CMSC 330 Quiz 4 Spring 2022

Q1. Loco Lists

Q1.1. Write a CFG to represent a list consisting of positive integers and other lists. These lists (and sublists) can have arbitrarily large dimensions.

Notes:

- An empty list is also a valid list.
- You can use n to denote a positive integer in the CFG. You don't have to worry about representing multidigit numbers since n encapsulates them all.
- To represent ϵ in the CFG, you can either write the word epsilon or just type the letter e.

Examples of Valid Lists:

```
[]
[[[]]]
[1,[[1,2],[4],56],[[[564]]]]
[1,2,3]
```

Q1.2. Is the language defined by the grammar given above regular?

Yes/No

Q2. Context-Free Grammars

My friend Hamza with a peculiar lexicon likes modifying common acronyms in his speech and texting as defined by the following CFG:

```
S -> A | B
A -> loL
L -> l | l out loud | A
B -> smH
H -> h | h my head | B
```

Can the grammar above be parsed by a LL1 recursive descent parser (like Project 4)? Justify your answer.

Q3. Ambiguity

Prove that the following grammar is ambiguous:

```
S -> bS | Sb | T
T -> Sa | Sb | Sc | ε
```

Q4. Operational Semantics

Using the gives rules, fill in the blanks the complete the derivation below:

${A; \ { m n} \Rightarrow { m n}} \qquad {A({ m x}) = { m v}\over A; \ { m x} \Rightarrow { m v}}$			
$rac{A; \ \mathrm{e}_1 \Rightarrow \mathrm{v}_1 \qquad A, \mathrm{x}: \mathrm{v}_1; \ \mathrm{e}_2 \Rightarrow \mathrm{v}_2}{A; \ \mathrm{let} \ \mathrm{x} = \mathrm{e}_1 \ \mathrm{in} \ \mathrm{e}_2 \Rightarrow \mathrm{v}_2}$			
$rac{A; \ \mathrm{e}_1 \Rightarrow \mathrm{v}_1 \qquad A; \ \mathrm{e}_2 \Rightarrow \mathrm{v}_2 \qquad \mathrm{v}_3 \ \mathrm{is} \ \mathrm{v}_1 \wedge \mathrm{v}_2}{A; \ \mathrm{e}_1 \wedge \mathrm{e}_2 \Rightarrow \mathrm{v}_3}$			
(#2)	$\frac{(\#4)}{A, \mathbf{x}: \text{"cmsc"}, \mathbf{y}: \text{"330"}; \ \mathbf{x} \Rightarrow \text{"cmsc"}}$	$\frac{(\#5)}{A, x: \text{"cmsc"}, y: \text{"330"}; y \Rightarrow \text{"330"}}$	(#6)
$\overline{A; \text{"cmsc"} \Rightarrow \text{"cmsc"}} \qquad \overline{(\#2)}$	$A, \mathbf{x} : \text{"cmsc"}, \mathbf{y} : \text{"330"}; (\#3) \Rightarrow \text{"cmsc330"}$ $A, \mathbf{x} : \text{"cmsc"}; \text{ let } \mathbf{y} = \text{"330" in } \mathbf{x} \land \mathbf{y} \Rightarrow \text{"cmsc330"}$		
	A; (#1) in let $y = "330"$ in $x \land y \Rightarrow "c$	cmsc330"	

Blank #1:

Blank #2:

Blank #3:

Blank #4:

Blank #5:

Blank #6: