CMSC 330: Organization of Programming Languages

Functional Programming with Lists

CMSC 330 - Spring 2020

Lists in OCaml

- The basic data structure in OCaml
 - Lists can be of arbitrary length
 - Implemented as a linked data structure
 - Lists must be homogeneous
 - All elements have the same type
- Operations
 - Construct lists
 - Destruct them via pattern matching

Constructing Lists

Syntax

- [] is the empty list (pronounced "nil")
- e1::e2 prepends element e1 to list e2
 - Operator :: is pronounced "cons"
 - e1 is the head, e2 is the tail
- [e1;e2;...;en] is syntactic sugar for e1::e2::...:en::[]

Examples

3::[] (* The list [3] *)
2::(3::[]) (* The list [2; 3] *)
[1; 2; 3] (* The list 1::(2::(3::[])) *)

Both *cons* and *nil* are terms from LISP

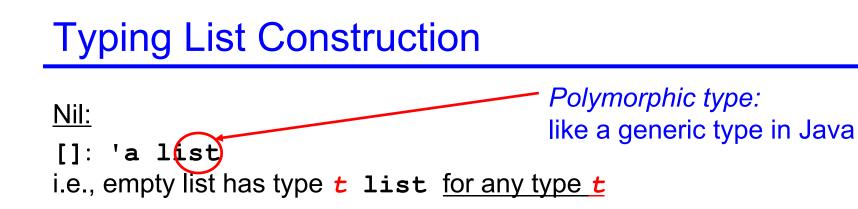
Constructing Lists

Evaluation

- [] is a value
- To evaluate [e1;...; en], evaluate e1 to a value v1,, evaluate en to a value vn, and return [v1;...; vn]

Examples

```
# let y = [1; 1+1; 1+1+1] ;;
val y : int list = [1; 2; 3]
# let x = 4::y ;;
val x : int list = [4; 1; 2; 3]
# let z = 5::y ;;
val z : int list = [5; 1; 2; 3]
# let m = "hello"::"bob"::[];;
val m : string list = ["hello"; "bob"]
```



<u>Cons:</u>

```
If e1: t and e2: t list then e1::e2: t list
```

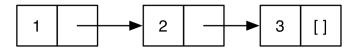
```
With parens for clarity:
If e1: t and e2: (t list) then (e1::e2): (t list)
```

Examples

```
# let x = [1;"world"] ;;
This expression has type string but an expression was
 expected of type int
# let m = [[1];[2;3]];;
val y : int list list = [[1]; [2; 3]]
# let y = 0::[1;2;3] ;;
val y : int list = [0; 1; 2; 3]
# let w = [1;2]::y ;;
This expression has type int list but is here used with
  type int list list
```

- The left argument of :: is an element, the right is a list
- Can you construct a list y such that [1;2]::y makes sense?

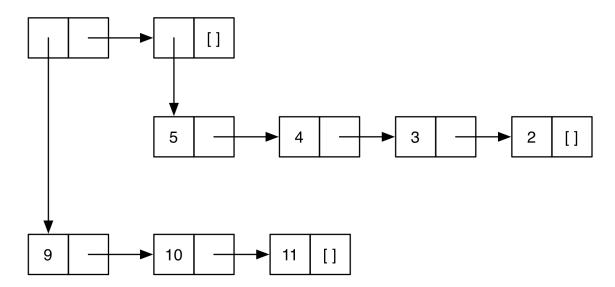
Lists in Ocaml are Linked



- [1;2;3] is represented above
 - A nonempty list is a pair (element, rest of list)
 - The element is the head of the list
 - The pointer is the tail or rest of the list
 - ...which is itself a list!
- Thus in math (i.e., inductively) a list is either
 - The empty list []
 - Or a pair consisting of an element and a list
 - · This recursive structure will come in handy shortly

Lists of Lists

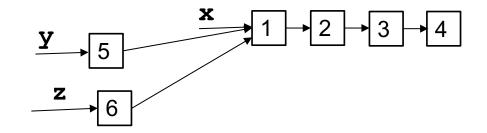
- Lists can be nested arbitrarily
 - Example: [[9; 10; 11]; [5; 4; 3; 2]]
 - (Type int list list)



Lists are Immutable

- No way to *mutate* (change) an element of a list
- Instead, build up new lists out of old, e.g., using ::

let x = [1;2;3;4]
let y = 5::x
let z = 6::x



Quiz 1

What is the type of the following expression?

```
[1.0; 2.0; 3.0; 4.0]
```

A. array

B. list

C. float list

D. int list

What is the type of the following expression?

```
[1.0; 2.0; 3.0; 4.0]
```

A. array

B. list

C. float list

D. int list

Quiz 2

What is the type of the following expression?

