# Graphical models and their Role in Databases VLDB 2007 Tutorial 

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## Why a tutorial on graphical models at VLDB?

- VLDB
- Many DB tasks use probabilistic modeling
* Core: Selectivity estimation, Imprecise databases,
* Appication: Information extraction, Duplicate elimination, sensor networks.
* Data mining: Classification (naive Bayes, logistic), clustering (EM)
- Probabilistic modeling is simultaneously
$\star$ intuitive (low barrier to entry)
* subtle (important to understand well for correctness \& efficiency)
- Graphical models
- Fundamental tools for intuitively and efficiently modeling probabilities
- Distilled body of knowledge from many fields (let us build upon them, instead of reinveting)
VLDB wants to broaden, GM a fun and useful candidate for broadening


## Probabilistic modeling

- Given: several variables: $x_{1}, \ldots x_{n}, n$ is large.
- Task: build a joint distribution function $\operatorname{Pr}\left(x_{1}, \ldots x_{n}\right)$
- Goal: Answer several kind of projection queries on the distribution
- Basic premise
- Explicit joint distribution is dauntingly large
- Queries are simple aggregates over the joint distribution.


## Example: Selectivity estimation in databases

- Variables are columns of a table

| Age | Income | Experience | Degree | Location |
| :---: | :---: | :---: | :---: | :---: |
| 10 ranges | 7 scales | 7 scales | 3 scales | 30 places |
|  |  |  |  |  |

- An explicit joint distribution over all columns not tractable: number of combinations: $10 \times 7 \times 7 \times 3 \times 30=44100$.
- Queries: Estimate number of people with
- Income $>200 \mathrm{~K}$ and Degree="Bachelors",

Income $<200 \mathrm{~K}$, Degree="PhD" and experience $>10$ years.
Many, many more.

## Alternatives to an explicit joint distribution

- Assume all columns are independent of each other: bad assumption
- Use data to detect pairs of highly correlated column pairs and estimate their pairwise frequencies
- Many highly correlated pairs
income $\nmid \perp$ age, income $\not \Perp \perp$ experience, age $\nmid l$ experience
- Ad hoc methods of combining these into a single estimate
- Go beyond pairwise correlations: understand finer dependencies
- income $\not \Perp$ age, but income $\Perp$ age | experience
- experience $\Perp$ degree, but experience $\not \Perp$ degree $\mid$ income


## Graphical models make explicit an efficient joint

 distribution from these independencies
## Graphical models

Model joint distribution over several variables as a product of smaller factors that is
(1) Intuitive to represent and visualize

- Graph: represent structure of dependencies
- Potentials over subsets: quantify the dependencies
(2) Efficient to query
- given values of any variable subset, reason about probability distribution of others.
- many efficient exact and approximate inference algorithms


## Graphical models $=$ graph theory + probability theory.

## Graphical models in use

- Roots in statistical physics for modeling interacting atoms in gas and solids [ 1900]
- Early usage in genetics for modeling properties of species [ 1920]
- AI: expert systems (1970s-80s)
- Now many new applications:
- Error Correcting Codes: Turbo codes, impressive success story (1990s)
- Robotics and Vision: image denoising, robot navigation.
- Text mining: information extraction, duplicate elimination, hypertext classification, help systems
- Bio-informatics: Secondary structure prediction, Gene discovery
- Data mining: probabilistic classification and clustering.


## Overall plan

- Fundamentals
- Representation
- Exact inference
- Applications
- Selectivity estimation
- Probabilistic databases
- Applications: Sensor data management
- Fundamentals
(1) Learning a graphical model
(2) Conditional Random Fields
- Applications
- Information extraction
- Duplicate elimination


## Part I: Fundamentals of Graphical Models

## Part I: Outline

(1) Representation

- Directed graphical models: Bayesian networks
- Undirected graphical models
(2) Inference Queries
- Exact inference on chains
- Exact inference on general graphs
(3) Constructing a graphical model
- Graph Structure
- Parameters in Potentials
(4) Approximate inference
- Generalized belief propagation
- Sampling: Gibbs, Particle filters


## Representation

Structure of a graphical model: Graph + Potential

## Graph

- Nodes: variables $\mathbf{x}=x_{1}, \ldots x_{n}$

Continuous: Sensor temperatures, income Discrete: Degree (one of Bachelors, Masters, PhD), Levels of age

- Edges: direct interaction

Directed edges: Bayesian networks
Undirected edges: Markov Random fields


## Representation

## Potentials: $\psi_{c}\left(\mathbf{x}_{c}\right)$

- Scores for assignment of values to subsets $c$ of directly interacting variables.
- Which subsets? What do the potentials mean?

