Problem 1. Use mathematical induction to show the following:

(a) \[ \sum_{i=1}^{n} i(i + 1) = \frac{n(n + 1)(n + 2)}{3} \]

(b) \[ \sum_{i=0}^{n} 2^i = 2^{n+1} - 1 \]

Problem 2.

(a) Assume \( b^x = a \). What is \( x \) (in terms of \( a \) and \( b \))? 

(b) Using only part (a), show that \( \log_c(ab) = \log_c a + \log_c b \).

(c) Show that \( a^{\log_b n} = n^{\log_b a} \).

Problem 3. Differentiate the following functions:

(a) \( \ln(x^2 + 5) \)

(b) \( \lg(x^2 + 5) \) [NOTE: \( \lg x = \log_2 x \).]

(c) \( \frac{1}{\ln(x^2 + 5)} \)

Problem 4. Integrate the following functions:

(a) \( \frac{1}{x} \)

(b) \( \frac{1}{3x+7} \)

(c) \( \ln x \) [HINT: Use integration by parts.]

(d) \( x \ln x \) [HINT: Use integration by parts.]

(e) \( x \lg x \)