of smallest physical address
  • Limit register contains range of logical addresses – each logical address must be less than the limit register
  • MMU maps logical address *dynamically*
  • Can then allow actions such as kernel code being *transient* and kernel changing size
Base and Limit Registers

• A pair of **base** and **limit registers** define the logical address space
• CPU must check every memory access generated in user mode to be sure it is between base and limit for that user
Hardware Support for Relocation and Limit Registers

CPU

limit register

relocation register

logical address

<

yes

physical address

no

trap: addressing error

memory
Dynamic relocation using a relocation register

- Routine is not loaded until it is called
- Better memory-space utilization; unused routine is never loaded
- All routines kept on disk in relocatable load format
- Useful when large amounts of code are needed to handle infrequently occurring cases
- No special support from the operating system is required
  - Implemented through program design
  - OS can help by providing libraries to implement dynamic loading
Multiple-partition allocation

- Degree of multiprogramming limited by number of partitions
- **Variable-partition** sizes for efficiency (sized to a given process’ needs)
- **Hole** – block of available memory; holes of various size are scattered throughout memory
- When a process arrives, it is allocated memory from a hole large enough to accommodate it
- Process exiting frees its partition, adjacent free partitions combined
- Operating system maintains information about:
  a) allocated partitions   b) free partitions (hole)
Dynamic Storage-Allocation Problem

How to satisfy a request of size $n$ from a list of free holes?

- **First-fit**: Allocate the *first* hole that is big enough

- **Best-fit**: Allocate the *smallest* hole that is big enough; must search entire list, unless ordered by size
  - Produces the smallest leftover hole
    - First-fit and best-fit better than worst-fit in terms of speed and storage utilization

- **Worst-fit**: Allocate the *largest* hole; must also search entire list
  - Produces the largest leftover hole
Fragmentation

• **External Fragmentation** – total memory space exists to satisfy a request, but it is not contiguous

• **Internal Fragmentation** – allocated memory may be slightly larger than requested memory; this size difference is memory internal to a partition, but not being used

• First fit analysis reveals that given $N$ blocks allocated, $0.5 \times N$ blocks lost to fragmentation
  • $1/3$ may be unusable -> **50-percent rule**
Fragmentation (Cont.)

• Reduce external fragmentation by **compaction**
  • Shuffle memory contents to place all free memory together in one large block
  • Compaction is possible *only* if relocation is dynamic, and is done at execution time

• I/O problem
  • Latch job in memory while it is involved in I/O
  • Do I/O only into OS buffers

• Now consider that backing store has same fragmentation problems
Memory Management Schemes from I

• The logical address space of a process must be resident in the physical memory when this process is executing

Desirable Features:
• Very large address space
• Ability to execute partially loaded programs
• Dynamic Relocatability
• Sharing
• Protection
Programmers View

• Each Module starts with address 0
• When linking/loading start from 0 again but only one module can be at location 0. Others have to be relocated.
• What if each module was treated independently.
Logical Address Space

• Single linear address space
  • Address is \((d)\) where \(d\) is a number between 0 and \(2^k - 1\), when address uses \(k\) bits.

• Segmented
  • Logical address space consists of a collection of segments where each segment is an independent linear address space
  • Address now consists of \((s,d)\) where \(s\) is the segment identifier and \(d\) an address in the linear address space of the segment
Segmentation

- Memory-management scheme that supports user view of memory
- A program is a collection of segments
  - A segment is a logical unit such as:
    - main program
    - procedure
    - function
    - method
    - object
    - local variables, global variables
    - common block
    - stack
    - symbol table
    - arrays
User’s View of a Program
Logical View of Segmentation

user space

physical memory space
Segmentation Architecture

• Logical address consists of a two tuple:
  <segment-number, offset>,

• **Segment table** – maps two-dimensional physical addresses; each table entry has:
  • **base** – contains the starting physical address where the segments reside in memory
  • **limit** – specifies the length of the segment

• **Segment-table base register (STBR)** points to the segment table’s location in memory

• **Segment-table length register (STLR)** indicates number of segments used by a program;
  segment number \( s \) is legal if \( s < STLR \)
Segmentation Architecture (Cont.)