Different for directed and undirected graphs

## Probability

Factorizes as product of potentials

$$
\operatorname{Pr}\left(\mathbf{x}=x_{1}, \ldots x_{n}\right) \propto \prod \psi_{S}\left(\mathbf{x}_{S}\right)
$$

## Directed graphical models: Bayesian networks

- Graph G: directed acyclic
- Parents of a node: $\mathrm{Pa}\left(x_{i}\right)=$ set of nodes in $G$ pointing to $x_{i}$
- Potentials: defined at each node in terms of its parents.

$$
\psi_{i}\left(x_{i}, \operatorname{Pa}\left(x_{i}\right)\right)=\operatorname{Pr}\left(x_{i} \mid \operatorname{Pa}\left(x_{i}\right)\right.
$$

- Probability distribution

$$
\operatorname{Pr}\left(x_{1} \ldots x_{n}\right)=\prod_{i=1}^{n} \operatorname{Pr}\left(x_{i} \mid p a\left(x_{i}\right)\right)
$$

## Example of a directed graph



$$
\psi_{1}(L)=\operatorname{Pr}(L)
$$

| NY | CA | London | Other |
| :---: | :---: | :---: | :---: |
| 0.2 | 0.3 | 0.1 | 0.4 |

$$
\psi_{2}(A)=\operatorname{Pr}(A)
$$

| $\mathbf{2 0 - 3 0}$ | $\mathbf{3 0 - 4 5}$ | $>\mathbf{4 5}$ |
| :---: | :---: | :---: |
| 0.3 | 0.4 | 0.3 |

or, a Guassian distribution $(\mu, \sigma)=(35,10)$


$$
\psi_{2}(I, E, D)=\operatorname{Pr}(I \mid D, A)
$$

3 dimensional table, or a histogram approximation.

$$
\begin{aligned}
& \text { Probability distribution } \\
& \operatorname{Pa}(\mathbf{x}=L, D, I, A, E)=\operatorname{Pr}(L) \operatorname{Pr}(D) \operatorname{Pr}(A) \operatorname{Pr}(E \mid A) \operatorname{Pr}(I \mid D, E)
\end{aligned}
$$

## Popular Bayesian networks

- Hidden Markov Models: speech recognition, information extraction

- State variables: discrete phoneme, entity tag
- Observation variables: continuous (speech waveform), discrete (Word)
- Kalman Filters: State variables: continuous
- Discussed later
- PRMs: Probabilistic relational networks:
- An important relevant class for relational data
- Discussed later
- QMR (Quick Medical Reference) system


## Undirected graphical models

- Graph G: arbitrary undirected graph
- Useful when variables interact symmetrically, no natural parent-child relationship

- Example: labeling pixels of an image.
- Potentials defined on arbitrary subcliques $C$ of $G$. Popular choices:
- Node potentials
- Edge potentials

Probability distribution

$$
\operatorname{Pr}\left(\mathbf{x}=y_{1} \ldots y_{n}\right)=\frac{1}{Z} \prod_{C \in G} \psi_{C}\left(\mathbf{y}_{C}\right)
$$

where $Z=\sum_{\mathbf{y}^{\prime}} \prod_{C \in G} \psi_{C}\left(\mathbf{y}_{C}^{\prime}\right)$

## Example



- Node potentials
- $\psi_{1}(0)=4, \psi_{1}(1)=1$
- $\psi_{2}(0)=2, \psi_{2}(1)=3$
- $\psi_{9}(0)=1, \psi_{9}(1)=1$
- Edge potentials: Same for all edges
- $\psi(0,0)=5, \psi(1,1)=5, \psi(1,0)=1, \psi(0,1)=1$
- Probability: $\operatorname{Pr}\left(y_{1} \ldots y_{9}\right) \propto \prod_{k=1}^{9} \psi_{k}\left(y_{k}\right) \prod_{(i, j) \in E(G)} \psi\left(y_{i}, y_{j}\right)$


## Popular undirected graphical models

- Interacting atoms in gas and solids [ 1900]
- Markov Random Fields in vision for image segmentation
- Conditional Random Fields for information extraction


## Comparing directed and undirected graphs

- Some distributions can only be expressed in one and not the other.