31::[3]

A. int
B. int list
C. int list list
D. error

Quiz 2

What is the type of the following expression?

31::[3]

A. int
B. int list
C. int list list
D. error

What is the type of the following definition?

```
let f x = "alien"::[x]
```

```
A. string -> string
B. string list
C. string list -> string list
D. string -> string list
```

What is the type of the following definition?

```
let f x = "alien"::[x]
```

```
A. string -> string
B. string list
C. string list -> string list
D. string -> string list
```

Pattern Matching

- To pull lists apart, use the **match** construct
- Syntax

match e with
| p1 -> e1
| ...
| pn -> en

- Evaluate e to a value v
- If p1 matches v, then evaluate e1 to v1 and return v1
- ...
- Else if *pn* matches *v*, then evaluate *en* to *vn* and return *vn*
- Else, no patterns match: raise Match_failure exception

Pattern Matching Example

- Example runs
 - is_empty [] (* evaluates to true *)
 - is_empty [1] (* evaluates to false *)
 - is_empty [1;2] (* evaluates to false *)

Pattern Matching Example (cont.)

let hd l =

match 1 with

- (h::t) -> h
- Example runs
 - hd [1;2;3] (* evaluates to 1 *)
 - hd [2;3] (* evaluates to 2 *)
 - hd [3] (* evaluates to 3 *)
 - hd [] (* Exception: Match_failure *)

To what does the following expression evaluate?

```
match [1;2;3] with
  [] -> [0]
  [ h::t -> t
```

A. [] B. [0] C. [1] D. [2;3] To what does the following expression evaluate?

```
match [1;2;3] with
  [] -> [0]
  [ h::t -> t
```

A. [] B. [0] C. [1] D. [2;3]

"Deep" pattern matching

- You can nest patterns for more precise matches
 - a::b matches lists with at least one element
 - Matches [1;2;3], binding a to 1 and b to [2;3]
 - a::[] matches lists with exactly one element
 - Matches [1], binding a to 1
 - Could also write pattern a::[] as [a]
 - a::b::[] matches lists with exactly two elements
 - Matches [1;2], binding a to 1 and b to 2
 - Could also write pattern a::b::[] as [a;b]
 - a::b::c::d matches lists with at least three elements
 - Matches [1;2;3], binding a to 1, b to 2, c to 3, and d to []
- CMSC 330 Spring 2020 Cannot write pattern as [a;b;c]::d (why?)

Pattern Matching – Wildcards

- An underscore _ is a wildcard pattern
 - Matches anything
 - But doesn't add any bindings
 - Useful to hold a place but discard the value
 - i.e., when the variable does not appear in the branch expression
- In previous examples
 - Many values of h or t ignored
 - Can replace with wildcard _

Pattern Matching – Wildcards (cont.)

- - let is_empty l = match l with
 - [] -> true | (_::_) -> false
 - -let hd l = match l with $(h::_) \rightarrow h$
 - let tl l = match l with $(::t) \rightarrow t$
- Outputs
 - is_empty[1](* evaluates to false *)
 - is_empty[](* evaluates to true *)
 - hd [1;2;3] (* evaluates to 1 *)
 - hd [1] (* evaluates to 1 *)
 - tl [1;2;3] (* evaluates to [2;3] *)
 - tl [1] (* evaluates to [] *)

To what does the following expression evaluate?

