Content Sensitive Analysis

Roadmap (Where are we?)

Last lecture

- LR(1) parsing
  - Building ACTION / GOTO tables
  - Shift / reduce and reduce / reduce conflicts
  - SLR(1), LR(1) parsers

This lecture

- Context-sensitive analysis
  - Motivation
  - Attribute grammars
    - Attributes
    - Evaluation order
  - Ad hoc Syntax-directed translation

Context-Sensitive Analysis: Beyond Syntax

There is a level of correctness that is deeper than grammar

```c
fie(a,b,c,d)
int a, b, c, d;
{ ... }
```

```c
fee() {
int f[3], g[0], h, i, j, k;
char *p;
fie(h, i, "ab", j, k);
k = f * i + j;
h = g[17];
printf("%s,%s\n", p, q);
p = 10;
}
```

To generate code, we need to understand its meaning!

What is wrong with this program?
(let me count the ways …)

- declared g[0], used g[17]
- wrong number of args to fie()
- "ab" is not an int
- wrong dimension on use of f
- undeclared variable q
- 10 is not a character string

All these errors are "deeper than syntax"

Beyond Syntax

To generate code, the compiler needs to answer many questions

- Is "x" a scalar, an array, or a function? Is "x" declared?
- Are there names that are not declared? Declared but not used?
- Which declaration of "x" does each use reference?
- Is the expression "x * y + z" type-consistent?
- In "a[i][k]", does a have three dimensions?
- Where can "z" be stored? (register, local, global, heap, static)
- In "f ← 10" , how should f be represented?
- How many arguments does "fie ()" take? What about "printf ()"?
- Does "*p" reference the result of a "malloc ()"?
- Do "p" & "q" refer to the same memory location?
- Is "x" defined before it is used?

Beyond Syntax

Telling the story

- The attribute grammar formalism is important
  - Succinctly makes many points clear
  - Sets the stage for actual, ad-hoc practice
- The problems with attribute grammars motivate practice
  - Non-local computation
  - Need for centralized information

We will cover attribute grammars, then move on to ad-hoc ideas

Beyond Syntax

These questions are part of context-sensitive analysis

- Answers depend on "values", not parts of speech
- Questions & answers involve non-local information
- Answers may involve computation

How can we answer these questions?

- Use formal methods
  - Context-sensitive grammars?
  - Attribute grammars?
- Use ad-hoc techniques
  - Symbol tables
  - Ad-hoc code

In scanning & parsing, formalism won; different story here.

These are beyond a CFG
Attribute Grammars

What is an attribute grammar?
- A context-free grammar augmented with a set of rules
- Each symbol in the derivation has a set of values, or attributes
- The rules specify how to compute a value for each attribute

Example grammar

```
Number  →  Sign List
Sign     →  +  |  –
List     →  List Bit  |  Bit
Bit      →  0  |  1
```

This grammar describes signed binary numbers. We would like to augment it with rules that compute the decimal value of each valid input string.

Add rules to compute the decimal value of a signed binary number.

<table>
<thead>
<tr>
<th>Productions</th>
<th>Attribution Rules</th>
</tr>
</thead>
</table>
| Number  →  Sign List | Sign.neg ← false  
|             |  If Sign.neg then Number.val ← – List.val  
|             |  else Number.val ← List.val  
| Sign     →  +  |  Sign.neg ← false  
|             |  If Sign.neg then Number.val ← – List.val  
|             |  else Number.val ← List.val  
| List     →  List Bit  |  List.pos ← List.pos + 1  
| Bit      →  0  |  Bit.val ← – List.val  
|           |  Bit.val ← List.val + Bit.val  

Symbol Attributes
- Number
  - val
- Sign
  - neg
- List
  - pos, val
- Bit
  - pos, val

Note:
- Semantic rules associated with production $A \rightarrow \alpha$ have to specify the values for all
  - synthesized attributes for $A$ (root)
  - inherited attributes for grammar symbols in $\alpha$ (children)
- Rules must specify local value flow!
- Terminals can be associated with values returned by the scanner. These input values are associated with a synthesized attribute.
- Starting symbol cannot have inherited attributes.

Examples

For "–1":
```
Number  →  Sign List  
      →  – List  
      →  – Bit  
       ⇒  – 1
```

```
Number  →  Sign List  
      →  – List Bit  
      →  – Bit  
       ⇒  – 101
```

For "–101":
```
Number  →  Sign List  
      →  – List Bit  
      →  – Bit  
       ⇒  – 101
```

We will use these two throughout the lecture.

`CS430`
Knuth suggested a data-flow model for evaluation:
- Independent attributes first
- Others in order as input values become available

One possible evaluation order:
1. List.pos
2. Sign.neg
3. Bit.pos
4. Bit.val
5. List.val
6. Number.val

Other orders are possible

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The Rules of the Game

- Attributes associated with nodes in parse tree
- Rules are value assignments associated with productions
- Attribute is defined once, using local information
- Label identical terms in production for uniqueness
- Rules & parse tree define an attribute dependence graph
  \[ \rightarrow \] Graph must be non-circular
This produces a high-level, functional specification

Synthesized attribute
  \[ \rightarrow \] Depends on values from children
Inherited attribute
  \[ \rightarrow \] Depends on values from siblings & parent

Using Attribute Grammars

Attribute grammars can specify context-sensitive actions
- Take values from syntax
- Perform computations with values
- Insert tests, logic, ...

Synthesized Attributes
- Use values from children & from constants
  - S-attributed grammars: synthesized attributes only
  - Evaluate in a single bottom-up pass
  - Good match to LR parsing

Inherited Attributes
- Use values from parent, constants, & siblings
  - L-attributed grammars: A \rightarrow X_1 X_2 X_n and each inherited attribute of X_i depends on
  - attributes of X_1 X_2 X_i-1, and
  - inherited attributes of A
  - Evaluate in a single top-down pass (left to right)
  - Good match for LL parsing

Evaluation Methods

Dynamic, dependence-based methods
- Build the parse tree
- Build the dependence graph
- Topological sort the dependence graph
- Define attributes in topological order

Rule-based methods
- Analyze rules at compiler-generation time
- Determine a fixed (static) ordering
- Evaluate nodes in that order

Oblivious methods
- Ignore rules & parse tree
- Pick a convenient order (at design time) & use it

This is the complete attribute dependence graph for “–101”.
It shows the flow of all attribute values in the example.
Some flow downward
\[ \rightarrow \] inherited attributes
Some flow upward
\[ \rightarrow \] synthesized attributes
A rule may use attributes in the parent, children, or siblings of a node
For “–101”

Inherited Attributes

Synthesized attributes

If we show the computation...
& then peel away the parse tree ...

The dependence graph must be acyclic.

All that is left is the attribute dependence graph. This succinctly represents the flow of values in the problem instance. The dynamic methods sort this graph to find independent values, then work along graph edges. The rule-based methods try to discover “good” orders by analyzing the rules. The oblivious methods ignore the structure of this graph.

The dependence graph must be acyclic.
We can prove that some grammars can only generate instances with acyclic dependence graphs.

- Largest such class is "strongly non-circular" grammars (SNC)
- SNC grammars can be tested in polynomial time

Many evaluation methods discover circularity dynamically
⇒ Bad property for a compiler to have

SNC grammars were first defined by Kennedy & Warren

An Extended Example

Grammar for a basic block

Properties of the example grammar

- All attributes are synthesized ⇒ S-attributed grammar
- Rules can be evaluated bottom-up in a single pass
  → Good fit to bottom-up shift/reduce parser
- Easily understood solution
- Seems to fit the problem well

What about an improvement?

- Values are loaded only once per block (not at each use)
- Need to track which values have been already loaded

Things will get more complicated.

A Better Execution Model

Adding load tracking

- Need sets Before and After for each production
- Must be initialized, updated, and passed around the tree

A sample production

These copy rules multiply rapidly
Each creates an instance of the set
Lots of work, lots of space, lots of rules to write
The Moral of the Story

• Non-local computation needed lots of supporting rules
• “Complex” local computation is relatively easy

The Problems

• Copy rules increase cognitive overhead
• Copy rules increase space requirements
  → Need copies of attributes
• Result is an attributed tree
  → Must build the parse tree
  → Either search tree for answers or copy them to the root

The Realist’s Alternative

Ad-hoc syntax-directed translation

• Associate pieces of code with each production
• At each reduction, the corresponding code is executed
• Allowing arbitrary code provides complete flexibility
  → Includes ability to do tasteless & bad things

To make this work

• Need names for attributes of each symbol on lhs & rhs
  → Typically, one attribute passed through parser + arbitrary code
  → Yacc introduced $1, $2, … $n
• Need an evaluation scheme
  → Fits nicely into LR(1) parsing algorithm

Addressing the Problem

What would a good programmer do?