- Potentials
- Directed: conditional probabilities, more intuitive
- Undirected: arbitrary scores, easy to set.
- Dependence structure
- Directed: Complicated d-separation test
- Undirected: Graph separation: $A \Perp B \mid C$ iff $C$ separates $A$ and $B$ in $G$.
- Often application makes the choice clear.
- Directed: Causality
- Undirected: Symmetric interactions.


## Part I: Outline

(1) Representation

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- Undirected graphical models
(2) Inference Queries
- Exact inference on chains
- Exact inference on general graphs
(3) Constructing a graphical model
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(4) Approximate inference
- Generalized belief propagation
- Sampling: Gibbs, Particle filters


## Inference queries

(1) Marginal probability queries over a small subset of variables:

- Find $\operatorname{Pr}$ (Income='High \& Degree='PhD')
- Find $\operatorname{Pr}\left(\right.$ pixel $\left.y_{9}=1\right)$

$$
\operatorname{Pr}\left(x_{1}\right)=\sum_{x_{2} \ldots x_{n}} \operatorname{Pr}\left(x_{1} \ldots x_{n}\right)
$$

(2) Most likely labels of remaining variables: (MAP queries)

- Find most likely entity labels of all words in a sentence
- Find likely temperature at sensors in a room

$$
\mathbf{x}^{*}=\operatorname{argmax}_{x_{1} \ldots x_{n}} \operatorname{Pr}\left(x_{1} \ldots x_{n}\right)
$$

## Exact inference on chains

- Given,
- Graph $\mathrm{y}_{1} \rightarrow \mathrm{y}_{2} \rightarrow \mathrm{y}_{3} \rightarrow \mathrm{y}_{4} \longrightarrow \mathrm{y}_{5}$
- Potentials: $\psi_{i}\left(y_{i}, y_{i+1}\right)$
- $\operatorname{Pr}\left(y_{1}, \ldots y_{n}\right)=\prod_{i} \psi_{i}\left(y_{i}, y_{i+1}\right)$
- Find, $\operatorname{Pr}\left(y_{i}\right)$ for any $i$, say $\operatorname{Pr}\left(y_{5}=1\right)$
- Exact method: $\operatorname{Pr}\left(y_{5}=1\right)=\sum_{y_{1}, \ldots y_{4}} \operatorname{Pr}\left(y_{1}, \ldots y_{4}, 1\right)$ requires exponential number of summations.
- A more efficient alternative...


## Exact inference on chains

$$
\begin{aligned}
\operatorname{Pr}\left(y_{5}=1\right) & =\sum_{y_{1}, \ldots y_{4}} \operatorname{Pr}\left(y_{1}, \ldots y_{4}, 1\right) \\
& =\sum_{y_{1}} \sum_{y_{2}} \sum_{y_{3}} \sum_{y_{4}} \psi_{1}\left(y_{1}, y_{2}\right) \psi_{2}\left(y_{2}, y_{3}\right) \psi_{3}\left(y_{3}, y_{4}\right) \psi_{4}\left(y_{4}, 1\right) \\
& =\sum_{y_{1}} \sum_{y_{2}} \psi_{1}\left(y_{1}, y_{2}\right) \sum_{y_{3}} \psi_{2}\left(y_{2}, y_{3}\right) \sum_{y_{4}} \psi_{3}\left(y_{3}, y_{4}\right) \psi_{4}\left(y_{4}, 1\right) \\
& =\sum_{y_{1}} \sum_{y_{2}} \psi_{1}\left(y_{1}, y_{2}\right) \sum_{y_{3}} \psi_{2}\left(y_{2}, y_{3}\right) B_{3}\left(y_{3}\right) \\
& =\sum_{y_{1}} \sum_{y_{2}} \psi_{1}\left(y_{1}, y_{2}\right) B_{2}\left(y_{2}\right) \\
& =\sum_{y_{1}} B_{1}\left(y_{1}\right)
\end{aligned}
$$