A. [] B. [0] C. [1] D. [2;3] To what does the following expression evaluate?

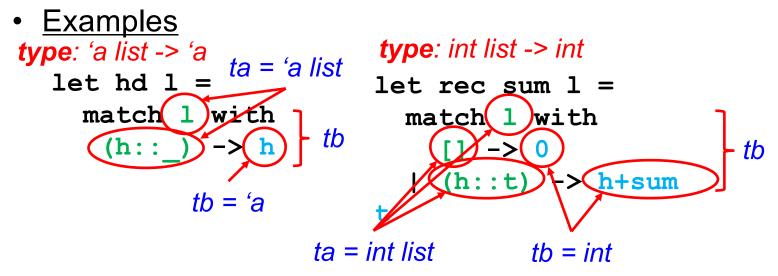
A. [] B. [0] C. [1] D. [2;3]

Pattern Matching – An Abbreviation

- let f p = e, where p is a pattern
 - is shorthand for let f x = match x with $p \rightarrow e$
- Examples
 - let hd (h::_) = h
 - let tl (_::t) = t
 - -let f $(x::y::_) = x + y$
 - -let g [x; y] = x + y
- Useful if there's only one acceptable input

Pattern Matching Typing

- If *e* and *p1*, ..., *pn* each have type *ta*
- and e1, ..., en each have type tb
- Then entire match expression has type tb



match e with

p1 -> e1

pn -> en

Polymorphic Types

- The sum function works only for int lists
- But the hd function works for any type of list
 - hd [1; 2; 3] (* returns 1 *)
 - hd ["a"; "b"; "c"] (* returns "a" *)
- OCaml gives such functions polymorphic types
 - hd : 'a list \rightarrow 'a
 - this says the function takes a list of *any* element type 'a, and returns something of that same type
- These are basically generic types in Java
 - 'a list is like List<T>

Examples Of Polymorphic Types

```
• let tl (_::t) = t
    # tl [1; 2; 3];;
    - : int list = [2; 3]
    # tl [1.0; 2.0];;
    - : float list = [2.0]
    (* tl : 'a list -> 'a list *)
```

```
• let fst x y = x
# fst 1 "hello";;
- : int = 1
# fst [1; 2] 1;;
- : int list = [1; 2]
(* fst : 'a -> 'b -> 'a *)
```

Examples Of Polymorphic Types

- let eq x y = x = y (* let eq x y = (x = y) *)
 # eq 1 2;;
 - : bool = false
 - # eq "hello" "there";;
 - : bool = false
 - **#** eq "hello" 1 -- type error
 - (* eq : 'a -> 'a -> bool *)

Quiz 6

What is the type of the following function?

Quiz 6

What is the type of the following function?

Pattern matching is **AWESOME**

- 1. You can't forget a case
 - Compiler issues inexhaustive pattern-match warning
- 2. You can't duplicate a case
 - Compiler issues unused match case warning
- 3. You can't get an exception
 - Can't do something like List.hd []
- 4. Pattern matching leads to elegant, concise, beautiful code

Lists and Recursion

- Lists have a recursive structure
 - And so most functions over lists will be recursive

```
let rec length l = match l with
   [] -> 0
   | (_::t) -> 1 + (length t)
```

- This is just like an inductive definition
 - The length of the empty list is zero
 - The length of a nonempty list is 1 plus the length of the tail
- Type of length?
 - `a list -> int

More Examples

```
• sum l (* sum of elts in l *)
let rec sum l = match l with
[] -> 0
| (x::xs) -> x + (sum xs)
```

```
• negate 1 (* negate elements in list *)
    let rec negate 1 = match 1 with
    [] -> []
    | (x::xs) -> (-x) :: (negate xs)
```

```
    last 1 (* last element of 1 *)
        let rec last 1 = match 1 with
            [x] -> x
            | (x::xs) -> last xs
```

More Examples (cont.)

- (* return a list containing all the elements in the list l
 followed by all the elements in list m *)
- append 1 m

```
let rec append 1 m = match 1 with
```

[] \rightarrow m | (x::xs) \rightarrow x::(append xs m)

```
• rev l (* reverse list; hint: use append *)
let rec rev l = match l with
[] -> []
| (x::xs) -> append (rev xs) [x]
```

• **rev** takes O(n²) time. Can you do better?

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