• Introduce a central repository for facts
• Table of names
  → Field in table for loaded/not loaded state
• Avoids all the copy rules, allocation & storage headaches
• All inter-assignment attribute flow is through table
  → Clean, efficient implementation
  → Good techniques for implementing the table (hashing, § B.4)
• When its done, information is in the table !
  → Cures most of the problems

• Unfortunately, this design violates the functional paradigm
  → Do we care?

Reworking the Example

(with load tracking)

Start → Init Block
Init → ε
Blocki → Block, Assign
Assign → Assign | Ident = Expr
| Expr, + Term
| Expr, * Term
| Term
| Term, + Factor
| Term, / Factor
| Factor
| ( Expr )
| Number
| Identifier

This looks cleaner & simpler than the AG sol’n !

One missing detail: initializing “cost” (we ignore Table[ ] for now)

Reworking the Example

(with load tracking)

This version passes the values through attributes. It avoids the need for initializing "cost"

However, Table[ ] still needs to be initialized

... and so on asi in the previous version of the example ...

• Before parser can reach Block, it must reduce Init
• Reduction by Init sets cost to zero

This is an example of splitting a production to create a reduction in the middle — for the sole purpose of hanging an action routine there (marker production)!
Example — Building an Abstract Syntax Tree

- Assume constructors for each node
- Assume stack holds pointers to nodes
- Assume yacc syntax

<table>
<thead>
<tr>
<th>Goal</th>
<th>Expr</th>
<th>$S = $1;</th>
</tr>
</thead>
<tbody>
<tr>
<td>Expr</td>
<td>Expr + Term</td>
<td>$S = \text{MakeAddNode}($1,$3);</td>
</tr>
<tr>
<td></td>
<td>Expr - Term</td>
<td>$S = \text{MakeSubNode}($1,$3);</td>
</tr>
<tr>
<td>Term</td>
<td>Term * Factor</td>
<td>$S = \text{MakeMulNode}($1,$3);</td>
</tr>
<tr>
<td></td>
<td>Term / Factor</td>
<td>$S = \text{MakeDivNode}($1,$3);</td>
</tr>
<tr>
<td>Factor</td>
<td>$S = $1;</td>
<td></td>
</tr>
</tbody>
</table>

Typical Uses (Semantic Analysis)

- Building a symbol table
  -> Enter declaration information as processed
  -> At end of declaration syntax, do some post processing
  -> Use table to check errors as parsing progresses

- Simple error checking/type checking
  -> Define before use, lookup on reference
  -> Dimension, type, ... check as encountered
  -> Type conformability of expression -> bottom-up walk
  -> Procedure interfaces are harder
    - Build a representation for parameter list & types
    - Check actual vs. formal parameter list
    - Positional or keyword associations

Making Ad-hoc Syntax Directed Translation Work

How do we fit this into an LR(1) parser?
- Need a place to store the attributes
  -> Stash them in the stack, along with state and symbol
  -> Push three items each time, pop 3 x (|β| - n) symbols
- Need a naming scheme to access them
  -> $n transnslates into stack location: top - 3 x (|β| - n)
- Need to sequence rule applications
  -> On every reduce action, perform the action rule

What about a rule that must work in mid-production?
- Can transform the grammar
  -> Split it into two parts at the point where rule must go
  -> Introduce marker productions $M \rightarrow \varepsilon$ with appropriate action

Reality

Most parsers are based on this ad-hoc style of context-sensitive analysis

Advantages
- Addresses the shortcomings of the AG paradigm
- Efficient, flexible

Disadvantages
- Must write the code with little assistance
- Programmer deals directly with the details

Most parser generators support a yacc-like notation

Is This Really "Ad-hoc"?

Relationship between practice and attribute grammars

Similarities
- Both rules & actions associated with productions
- Application order determined by tools
- (Somewhat) abstract names for symbols

Differences
- Actions applied as a unit; not true for AG rules
- Anything goes in ad-hoc actions; AG rules are (purely) functional
- AG rules are higher level than ad-hoc actions