Instructions
- The exam has 15 pages (front and back); make sure you have them all.
- Do not start this test until you are told to do so!
- You have 120 minutes to take this exam.
- This is a closed book exam. No notes or other aids are allowed.
- Answer essay questions concisely in 2-3 sentences. Longer answers are not needed.
- For partial credit, show all of your work and clearly indicate your answers.
- Write neatly. Credit cannot be given for illegible answers.

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1. PL Concepts [8 pts]
Circle your answers. Each T/F question is 1 point.

1) T / F  OCaml and Ruby use garbage collection.

2) T / F  Let statements declare immutable variables by default in OCaml and Rust.

3) T / F  When using a language with a call-by-value evaluation strategy, arguments are reduced to a value before being passed onto a function.

4) T / F  Tail recursive functions can be optimized by a compiler to not cause stack overflows.

5) T / F  If the program terminates, CALL BY VALUE and CALL BY NAME will always generate the same value.

6) T / F  OCaml is not statically-typed because you don’t have to explicitly declare types.

7) T / F  Reference counting and mark and sweep are both techniques used by garbage collection algorithms.

8) T / F  All NFAs are DFAs, but not all DFAs are NFAs.
2. Lambda Calculus [10 pts]

A. Make the parentheses explicit.

1) [2 pts] \((\lambda x. \ x \ z) \ \lambda y. \ w \ \lambda w. \ w \ y \ z \ x\)

\((\lambda x. \ (x \ z)) \ (\lambda y. \ (w \ (\lambda w. \ (((w \ y) \ z) \ x))))\)

2) [2 pts] \(\lambda x. \ x \ y \ \lambda x. \ y \ x\)

\((\lambda x. \ ((x \ y) \ (\lambda x. \ (y \ x))))\)

B. Reduce the following lambda expressions using Call By Name and Call By Value strategies. Make appropriate use of parentheses and alpha reductions to get maximal partial credit.

\((\lambda x. \ x \ y) \ ((\lambda y. \ a) \ (\lambda x. \ y))\)

[3 pts] Call By Name

\((\lambda x. \ x \ y) \ ((\lambda y. \ a) \ (\lambda x. \ y))\)

= \((\lambda y. \ a) \ (\lambda x. \ y)) \ y\)

= \(a \ y\)

[3 pts] Call By Value

\((\lambda x. \ x \ y) \ ((\lambda y. \ a) \ (\lambda x. \ y))\)

= \((\lambda x. \ x \ y) \ a\)

= \(a \ y\)
3. OCaml [20 pts]

A. Write the types of the following OCaml expressions. If the expression doesn’t type check, just write “type error” with no explanation required.

1) [3 pts] fun x -> fun y -> [x = (y + 1)]

```
int -> int -> bool list
```

2) [3 pts] fun x y z -> match (x = y z) with true -> y z | false -> y x

```
'a -> ('a -> 'a) -> 'a -> 'a
```

B. [4 pts] What would you put in place for the blank such that the following code returns 44.

```
let f = fun x y z ->
    List.fold_left(fun acc ele -> acc + (ele + (y z))) 0 x
in f [1; 1; 1; 1] _________________ 4
```

```
(fun x -> x + 6)
```

For the questions C and D, you may not use the List module or @, but you may use the helper functions given below. You may also write your own helper functions.

Helper Functions:

```
let rec map f xs = match xs with
| [] -> []
| x::xt -> (f x)::(map f xt)

let rec foldl f a xs = match xs with
| [] -> a
| x::xt -> foldl f (f a x) xt

let rec foldr f xs a = match xs with
| [] -> a
| x::xt -> f x (foldr f xt a)
```
C. [5 pts] Write a function `make_palindrome` of type `'a list -> 'a list` which makes the input list into a palindrome.

**Examples:**
make_palindrome [] = []
make_palindrome [1; 2; 3] = [1; 2; 3; 3; 2; 1]
make_palindrome ["c"; "m"; "s"; "c"; "s"; "m"; "c"]

```ocaml
let rec make_palindrome lst =
  let rev = foldl (fun a x -> x::a) [] lst in
  foldr (fun x a -> x::a) lst rev
```

D. [5 pts] Write a function `lod` of type `'int list -> int list -> int list` that creates a new list that is the result of subtracting each item of the second list from each item at the same index in the first list. Assume two lists have the same size.

**Examples:**
lod [] [] = []
lod [1; 2; 3] [3; 2; 1] = [-2; 0; 2] (*[(1-3);(2-2);(3-1)] *)

```ocaml
let rec lod lst1 lst2 =
  match lst1, lst2 with
  | [],[] -> []
  | h1::t1,h2::t2 -> (h1-h2)::(lod t1 t2)
```
4. Ruby [15 pts]

In 2019, the University of Maryland awarded a $100 million contract to Workday to upgrade Testudo to a new cloud-based system. You were hired by Workday to develop a part of the course registration system because of your experience in registering for classes and your Ruby skills.