• Protection
  • With each entry in segment table associate:
    • validation bit = 0 ⇒ illegal segment
    • read/write/execute privileges

• Protection bits associated with segments; code sharing occurs at segment level

• Since segments vary in length, memory allocation is a dynamic storage-allocation problem

• A segmentation example is shown in the following diagram
Segmentation Hardware

CPU

s d

<

yes

no

trap: addressing error

limit base

segment table

physical memory
Example of Segmentation
Sharing of Segments
Paging

• Used to map a linear, contiguous Logical Address Space on to (linear) Physical Address Space
• View physical memory consisting of fixed-sized blocks called frames
  • Size is power of 2, between 512 bytes and 16 Mbytes
• View logical memory consisting of blocks of same size called pages
• To run a program of size $N$ pages, need to find $N$ free frames and load program
• Set up a page table to translate logical to physical addresses
Paging Model of Logical and Physical Memory

- Logical memory:
  - page 0
  - page 1
  - page 2
  - page 3

- Page table:
  - page 0
    - 1
  - page 1
    - 4
  - page 2
    - 3
  - page 3
    - 7

- Physical memory:
  - frame number:
    - 0
      - page 0
    - 1
      - page 1
    - 2
      - page 2
    - 3
      - page 3

Address Translation Scheme

• Address generated by CPU is divided into:
  • **Page number** \((p)\) – used as an index into a **page table** which contains base address of each page in physical memory
  • **Page offset** \((d)\) – combined with base address to define the physical memory address that is sent to the memory unit

- For given logical address space \(2^m\) and page size \(2^n\)
Paging Hardware

CPU -> logical address

physical address -> f0000 ... 0000

f1111 ... 1111

physical memory

page table

p d

f d
Paging Example

\[ n=2 \text{ and } m=4 \quad 32\text{-byte memory and 4-byte pages} \]
Paging (Cont.)

- Calculating internal fragmentation
  - Page size = 2,048 bytes
  - Process size = 72,766 bytes
  - 35 pages + 1,086 bytes
  - Internal fragmentation of 2,048 - 1,086 = 962 bytes
  - Worst case fragmentation = 1 frame – 1 byte
  - On average fragmentation = 1 / 2 frame size
  - So small frame sizes desirable?
  - But each page table entry takes memory to track
  - Page sizes growing over time
    - Solaris supports two page sizes – 8 KB and 4 MB

- Process view and physical memory now very different
- By implementation process can only access its own memory
Free Frames

![Diagram showing free frames before and after allocation](image)

**Before allocation**

**After allocation**
Implementation of Page Table

• Page table is kept in main memory

• **Page-table base register** (*PTBR*) points to the page table

• **Page-table length register** (*PTLR*) indicates size of the page table

• In this scheme every data/instruction access requires two memory accesses
  • One for the page table and one for the data / instruction

• The *two memory* access problem can be helped some by the use of a special fast-lookup hardware cache called **associative memory** or **translation look-aside buffers** (TLBs)
Translation Lookaside Buffer

• Keep a list of translations
• Provide means for fast look up

<table>
<thead>
<tr>
<th>Page #</th>
<th>Frame #</th>
</tr>
</thead>
<tbody>
<tr>
<td>Page #</td>
<td>Frame #</td>
</tr>
<tr>
<td>Page #</td>
<td>Frame #</td>
</tr>
<tr>
<td>Page #</td>
<td>Frame #</td>
</tr>
<tr>
<td>Page #</td>
<td>Frame #</td>
</tr>
<tr>
<td>Page #</td>
<td>Frame #</td>
</tr>
<tr>
<td>Page #</td>
<td>Frame #</td>
</tr>
<tr>
<td>Page #</td>
<td>Frame #</td>
</tr>
<tr>
<td>Page #</td>
<td>Frame #</td>
</tr>
<tr>
<td>Page #</td>
<td>Frame #</td>
</tr>
</tbody>
</table>
Implementation of Page Table (Cont.)

• Some TLBs store **address-space identifiers (ASIDs)** in each TLB entry – uniquely identifies each process to provide address-space protection for that process
  • Otherwise need to flush at every context switch
• TLBs typically small (64 to 1,024 entries)
• On a TLB miss, value is loaded into the TLB for faster access next time
  • Replacement policies must be considered
  • Some entries can be **wired down** for permanent fast access
Associative Memory

- Associative memory – parallel search

<table>
<thead>
<tr>
<th>Page #</th>
<th>Frame #</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
</tr>
</tbody>
</table>

- Address translation (p, d)
  - If p is in associative register, get frame # out
  - Otherwise get frame # from page table in memory
Paging Hardware With TLB

[Diagram of paging hardware with TLB]

CPU → logical address

page number

frame number

TLB

TLB hit

TLB miss

page table

physical memory

physical address

April 2020
Effective Access Time

• Associative Lookup = $\varepsilon$ time unit
  • Can be < 10% of memory access time

• Hit ratio = $\alpha$
  • Hit ratio – percentage of times that a page number is found in the associative registers; ratio related to number of associative registers

• Consider $\alpha = 80\%$, $\varepsilon = 20$ns for TLB search, 100ns for memory access
  • The time for accessing TLB is often ignored as it is overlapped with memory access.

