

*Closed book. Closed notes. No electronic device.*

### Conventions

$[sk, pk]$	public-key pair
$E_P(pk, x)$	public-key encryption of $x$ with public key $pk$
$Sgn(sk, x)$	public-key signature of $x$ with secret key $sk$
$E_{AES}(s, x)$	symmetric-key AES block encryption with key $s$
$D_{AES}(s, x)$	symmetric-key AES block decryption with key $s$
$E(s, x)$	symmetric-key CBC-AES (CBC mode using AES) encryption of $x$ with key $s$
$D(s, x)$	symmetric-key CBC-AES (CBC mode using AES) decryption of $x$ with key $s$
$MAC(s, x)$	symmetric-key MAC (ECBC) of $x$ with key $s$
$H(x)$	SHA-256 hash function of $x$
$HMAC(k, x)$	HMAC of $x$ using key $k$ and $H$
$H^k(x)$	$k$ -fold hash: $H(H(\dots H(x)\dots))$

1.

AES
Authenticity
Block cipher
Collision resistant
CA
Certificate
Certificate chain
CRL
Confidentiality
DES
Diffie-Helman
Dictionary attack
Euclid's algorithm
Eucler's theorem
Existential forgery
HMAC
Integrity
KDC
MAC
Mode
CBC
CTR
OFB
Non-repudiation
OCSP
OCSP stapling
One-time pad
Pre-image resistant
PGP
PKCS
PKI
RSA
Session key
Signing
Ticket
Totient function
Verification

For each description below, give **one** term that *best* describes it. **In many cases, but not all, the term will be in the table at left. In each case, give only one answer of at most 4 words (otherwise you get zero).**

- This ensures that the data can be read only by the intended receiver.
- This ensures that any modification to the data is detected by the intended receiver.
- This ensures that data received was sent by the specified sender.
- This ensures that a third party can verify that the data was sent by the specified sender.
- This kind of crypto uses different keys for encryption and decryption.
- The attack model in which the attacker has access to an encryption oracle but not a decryption oracle.
- This symmetric block cipher supports only one key size.
- This symmetric block cipher supports multiple key sizes.
- This defines how to use a block cipher on arbitrary-size data.
- This ensures that encrypting the same message more than once results in different ciphertext.
- This mode allows the block cipher encryption function calls to be made before the data is available.
- This mode allows encryption to be done in parallel.
- This mode allows a hash function to be used for encryption of arbitrary-size data.
- The property of a hash function that makes it hard to find a message  $m$  that hashes to a given number.
- This is the standard method for generating MACs from block ciphers.
- This is the standard method for generating MACs from hash functions.
- This is the set of integers in  $1, \dots, n - 1$  that are relatively prime to  $n$ .
- This is the number of integers in  $1, \dots, n - 1$  that are relatively prime to  $n$ .
- What do we need to efficiently compute the number of integers in  $1, \dots, n - 1$  that are relatively prime to  $n$ .
- What allows us to efficiently compute  $\phi(n)$ .
- An attack that goes through a set of candidate passwords.
- This means that after a session-key is forgotten by the principals that used it, no one can decrypt data encrypted with that key.
- A public-key infrastructure that is not hierarchical.

**2.** Alice has an account with a server. The server makes her change her password every few months, to which Alice just increments a number in her password, e.g., `pwd1`, `pwd2`, `...`.

Why does the server not complain that the new password is very much like her old one?

**3.** Let  $[e, n]$  be the RSA public key of a server. Suppose someone gives you the prime factors of  $n$ , say  $p$  and  $q$ . Can you obtain the private key  $[d, n]$ ? If not, explain briefly. If yes, briefly give the steps.

**4.** A hash function  $H()$  generates a 256-bit hash. How many random messages on average would one have to hash before finding two distinct messages that hash to the same value.

**5.** Is a strong password significantly better than a weak password against an online dictionary attack.

**6.** Is a strong password significantly better than a weak password against an offline dictionary attack.

**7.** A server has  $N$  users and stores hashes of the users' passwords in a map  $P$  indexed by user id. Specifically, for user  $u$ , the entry  $P(u)$  is  $H^4(p)$ , where  $p$  is  $u$ 's password.