The goal of the course registration system is to allow students to add/drop classes and see all the courses they've registered for. You will be given a file called courses.txt which contains information about every course offered by the university. Each line in courses.txt will have the format:

Course, Seats

The course name will consist of 4 uppercase letters followed by 3 digits and the total number of seats will be a number with one or more digits. All invalid lines should be ignored. For example, the following line is valid: CMSC330, 30

Each student will be represented as a string. We will simply denote this as id.

You will have to implement four functions, described below:

- [3 pts] initialize(path) - Reads the file and parses the contents. Store the contents in any data structure you like, as long as these other functions work as described below.
- [4 pts] add(id, course) - Registers a student to the given course and returns true if there is an open seat and the student has not already registered for the course. Otherwise, return false. Note that the total number of seats given in courses.txt is not the same as the total number of open seats. You will have to keep track of open seats.
- [4 pts] drop(id, course) - Drops a student from the given course if the student has registered for it and returns true. In all other cases, return false.
- [4 pts] get_courses(id) - Returns an array containing all the courses a student has registered for. If there's no such student/no registration, return an empty array.

The class definition is given on the following page for you to fill in. Feel free to add any class or instance variables you feel are necessary. Here is an example interaction with the class:

```ruby
r = CourseRegistration.new('courses.txt')
r.add('1001', 'CMSC351')
=> true
r.add('1001', 'CMSC330')
=> true
r.add('1002', 'CMSC330')
=> true
r.add('1010', 'CMSC330')
=> false # No more open seats! :(
```
r.drop('1002', 'CMSC330')
=> true
r.get_courses('1001')
=> ['CMSC330', 'CMSC351']

class CourseRegistration
  def initialize(path)
    @courses = {};

    File.open(path).each do |line|
      if line =~ /^([A-Z]{4}\d{3}),\d+$/
        @courses[$1] = [$2.to_i, []]
      end
    end
  end

  def add(id, course)
    if @courses[course] && @courses[course][1].count < @courses[course][0] && !@courses[course][1].include?(id)
      @courses[course][2] << id
      true
    else
      false
    end
  end

  def drop(id, course)
    if @courses[course]
      @courses[course][2].delete(id)
      true
    else
      false
    end
  end

  def get_courses(id)
    list = []
    @courses.each do |k,v|
      if v[1].include?(id)
        list << k
      end
    end
    list
  end
5. Rust [10 pts]

A. [3 pts] Does the following program compile? If so, write out the output of the program execution. Otherwise, point out the line that causes the error and explain why the program doesn't compile.

```rust
1 fn main () {
2   let mut a = 3;
3   let b = &mut a;
4   let &mut c = b;
5   *b = 5;
6   println! ("{}", a + c);
7 }
```

Compiles and prints 8

B. [3 pts] Who is the owner of the string “330 rocks!” when the execution stops at HERE?

```rust
1 fn main () {
2   let a = String::from("330 rocks!");
3   let b = a;
4   let c = &b;
5   let d = &c;
6   let e = d;
7   let f = &*c;
8   let g = e;
9   // HERE
10 }
```

b
C. [4 pts] The function `add_elems` sums up the elements of an integer array. Find and fix the errors in the function. Find three - there may be more, any three are fine.

```rust
fn add_elems(arr : &[i32]) -> i32 {
    let sum = 0;
    for i in arr.iter() {
        sum += arr[i];
    }
    sum;
}
```

1. `sum` must be mutable
2. Should be adding `i` instead of `arr[i]`
3. Line 6 should not have a semicolon
6. Regex, FAs, CFGS [14 pts]

A. [6 pts] Use the subset algorithm to convert the above NFA to a DFA.
Show all steps and draw the final DFA.

Final DFA after subset construction should have the following formal definition:

\[\begin{aligned}
\Sigma & : \{a, b, c\} \\
Q & : \\{\{0, 2, 4\}, \{1\}, \{5, 2, 4\}, \{3, 5, 2, 4\}\} \\
\mathit{q_0} & : \{0, 2, 4\} \\
F & : \{\{1\}, \{5, 2, 4\}, \{3, 5, 2, 4\}\} \\
\delta & : \{(\{0, 2, 4\}, a, \{1\}), (\{0, 2, 4\}, b, \{5, 2, 4\}), \\
&(\{0, 2, 4\}, c, \{3, 5, 2, 4\}), (\{1\}, a, \{1\}), (\{5, 2, 4\}, b, \{5, 2, 4\}), \\
&(\{5, 2, 4\}, c, \{3, 5, 2, 4\}), (\{3, 5, 2, 4\}, b, \{5, 2, 4\}), \\
&(\{3, 5, 2, 4\}, c, \{3, 5, 2, 4\})\}
\end{aligned}\]
B. [4 pts] Write a regex to describe the language of the above NFA:

\[(a+)\|(b|c)+\]\n
C. [4 pts] Write a context free grammar that generates the following language:

\[a^x b^y c^z\] where \[z = x + y\], \[x \geq 0\] and \[y \geq 0\]

\[
S \rightarrow aSC \mid T \\
T \rightarrow bTc \mid \varepsilon
\]
7. Parsing [10 pts]
A. [3 pts] List the first sets for the following grammar:
You may use e or ε for epsilon. Do not use E as that could imply a non-terminal.
\[
S \rightarrow aB \mid R w
\]
\[
B \rightarrow dR \mid n
\]
\[
R \rightarrow c \mid \varepsilon
\]

