

## Quiz 3 from Fall 2020 (Practice)

STUDENT NAME

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### Q1 First Sets

3 Points

Consider the following CFG:

$$S \rightarrow TTVT$$

$$T \rightarrow \mathbf{x} \mid \varepsilon$$

$$V \rightarrow \mathbf{y} \mid \mathbf{z}$$

#### Q1.1

1 Point

Which non-terminals are in the first set of  $S$ ?

$\mathbf{x}$

$\mathbf{y}$

$\mathbf{z}$

$\varepsilon$

Save Answer

#### Q1.2

1 Point

Which non-terminals are in the first set of  $T$ ?

$\mathbf{x}$

$\mathbf{y}$

$\mathbf{z}$

$\varepsilon$

Save Answer

### Q1.3

1 Point

Which non-terminals are in the first set of  $V$ ?

**x**

**y**

**z**

$\epsilon$

Save Answer

### Q2 Parsing

6 Points

Consider the following CFG:

$$S \rightarrow \mathbf{xySz} \mid \mathbf{xTyz}$$
$$T \rightarrow \mathbf{wT} \mid \epsilon$$

Complete the `parse_S` and `parse_T` functions below, which should parse  $T$  and  $S$ , respectively. Your functions should not return anything, but should fail if the input is invalid (if the input is valid, simply return `()`).

The structure of the program is as follows:

```
let rec parse_S toks =
  (* TODO *)

and rec parse_T toks =
  (* TODO *)
```

The `lookahead` and `match_tok` functions are provided below:

```
let lookahead toks =
  match toks with
  | h :: t -> h
  | [] -> raise (ParseError "no tokens")

let match_tok toks tok =
  match toks with
  | h :: t when h == tok -> t
  | _ -> raise (ParseError "bad match")
```

### Q2.1

3 Points

Implement `parse_S` below of type `string list -> unit`. The first line of your answer should be `let rec parse_S toks =`.

Enter your answer here

Save Answer

## Q2.2

3 Points

Implement `parse_T` below of type `string list -> unit`. The first line of your answer should be `and rec parse_T toks =`.

Enter your answer here

Save Answer

## Q3 CFG Construction

3 Points

Construct a CFG that generates strings of the form  $a^x b^y$  where  $y \geq 2x$ .

Enter your answer here

Save Answer

## Q4 Ambiguous Grammars

2 Points

Consider the following CFG:

$$S \rightarrow aS \mid aT$$

$$T \rightarrow a \mid b \mid \epsilon$$

Prove that this grammar is ambiguous.

Enter your answer here

Save Answer

# Q5 Operational Semantics

6 Points

$$\frac{}{A; n \rightarrow n} \quad \frac{A(x) = v}{A; x \rightarrow v} \quad \frac{A; e_1 \rightarrow v_1 \quad A, x : v_1; e_2 \rightarrow v_2}{A; \text{let } x = e_1 \text{ in } e_2 \rightarrow v_2}$$

$$\frac{A; e_1 \rightarrow n_1 \quad A; e_2 \rightarrow n_2 \quad n_1 > n_2}{A; e_1 > e_2 \rightarrow \text{true}} \quad \frac{A; e_1 \rightarrow n_1 \quad A; e_2 \rightarrow n_2 \quad n_1 \leq n_2}{A; e_1 > e_2 \rightarrow \text{false}}$$

$$\frac{A; e_1 \rightarrow \text{true} \quad A; e_2 \rightarrow v}{A; \text{if } e_1 \text{ then } e_2 \text{ else } e_3 \rightarrow v} \quad \frac{A; e_1 \rightarrow \text{false} \quad A; e_3 \rightarrow v}{A; \text{if } e_1 \text{ then } e_2 \text{ else } e_3 \rightarrow v}$$

Using the above rules, fill in the blanks in the derivation show below:

$$\frac{\frac{A; \boxed{2}}{A, x: 7; \text{true} \rightarrow \text{true}} \quad \frac{\frac{\boxed{5}}{A, x: 7; x \rightarrow 7} \quad \frac{A, x: 7; 13 \rightarrow 13}{A, x: 7; \boxed{3} \rightarrow \text{false}}}{A, x: 7; \text{if true then } x > 13 \text{ else true} \rightarrow \text{false}} \quad \boxed{4}}{A; \text{let } \boxed{1} \text{ in if true then } x > 13 \text{ else true} \rightarrow \text{false}}$$

**IMPORTANT: Double-check that the BLUE box numberings correspond with your answers; the boxes are numbered from bottom to top. We will not accept out-of-order answers.**

Blank 1:

Blank 2:

Blank 3:

Blank 4:

Blank 5:

Save Answer

Save All Answers

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