- What would the entry be if you "salted" the entries.
- If  $N$  is 20, does salting improve security significantly? Explain briefly.

**8.** Let  $x$  be an element of  $Z_n$  and  $y$  denote its multiplicative-inverse-mod- $n$ .

- When does  $y$  exist?
- Give the equation that  $x$  and  $y$  satisfy.

**9.** Let message  $msg$  consist of blocks  $[m_1, \dots, m_n]$ . Let  $[c_0, c_1, \dots, c_n]$  be the ciphertext resulting from encrypting  $msg$  using AES with key  $k$  in some mode.

- Assume CBC mode. Give  $c_i$  as a function of the plaintext, key,  $E_{AES}()$  and/or  $D_{AES}()$ , for  $i = 1, \dots, n$ .
- Repeat part a for CTR mode.

**10.** For an arbitrary-size message  $msg$ , let  $M(k, msg)$  denote the last block of CBC-AES encryption using key  $k$  and  $IV = 0$ . Is  $M(k, msg)$  a secure MAC. If you answer yes, explain briefly. If you answer no, give a counter example.

**11.** Why is a random pad needed for RSA encryption of a msg.

**12.** Server  $B$  has a well-known fixed IP address and TCP port, and no other service can use that address and port. User  $A$  shares a password, say  $pwd$  with  $B$ .  $A$  connects as follows:

- Establish a shared key  $s$  with a standard (not authenticated) Diffie-Helman.
- Send  $["A", pwd]$  encrypted with key  $s$  to the server.
- $B$  authenticates the user if the password matches.

- Assume an attacker that can only eavesdrop on messages. Does the above ensure that key  $s$  is securely shared between  $A$  and  $B$ . If you answer "no", give an attack. If you answer "yes", explain.
- Repeat part a for an attacker that can eavesdrop and tamper with messages (intercept and change them).

- 13.** A domain has a CA  $X$ , which is the trust anchor for the domain's users.
- What steps does a new user, say  $A$ , take upon joining the domain.
  - What steps are taken when a user, say  $A$ , leaves the domain.
  - What steps are taken when  $X$ 's secret key is exposed.
- 14.** The users in domain  $x.com$  has a CA  $X$  as trust anchor. The users in domain  $y.com$  has a CA  $Y$  as trust anchor. One day,  $x.com$  and  $y.com$  are acquired by  $z.com$ , which has a CA  $Z$  as trust anchor. List the steps that will allow users in all three domains to talk to each other. Minimize the number of new certificates that are issued.
- 15.** A domain's authentication is handled by KDC  $X$ .
- What steps does a new user, say  $A$ , take upon joining the domain.
  - What steps are taken when a user, say  $A$ , leaves the domain.
  - What steps are taken when  $X$ 's key (used to encrypt its user-key table) is exposed.
- 16.** A domain's authentication is handled by KDC  $X$ . Tickets can have long expiry times. Consider the following:
- $A$  gets a post-dated ticket  $T$  from the KDC to interact with server  $B$ .
  - $B$  changes its master key with the KDC.
  - $A$  presents  $T$  to  $B$ .

What is the problem here? What is a solution?

### 17. Authentication protocols

This problem has independent parts. Each part describes an authentication protocol that Alice ( $A$ ) initiates to send a message  $m$  to Bob ( $B$ ), and then asks one or more questions. Answer each question by circling *YES* or *NO*.

The first question asks whether the protocol is *broken*, i.e., does it require Alice or Bob to do something they cannot (e.g., decrypt a message without the key).

- If you answer *YES* to the first question, *skip the remaining questions in that part*. You will get full marks if your answer is correct, and zero otherwise.
- If you answer *NO* to the first question, *attempt to answer all the remaining questions in that part*. For each question, you will get 1 point if your answer is correct, zero points if you do not answer, and **-1 point if your answer is wrong**.

