Midterm 2
CMSC 430
Introduction to Compilers
Fall 2012

November 28, 2012

Instructions

This exam contains 9 pages, including this one. Make sure you have all the pages. Write your name on the top of this page before starting the exam.

Write your answers on the exam sheets. If you finish at least 15 minutes early, bring your exam to the front when you are finished; otherwise, wait until the end of the exam to turn it in. Please be as quiet as possible.

If you have a question, raise your hand. If you feel an exam question assumes something that is not written, write it down on your exam sheet. Barring some unforeseen error on the exam, however, you shouldn’t need to do this at all, so be careful when making assumptions.

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<th>Question</th>
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Question 1. Short Answer (20 points).

a. (6 points) Briefly explain what a basic block is.

Answer:
A basic block is a sequence of statements such that (a) there are no jumps from the basic block except after its last statement and (b) there are no jumps into the basic block except to its initial statement.

b. (7 points) Briefly explain what state transformation is in dynamic software updating and why it may be needed.

Answer:
State transformation is the process of modifying the application state to be compatible with a new program version. State transformation is needed because often code updates code with data representation and type changes.
c. (7 points) Briefly explain what a time travel debugger is.
Question 2. Subtyping (14 points). Suppose that int is a subtype of float. To save writing, let’s write i for int and f for float.

a. (7 points) Write down every type $t$ such that $t \leq (i \rightarrow i \rightarrow f)$, following standard subtyping rules. Hint: It may be easiest to write down everything that could possibly be a subtype and then cross out the ones that aren’t subtypes.

b. (7 points) In class, we argued it would be unsound to allow int ref $\leq$ float ref. Demonstrate the issue by writing down, in OCaml notation, a program that would type check under this subtyping rule but that would “go wrong” with a type error at run-time. Explain your answer very briefly.
**Question 3. Interval Analysis (30 points).** In this question, we will develop an *interval analysis*, which, for each variable $x$ at each program point, determines a closed interval $[a, b]$ such that the run-time value of $x$ is guaranteed to be in the interval $[a, b]$. We also allow $a$ and $b$ to be $-\infty$ and $\infty$, respectively, in case we cannot bound the interval on one or both sides. Use $\emptyset$ for the empty interval. For example, here is a CFG annotated with the intervals determined after each statement (empty intervals omitted):

```
/ \  
|  |  
x := 42  x ∈ [42, 42]  
  \  |
   \ /
   x := x + 3  x ∈ [45, 45]  
       |  
       x := 5  x ∈ [5, 5]  
          |  
          y := x - 1  x ∈ [5, 45], y ∈ [4, 44]  
             |  
             x := x - 1  x ∈ [-∞, 44], y ∈ [4, ∞]  
                |  
                y := y + 1  x ∈ [-∞, 44], y ∈ [4, ∞]  
                   |  
                   z := x + y  x ∈ [-∞, 44], y ∈ [4, ∞], z ∈ [-∞, ∞]
```

Note that we have left out any conditional tests; as is usual in dataflow analysis, your analysis should always assume all branches could be taken.

**a. (5 points)** Should the analysis be forward or backward?

**b. (5 points)** What should the initial facts be at the entry or exit of the program? (You can explain in words.)

**c. (5 points)** What should $\top$ be in the lattice? (You can explain in words.)
d. (5 points) Suppose that on one incoming edge to a join point, \( x \in [a, b] \), and on another incoming edge to the same point, \( x \in [c, d] \). What should \((x \in [a, b]) \cap (x \in [c, d])\) be defined as?

Answer: \( x \in [\min(a, c), \max(b, d)] \).

e. (5 points) Suppose \( x \in [a, b] \) just prior to each of the following statements. Write down the new dataflow fact \( x \in [c, d] \) after the statements:

i. \( x := 42 \)

Answer: \( x \in [42, 42] \)

ii. \( x := x + 1 \)

Answer: \( x \in [a + 1, b + 1] \)

iii. \( x := 4 - x \)

Answer: \( x \in [-b + 4, -a + 4] \)

f. (5 points) If we implement the usual dataflow analysis algorithm, is the algorithm guaranteed to terminate? Why or why not?
Question 4. Data flow analysis (12 points). Here is the control-flow graph from the last problem again, this time with numbers for each statement:

![Control-flow graph](image)

a. (6 points) Write down the sets of live variables at the *beginning* of each statement. Write $\emptyset$ for the empty set, if necessary.

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<th>Live variables at beginning of stmt</th>
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b. (6 points) Write down the sets of reaching definitions at the *end* of each statement. Write $\emptyset$ for the empty set, if necessary.

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Question 5. Code generation and register allocation (24 points). Below is a snippet of 08-codegen-2.ml from class, showing the input expression language, the “bytecode” instruction language, and compilation. We’ve made two small changes: We renamed ‘L_Register to ‘L_Reg to save some writing; and we removed reads and writes through pointers and identifiers.

```ml
type expr =
| EInt of int
| EAdd of expr * expr
| ESub of expr * expr
| EMul of expr * expr
| EIfZero of expr * expr * expr

let rec comp_expr (st:('L_Reg of int) list) = function
| EInt n ->
    let r = next_reg () in
    (r, [ILoad ('L_Reg r, 'L_Int n)])
| EIfZero (e1, e2, e3) ->
    let (r1, p1) = comp_expr st e1 in
    let (r2, p2) = comp_expr st e2 in
    let (r3, p3) = comp_expr st e3 in
    let r = next_reg () in
    (r, p1 @
    [ IIfZero ('L_Reg r1, (2+(List.length p3)))
    ] @
    p3 @
    [IMov ('L_Reg r, 'L_Reg r1);
    IJmp (1+(List.length p2))]
    @
    p2 @
    [IMov ('L_Reg r, 'L_Reg r2)]
    )
```

| a. (14 points) Suppose we extend the source language with short-circuiting disjunction EOr(e1, e2) that does the following: First, it evaluates expression e1 to produce a value v. If v is non-zero, then v is returned as the value of the disjunction. Otherwise, expression e2 is evaluated and its value is returned. For example, EOr (EInt 1, EInt 2) evaluates to 1, and EOr (EInt 0, EInt 2) evaluates to 2. (Notice that e2 is not evaluated if e1 is non-zero.)

Write a case of comp_expr that compiles EOr.

```ml
let rec comp_expr (st:('L_Reg of int) list) = function
| ... |
| EOr (e1, e2) ->
```
b. (10 points) Finally, consider the following slight modification of the CFG from the earlier problems:

\[
\begin{align*}
    x_0 &:= 42 \\
    x_1 &:= x_0 + 3 \\
    y_0 &:= x_1 - 1 \\
    x_2 &:= x_1 \\
    y_1 &:= y_0 \\
    x_2 &:= x_2 - 1 \\
    6. y_1 &:= y_1 + 1 \\
    7. z_0 &:= x_2 + y_1
\end{align*}
\]

Draw the interference graph for the variables referred to in the above CFG. After you have drawn the graph, “color” it by labeling nodes with colors \(a\), \(b\), \(c\), \(d\), etc., using the minimal number of colors possible.