# CRYPTOGRAPHY INTRO 

## GRAD SEC OCT 172017 <br> 

## SCENARIOS AND GOALS



Public network


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Public network


CONFIDENTIALITY Keep others from reading Alice's messages / data

INTEGRITY
Keep others from undetectably tampering with Alice's messages / data

Keep others from undetectably impersonating Alice (keep her to her word, too)

## RANDOMNESS



## RANDOMNESS

Message m


## RANDOMNESS



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This will be impossible with Alice and Bob having a shared secret

## WHAT WE IDEALLY HAVE: RANDOM FUNCTIONS

Consider the set of all permutations $f_{i}: X \rightarrow X$

$$
\begin{aligned}
& f_{2} \begin{array}{ll|l|l|l}
\hline 1 & 0 & 2 & 3 & 4 \\
\end{array} \\
& f_{|X|:} \begin{array}{l|l|l|l|l|}
\hline 7 & 9 & 5 & 1 & 8 \\
\hline
\end{array}
\end{aligned}
$$

Think of $X$ as all
128-bit bit strings

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$$
\begin{aligned}
& \begin{array}{l|l|l|l|l|l|}
\hline f_{1} & 0 & 0 & 1 & 2 & 3
\end{array}{ }^{\prime} \ldots
\end{aligned}
$$

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If you know $i$, then $f_{i}(x)$ is trivial to invert

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```
fl
```




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```
flX|: 7 7 9:5
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## WHAT WE IDEALLY HAVE: RANDOM FUNCTIONS

Shared secret: index $i$ chosen u.a.r.


In essence, this protocol is saying "Let's use the ${ }^{i t h}$ permutation function"

Infeasible to store all permutation functions
So instead cryptographers construct pseudorandom functions

## BLACKBOX \#1: BLOCK CIPHERS

## BLOCK CIPHERS



Plaintext


AES key sizes:
128, 192, 256


> Block ciphers are deterministic For a given $m$ and $K$,
> $E(K, m)$ always returns the same $c$

Confusion: Each bit of the ciphertext should depend on each bit of the key Diffusion: Flipping a bit in $m$ should flip each bit in c with $\operatorname{Pr}=1 / 2$

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## INITIALIZATION VECTORS

## rjust needs to be different each time

Random: Must send with the message Good if messages can be reordered

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## BLOCK CIPHERS HAVE FIXED SIZE




Electronic Codebook (ECB) mode encryption


Electronic Codebook (ECB) mode decryption


## NEVER use ECB

(but over 50\% of Android apps do)


Cipher Block Chaining (CBC) mode encryption


Cipher Block Chaining (CBC) mode decryption



Counter (CTR) mode encryption


Counter (CTR) mode decryption

# BLACKBOX \#2: MESSAGE AUTHENTICATION CODE (MAC) 

## MESSAGE AUTHENTICATION CODES



AES key sizes:
Plaintext
Same fixed block size
(AES: 128 bits)
Ciphertext

128, 192, 256


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## MESSAGE AUTHENTICATION CODES

- Sign: takes a key and a message and outputs a "tag"
- $\operatorname{Sgn}(\mathrm{k}, \mathrm{m})=\mathrm{t}$
- Verify: takes a key, a message, and a tag, and outputs Y/N - Vfy $(k, m, t)=\{Y, N\}$
- Correctness:
- Vfy(k, m, Sgn(k, m)) = Y


## ATTACKER'S GOAL: EXISTENTIAL FORGERY

- A MAC is secure if an attacker cannot demonstrate an existential forgery despite being able to perform a chosen plaintext attack:
- Chose plaintext:
- Attacker gets to choose m1, m2, m3, ...
- And in return gets a properly computed $\mathrm{t} 1, \mathrm{t} 2, \mathrm{t} 3, \ldots$
- Existential forgery:
- Construct a new $(m, t)$ pair such that $V f y(k, m, t)=Y$


## ENCRYPTED CBC

Just take the last block in CBC It's a trap!


Cipher Block Chaining (CBC) mode encryption

Use a separate key and encrypt the last block

## BLACKBOX \#3: HASH FUNCTIONS

## HASH FUNCTION PROPERTIES

- Very fast to compute
- Takes arbitrarily-sized inputs, returns fixed-sized output
- Pre-image resistant:

Given $\mathrm{H}(\mathrm{m})$, hard to determine m

- Collision resistant

Given $m$ and $H(m)$, hard to find $m^{\prime} \neq m$ s.t. $H(m)=H\left(m^{\prime}\right)$

Good hash functions: SHA family (SHA-256, SHA-512, ...)

## HASH MACS

- Sign(k, m):
- opad $=0 \times 5 c 5 c 5 c \ldots$
- ipad =0x363636...
- H( (k $\oplus$ opad) II H((k $\oplus$ ipad) II m ) )
- Verify:
- Recompute and compare