First(S) = \{a, c, w\}
First(B) = \{d, n\}
First(R) = \{c, \varepsilon\}

B. [3 pts] Fix the following grammar so that it can be parsed by a recursive descent parser
\[
S \rightarrow S A B \mid A B
\]
\[
A \rightarrow A a \mid a
\]
\[
B \rightarrow B b \mid b
\]

\[
S \rightarrow A B S \mid A B
\]
\[
A \rightarrow A a \mid a
\]
\[
B \rightarrow B b \mid b
\]

C. [4 pts] The following is the CFG for an even length palindrome over the alphabet \{a,b\}
\[
S \rightarrow a S a \mid b S b \mid \varepsilon
\]
Can you write a recursive descent parser for this grammar? If so, please write the parse_S function using either of the two implementations of lookahead or match_tok covered in the class. Assume the token list type of char list. For example: ['a'; 'b'; 'b'; 'a'].
If a recursive descent parser cannot parse this grammar, explain why.

CFG cannot be parsed by recursive descent because there is no unique first set for ε case, making the first and second halves of palindrome indistinguishable under recursive descent.
8. Operational Semantics [6 pts]

\[
\begin{align*}
A;\ false \Rightarrow false \quad (1) & \quad A;\ true \Rightarrow true \quad (2) \\
A;\ e_1 \Rightarrow n_1 & \quad A;\ e_2 \Rightarrow n_2 \quad \frac{v \text{ is } n_1 > n_2}{A;\ e_1 > e_2 \Rightarrow v} \quad (5) \\
A;\ e_1 \Rightarrow n_1 & \quad A;\ e_2 \Rightarrow n_2 \quad \frac{v \text{ is } n_1 + n_2}{A;\ e_1 + e_2 \Rightarrow v} \quad (7) \\
A;\ e_1 \Rightarrow v & \quad A;\ x : v_1;\ e_2 \Rightarrow v_2 \quad (9) \\
A;\ n \Rightarrow n & \quad (3) \\
A;\ x \Rightarrow v & \quad (4) \\
A;\ e_1 \Rightarrow true & \quad A;\ e_2 \Rightarrow v \quad (6) \\
A;\ if\ e_1 \text{ then } e_2 \text{ else } e_3 \Rightarrow v & \quad (8)
\end{align*}
\]

Consider the following incomplete (but partially filled!) proof tree using the above semantics:

\[
\begin{align*}
A;\ 4 \Rightarrow 4 \quad (3) & \quad 12 \text{ is } 4 + 8 \quad (b) \\
A;\ 15 \Rightarrow 15 \quad (3) & \quad \text{is } ? \quad (a) \\
A;\ if\ 4 + 8 > 15 \text{ then } 16 > 23 \text{ else } 42 \Rightarrow ?? \quad (8)
\end{align*}
\]

A. [4 pts] What rule numbers correspond to the holes in the tree?
ONLY WRITE THE RULE NUMBERS. DO NOT WRITE MORE THAN ONE DIGIT PER ITEM.

a) 5  
b) 7  
c) 3  
d) 3

B. [2 pts] What is the final answer? (In other words: what value should go in the box ??? in the bottom of the proof tree?)

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9. Security [7 pts]
A. [3 pts] There is a security vulnerability in the following code. Explain how the attacker can exploit the vulnerability assuming that stack is allocated high to low address.

```c
#include <stdlib.h>
#include <stdio.h>
#include <string.h>

void print_strings(char *buffer, int len) {
    for (int i=0; i<len; i++) {
        if (buffer[i] != 0) {
            printf("%c", buffer[i]);
        }
    }
    printf("\n");
}

int main(int argc, char **argv) {
    char secret[32];
    char public[32];
    strcpy(secret, "This is a secret");
    strcpy(public, "This is public data");
    int len = atoi(argv[1]);

    char buffer[len+1];
    memcpy(buffer, public, len);
    buffer[len] = 0;
    print_strings(buffer, len);
}
```

Buffer overflow. Large value for argv[1] can read memory outside of what's allowed i.e secret array.
B. [2 pts] SQL injections are best prevented by (select all that apply):
   a) Input Sanitization
   ✓ b) Prepared Statements
   ✓ c) Forced Type Checking
   d) Dynamic Memory Allocation
   e) Randomized Memory Access

C. [2 pts] A stored XSS attack typically can be prevented if the web servers
   ✓ a) never output data received as input directly without checking it for malicious code
   b) use the same origin policy
   c) disable javascript
   d) use prepared statements