Alice has public-key pair  $[sk_A, pk_A]$ . Bob has  $pk_A$ .

Bob has public-key pair  $[sk_B, pk_B]$ . Alice has  $pk_B$ .

Alice and Bob also share a symmetric key  $S_{AB}$

Unless otherwise stated, symmetric keys are strong, and the attacker can eavesdrop and tamper with messages.

#### 17.1.

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A: generate a new symmetric key  $s$   
 send  $[E_P(pk_B, s), E(s, m), \text{Sgn}(sk_A, H(m))]$       B: receive message; extract  $m$

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- |  |     |    |
|--|-----|----|
| • Is the protocol broken?  | yes | no |
| • Is confidentiality satisfied for $m$ ?   | yes | no |
| • Is integrity satisfied for $m$ ?   | yes | no |
| • Is non-repudiation satisfied for $m$ ?   | yes | no |
| • Is perfect forward secrecy satisfied for $m$ ?                                   | yes | no |
| • If $s$ comes from a password, is $m$ vulnerable to an offline dictionary attack? | yes | no |

**17.2.**


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<p>A: generate random <math>c_A</math>  <math>n_A \leftarrow E(S_{AB}, c_A)</math>  send <math>[n_A]</math></p>	<p>B: receive message  <math>c_A \leftarrow D(S_{AB}, n_A)</math>  <math>r_A \leftarrow E(S_{AB}, c_A + 1)</math>  generate random <math>c_B</math>  <math>n_B \leftarrow E(S_{AB}, c_B)</math>  send <math>[r_A, n_B]</math></p>
<p>A: receive message  if <math>(D(S_{AB}, r_A) \neq c_A + 1)</math> "FAIL"  <math>c_B \leftarrow D(S_{AB}, n_B)</math>  <math>r_B \leftarrow E(S_{AB}, c_B + 1)</math>  session key <math>x \leftarrow c_A \oplus c_B</math>  send <math>[r_B, E(x, m), \text{MAC}(x, m)]</math></p>	<p>B: receive message  if <math>(D(S_{AB}, r_B) \neq c_B + 1)</math> "FAIL"  extract msg <math>m</math></p>

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|---|-----|----|
| • Is the protocol broken?   | yes | no |
| • Is confidentiality satisfied for $m$ ?  | yes | no |
| • Is integrity satisfied for $m$ ?  | yes | no |
| • Is non-repudiation satisfied for $m$ ?  | yes | no |
| • Is perfect forward secrecy satisfied for $m$ ?  | yes | no |
| • If $S_{AB}$ comes from a password, is $m$ vulnerable to an offline dictionary attack: | yes | no |

**17.3.**


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<p>A: generate Diffie-Helman parameters <math>p</math> and <math>g</math>  generate random <math>x</math>  <math>T_A \leftarrow g^x \text{mod-} p</math>  send <math>[T_A]</math></p>	<p>B: receive message  generate random <math>y</math>  <math>T_B \leftarrow g^y \text{mod-} p</math>  <math>s \leftarrow T_A^y</math>  send <math>[T_B]</math></p>
<p>A: receive message  <math>s \leftarrow T_B^x</math>  send <math>[E(s, m)]</math></p>	<p>B: receive message  extract msg <math>m</math></p>

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|--|-----|----|
| • Is the protocol broken?                        | yes | no |
| • Is confidentiality satisfied for $m$ ?         | yes | no |
| • Is integrity satisfied for $m$ ?               | yes | no |
| • Is non-repudiation satisfied for $m$ ?         | yes | no |
| • Is perfect forward secrecy satisfied for $m$ ? | yes | no |

**17.4.** Repeat 17.3 assuming the attacker can only eavesdrop (but not tamper).

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|--|-----|----|
| • Is the protocol broken?                        | yes | no |
| • Is confidentiality satisfied for $m$ ?         | yes | no |
| • Is integrity satisfied for $m$ ?               | yes | no |
| • Is non-repudiation satisfied for $m$ ?         | yes | no |
| • Is perfect forward secrecy satisfied for $m$ ? | yes | no |