• **Effective Access Time (EAT)**

• Consider $\alpha = 80\%$, $\varepsilon = 20$ns for TLB search, 100ns for memory access
  • $EAT = 0.80 \times 100 + 0.20 \times 200 = 120$ns

• Consider more realistic hit ratio -> $\alpha = 99\%$, $\varepsilon = 20$ns for TLB search, 100ns for memory access
  • $EAT = 0.99 \times 100 + 0.01 \times 200 = 101$ns
Memory Protection

- Memory protection implemented by associating protection bit with each frame to indicate if read-only or read-write access is allowed
  - Can also add more bits to indicate page execute-only, and so on
- **Valid-invalid** bit attached to each entry in the page table:
  - “valid” indicates that the associated page is in the process’ logical address space, and is thus a legal page
  - “invalid” indicates that the page is not in the process’ logical address space
  - Or use page-table length register (PTLR)
- Any violations result in a trap to the kernel
Valid (v) or Invalid (i) Bit In A Page Table
Shared Pages

• **Shared code**
  • One copy of read-only (reentrant) code shared among processes (i.e., text editors, compilers, window systems)
  • Similar to multiple threads sharing the same process space
  • Also useful for interprocess communication if sharing of read-write pages is allowed

• **Private code and data**
  • Each process keeps a separate copy of the code and data
  • The pages for the private code and data can appear anywhere in the logical address space
Memory Management Schemes from II

• Segmentation
• Paging

• Address Translation Mechanisms

Desirable Features:
• Very large address space
• Ability to execute partially loaded programs
• Dynamic Relocatability
• Sharing
• Protection
Shared Pages

• **Shared code**
  - One copy of read-only (*reentrant*) code shared among processes (i.e., text editors, compilers, window systems)
  - Similar to multiple threads sharing the same process space
  - Also useful for interprocess communication if sharing of read-write pages is allowed

• **Private code and data**
  - Each process keeps a separate copy of the code and data
  - The pages for the private code and data can appear anywhere in the logical address space
Shared Code
Shared Pages Example
Structure of the Page Table

• Memory structures for paging can get huge using straight-forward methods
  • Consider a 32-bit logical address space as on modern computers
  • Page size of 4 KB ($2^{12}$)
  • Page table would have 1 million entries ($2^{32} / 2^{12}$)
  • If each entry is 4 bytes -> 4 MB of physical address space / memory for page table alone
    • That amount of memory used to cost a lot
    • Don’t want to allocate that contiguously in main memory

• Hierarchical Paging
• Hashed Page Tables
• Inverted Page Tables
Hierarchical Page Tables

• Break up the logical address space into multiple page tables
• A simple technique is a two-level page table
• We then page the page table
Two-Level Page-Table Scheme
Two-Level Paging Example

- A logical address (on 32-bit machine with 1K page size) is divided into:
  - a page number consisting of 22 bits
  - a page offset consisting of 10 bits

- Since the page table is paged, the page number is further divided into:
  - a 12-bit page number
  - a 10-bit page offset

- Thus, a logical address is page number page offset

<table>
<thead>
<tr>
<th>( p_1 )</th>
<th>( p_2 )</th>
<th>( d )</th>
</tr>
</thead>
<tbody>
<tr>
<td>12</td>
<td>10</td>
<td>10</td>
</tr>
</tbody>
</table>

- where \( p_1 \) is an index into the outer page table, and \( p_2 \) is the displacement within the page of the inner page table
- Known as forward-mapped page table
Address-Translation Scheme
64-bit Logical Address Space

• Even two-level paging scheme not sufficient
• If page size is 4 KB ($2^{12}$)
  • Then page table has $2^{52}$ entries
  • If two level scheme, inner page tables could be $2^{10}$ 4-byte entries
  • Address would look like

    ![Address Format Diagram]

    - Outer page table has $2^{42}$ entries or $2^{44}$ bytes
    - One solution is to add a 2$^{nd}$ outer page table
    - But in the following example the 2$^{nd}$ outer page table is still $2^{34}$ bytes in size
      • And possibly 4 memory access to get to one physical memory location
### Three-level Paging Scheme