An alternative view: flow of beliefs $B_{i}($.$) from node i+1$ to node $i$

$$
\mathrm{y}_{1} \rightarrow \mathrm{y}_{2} \rightarrow \mathrm{y}_{3} \rightarrow \mathrm{y}_{4} \longrightarrow \mathrm{y}_{5}
$$

## Adding evidence

Given fixed values of a subset of variables $\mathbf{x}_{e}$ (evidence), find the
(1) Marginal probability queries over a small subset of variables:

- Find $\operatorname{Pr}($ Income='High | Degree='PhD')

$$
\operatorname{Pr}\left(x_{1}\right)=\sum_{x_{2} \ldots x_{m}} \operatorname{Pr}\left(x_{1} \ldots x_{n} \mid \mathbf{x}_{e}\right)
$$

(2) Most likely labels of remaining variables: (MAP queries)

- Find likely temperature at sensors in a room given readings from a subset of them

$$
\mathbf{x}^{*}=\operatorname{argmax}_{x_{1} \ldots x_{m}} \operatorname{Pr}\left(x_{1} \ldots x_{n} \mid \mathbf{x}_{e}\right)
$$

Easy to add evidence, just change the potential.

## Inference in HMMs

- Given,
- Graph $\begin{array}{lllllll}\mathrm{x}_{1} & \mathrm{x}_{2} & \mathrm{x}_{3} & \mathrm{x}_{4} & \mathrm{x}_{5} & \mathrm{x}_{6} & \mathrm{x}_{7}\end{array}$
- Potentials: $\operatorname{Pr}\left(y_{i} \mid y_{i-1}\right), \operatorname{Pr}\left(x_{i} \mid y_{i}\right)$
- Evidence variables: $\mathbf{x}=x_{1} \ldots x_{n}=o_{1} \ldots o_{n}$.
- Find most likely values of the hidden state variables.

$$
\mathbf{y}=y_{1} \ldots y_{n}
$$

$$
\operatorname{argmax}_{\mathbf{y}} \operatorname{Pr}(\mathbf{y} \mid \mathbf{x}=\mathbf{0})
$$

- Define $\psi_{i}\left(y_{i-1}, y_{i}\right)=\operatorname{Pr}\left(y_{i} \mid y_{i-1}\right) \operatorname{Pr}\left(x_{i}=o_{i} \mid y_{i}\right)$
- Reduced graph only a single chain of $y$ nodes.

$$
y_{1} \longrightarrow y_{2} \longrightarrow y_{3} \longrightarrow y_{4} \longrightarrow y_{5} \longrightarrow y_{6} \longrightarrow y_{7}
$$

- Algorithm same as earlier, just replace "Sum" with "Max"


## This is the well-known Viterbi algorithm

## Exact inference on trees

- Basic steps for marginal and MAP queries.
- Perform sum/max over leaf node potential and send resulting "belief" to parent.
- Each internal node, on getting beliefs from its children
(1) Multiplies incoming beliefs with its own potentials
(2) Performs sum/max on the result
(3) Sends resulting "belief" factor to parent.
- Root has the answer.


## Linear in the number of nodes in the graph

## Junction tree algorithms

- An optimal general-purpose algorithm for exact marginal/MAP queries
- Simultaneous computation of many queries
- Efficient data structures
- Complexity: $O\left(m^{w} N\right) w=$ size of the largest clique in (triangulated) graph, $m=$ number of values of each discrete variable in the clique. $\rightarrow$ linear for trees.
- Basis for many approximate algorithms.
- Many popular inference algorithms special cases of junction trees
- Viterbi algorithm of HMMs
- Forward-backward algorithm of Kalman filters


## Creating a junction tree from a graphical model

1. Starting graph

2. Triangulate graph

3. Create clique nodes

4. Create tree edges such that variables connected.

5) Assign potentials to exactly one subsumed clique node.