<table>
<thead>
<tr>
<th>outer page</th>
<th>inner page</th>
<th>offset</th>
</tr>
</thead>
<tbody>
<tr>
<td>$p_1$</td>
<td>$p_2$</td>
<td>$d$</td>
</tr>
<tr>
<td>42</td>
<td>10</td>
<td>12</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>2nd outer page</th>
<th>outer page</th>
<th>inner page</th>
<th>offset</th>
</tr>
</thead>
<tbody>
<tr>
<td>$p_1$</td>
<td>$p_2$</td>
<td>$p_3$</td>
<td>$d$</td>
</tr>
<tr>
<td>32</td>
<td>10</td>
<td>10</td>
<td>12</td>
</tr>
</tbody>
</table>
Hashed Page Tables

• Common in address spaces > 32 bits
• The virtual page number is hashed into a page table
  • This page table contains a chain of elements hashing to the same location
• Each element contains (1) the virtual page number (2) the value of the mapped page frame (3) a pointer to the next element
• Virtual page numbers are compared in this chain searching for a match
  • If a match is found, the corresponding physical frame is extracted
• Variation for 64-bit addresses is clustered page tables
  • Similar to hashed but each entry refers to several pages (such as 16) rather than 1
  • Especially useful for sparse address spaces (where memory references are non-contiguous and scattered)
Hashed Page Table

logical address

\[ p \quad d \]

hash function

hash table

physical address

\[ r \quad d \]

\[ q \quad s \]

\[ p \quad r \]

\[ \ldots \]

physical memory
Inverted Page Table

• Rather than each process having a page table and keeping track of all possible logical pages, track all physical pages
• One entry for each real page of memory
• Entry consists of the virtual address of the page stored in that real memory location, with information about the process that owns that page
• Decreases memory needed to store each page table, but increases time needed to search the table when a page reference occurs
• Use hash table to limit the search to one — or at most a few — page-table entries
  • TLB can accelerate access
• But how to implement shared memory?
  • One mapping of a virtual address to the shared physical address
Inverted Page Table Architecture
Example: The Intel 32 and 64-bit Architectures

• Dominant industry chips

• Pentium CPUs are 32-bit and called IA-32 architecture

• Current Intel CPUs are 64-bit and called IA-64 architecture

• Many variations in the chips, cover the main ideas here
Example: The Intel IA-32 Architecture

• Supports both segmentation and segmentation with paging
  • Each segment can be 4 GB
  • Up to 16 K segments per process
  • Divided into two partitions
    • First partition of up to 8 K segments are private to process (kept in local descriptor table (LDT))
    • Second partition of up to 8K segments shared among all processes (kept in global descriptor table (GDT))
Example: The Intel IA-32 Architecture (Cont.)

• CPU generates logical address
  • Selector given to segmentation unit
    • Which produces linear addresses

• Linear address given to paging unit
  • Which generates physical address in main memory
  • Paging units form equivalent of MMU
  • Pages sizes can be 4 KB or 4 MB
Logical to Physical Address Translation in IA-32

- CPU
- logical address → segmentation unit
- linear address → paging unit
- physical address → physical memory

<table>
<thead>
<tr>
<th>page number</th>
<th>page offset</th>
</tr>
</thead>
<tbody>
<tr>
<td>$p_1$</td>
<td>$p_2$</td>
</tr>
<tr>
<td>10</td>
<td>10</td>
</tr>
</tbody>
</table>
Intel IA-32 Segmentation

logical address

selector | offset

descriptor table

segment descriptor

32-bit linear address
Intel IA-32 Paging Architecture

![Diagram of Intel IA-32 Paging Architecture](image-url)
32-bit address limits led Intel to create page address extension (PAE), allowing 32-bit apps access to more than 4GB of memory space.

- Paging went to a 3-level scheme.
- Top two bits refer to a page directory pointer table.
- Page-directory and page-table entries moved to 64-bits in size.
- Net effect is increasing address space to 36 bits – 64GB of physical memory.
Intel x86-64

- Current generation Intel x86 architecture
- 64 bits is ginormous (> 16 exabytes)
- In practice only implement 48 bit addressing
  - Page sizes of 4 KB, 2 MB, 1 GB
  - Four levels of paging hierarchy
- Can also use PAE so virtual addresses are 48 bits and physical addresses are 52 bits