## Belief propagation on junction trees

- Each node c
- sends belief $B_{c \rightarrow c^{\prime}}($.$) to each of its neighbors c^{\prime}$
$\star$ once it has beliefs from every other neighbor $N(c)-\left\{c^{\prime}\right\}$.
- $B_{c \rightarrow c^{\prime}}()=$. belief that clique $c$ has about the distribution of labels to common variables $s=c \cap c^{\prime}$

$$
B_{c \rightarrow c^{\prime}}\left(\mathbf{x}_{s}\right)=\sum_{\mathbf{x}_{c-s}} \psi_{c}\left(\mathbf{x}_{c}\right) \prod_{d \in N(c)-\left\{c^{\prime}\right\}} B_{d \rightarrow c}\left(\mathbf{x}_{d \cap c}\right)
$$

Replace "sum" with "max" for MAP queries.
Compute marginal probability of any variable $x_{i}$ as
(1) $c=$ clique in JT containing $x_{i}$
(2) $\operatorname{Pr}\left(x_{i}\right) \propto \sum_{\mathbf{x}_{c-x_{i}}} \psi_{c}\left(\mathbf{x}_{c}\right) \prod_{d \in N(c)} B_{d \rightarrow c}\left(\mathbf{x}_{d \cap c}\right)$

## Example

$\begin{gathered}\boldsymbol{y}_{1} y_{2} \\ \boldsymbol{y}_{2}\end{gathered}$
$\boldsymbol{y}_{2} y_{3} y_{4}-\boldsymbol{y}_{3} \boldsymbol{y}_{4}-\boldsymbol{y}_{3} y_{4} y_{5}$

$$
\begin{array}{r}
\psi_{234}\left(\mathbf{y}_{234}\right)=\psi_{23}\left(\mathbf{y}_{23}\right) \psi_{34}\left(\mathbf{y}_{34}\right) \\
\psi_{345}\left(\mathbf{y}_{345}\right)=\psi_{35}\left(\mathbf{y}_{35}\right) \psi_{45}\left(\mathbf{y}_{45}\right) \\
\psi_{234}\left(\mathbf{y}_{12}\right)=\psi_{12}\left(\mathbf{y}_{12}\right)
\end{array}
$$

(1) Clique " 12 " sends belief $B_{12 \rightarrow 234}\left(y_{2}\right)=\sum_{y_{1}} \psi_{12}\left(\mathbf{y}_{12}\right)$ to its only neighbor.
(2) Clique " 345 " sends belief $B_{345 \rightarrow 234}\left(\mathbf{y}_{34}\right)=\sum_{y_{5}} \psi_{234}\left(\mathbf{y}_{345}\right)$ to "234"
(3) Clique " 234 " sends belief $B_{234 \rightarrow 345}\left(\mathbf{y}_{34}\right)=\sum_{y_{2}} \psi_{234}\left(\mathbf{y}_{234}\right) B_{12 \rightarrow 234}\left(y_{2}\right)$ to " 345 "
(4) Clique " 234 " sends belief
$B_{234 \rightarrow 12}\left(y_{2}\right)=\sum_{y_{4}} \psi_{234}\left(\mathbf{y}_{234}\right) B_{345 \rightarrow 234}\left(\mathbf{y}_{34}\right)$ to " 12 "
$\operatorname{Pr}\left(y_{1}\right) \propto \sum_{y_{2}} \psi_{12}\left(\mathbf{y}_{12}\right) B_{234 \rightarrow 12}\left(y_{2}\right)$

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## Graph Structure

(1) Manual: Designed by domain expert

- Used in applications where dependency structure is well-understood
- Example: QMR systems, Kalman filters, Vision (Grids), HMM for speech recognition and IE.
(2) Learnt: from examples
- NP hard to find the optimal structure.
- Widely researched, mostly posed as a branch and bound search problem.
- Useful in dyanmic situations
- Example: Selectivity estimation over attributes of arbitrary tables.


## Parameters in Potentials

(1) Manual: Provided by domain expert

- Used in infrequently constructured graphs, example QMR systems
- Also where potentials are an easy function of the attributes of connected graphs, example: vision networks.
(2) Learnt: from examples
- More popular since difficult for humans to assign numeric values
- Many variants of parameterizing potentials.
(1) Each potential entry a parameter, example, HMMs
(2) Potentials: combination of shared parameters and data attributes: example, CRFs. (Discussed in later with extraction)


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## Why approximate inference

- Exact inference is NP hard. Complexity: $O\left(w^{m}\right)$
- $w=$ tree width $=$ size of the largest clique in (triangulated) graph-1,
- $m=$ number of values of each discrete variable in the clique.
- Many real-life graphs produce large cliques on triangulation
- A $n \times n$ grid has a tree width of $n$
- A Kalman filter on $K$ parallel state variables influencing a common observation variable, has a tree width of size $K+1$


## Generalized belief propagation

- Approximate junction tree with a cluster graph where
(1) Nodes $=$ arbitrary clusters, not cliques in triangulated graph. Only ensure all potentials subsumed.
(2) Separator nodes on edges $=$ subset of intersecting variables.


## Example cluster graph

Starting graph


Junction tree.
Cluster graph


## Belief propagation in cluster graphs

- Graph can have loops, tree-based two-phase method not applicable.
- Many variants on scheduling order of propagating beliefs.
- Simple loopy belief propagation [Pea88]
- Tree-reweighted message passing [Kol04]
- Residual belief probagation [EMK06]
- Most have no guarantees of convergence
- Works well in practice, default method of choice.
- Success story: Error correction using Turbo code


## MCMC (Gibbs) sampling

- Useful when all else failes, guaranteed to converge to the optimal over infinite number of samples.
- Basic premise: easy to compute conditional probability $\operatorname{Pr}\left(x_{i} \mid\right.$ fixed values of remaining variables $)$


## Algorithm

- Start with some initial assignment, say

$$
\mathbf{x}^{1}=\left[x_{1}, \ldots, x_{n}\right]=[0, \ldots, 0]
$$

- For several iterations

For each variable $x_{i}$
Get a new sample $\mathbf{x}^{t+1}$ by replacing value of $x_{i}$ with a new value sampled according to probability $\operatorname{Pr}\left(x_{i} \mid x_{1}^{t}, \ldots x_{i-1}^{t}, x_{i+1}^{t}, \ldots, x_{n}^{t}\right)$

## Others

- Combinatorial algorithms for MAP [BVZ01, DTEK07, GDS07]
- Greedy algorithms: relaxation labeling
- Variational methods
- LP and QP based approaches


## Inference Task in DBNs



- Simplied representation of a dynamic Bayesian network
- Hidden state variables: x; Observed variables: o
- Assumed to be vector valued
- Given:
- Prior on the initial state: $p\left(\mathbf{x}_{0}\right)$
- How state evolves: $p\left(\mathbf{x}_{t} \mid \mathbf{x}_{t-1}\right)$
- How obsevations depend on state: $p\left(\mathbf{o}_{t} \mid \mathbf{x}_{t}\right)$
- Estimate the state at time $t$ given observations till time $t$
- The posterior distribution: $p\left(\mathbf{x}_{t} \mid \mathbf{o}_{1: t}\right)$


## Alternative Inference Tasks in DBNs



- Estimate the most likely sequence of states (for discrete $\mathbf{x}$ )
- $\operatorname{argmax}_{\mathbf{x}_{1: t}} p\left(\mathbf{o}_{1: t} \mid \mathbf{x}_{1: t}\right)$
(Cf. Viterbi Algorithm)
- Estimate the distribution of all states till time $t$
- $p\left(\mathbf{x}_{1: t} \mid \mathbf{0}_{1: t}\right)$
- Estimate the state at time $t$ given measurements till time $t+I$ (fixed-lag smoothing)
- $p\left(\mathbf{x}_{t} \mid \mathbf{o}_{1: t+l}\right)$
- Why ? Belief about the state at time $t$ may change drastically given future observations


## Exact Inference in DBNs



- Easy to write down
- Using Bayes rule and Chain rule, we get:

$$
p\left(\mathbf{x}_{t} \mid \mathbf{o}_{1: t}\right)=\frac{p\left(\mathbf{o}_{t} \mid \mathbf{x}_{t}\right) \int p\left(\mathbf{x}_{t} \mid \mathbf{x}_{t-1}\right) p\left(\mathbf{x}_{t-1} \mid \mathbf{o}_{1: t-1}\right) d \mathbf{x}_{t-1}}{p\left(\mathbf{o}_{t} \mid \mathbf{o}_{1: t-1}\right)}
$$

- Where:
$\star p\left(\mathbf{o}_{t} \mid \mathbf{x}_{t}\right)$ and $p\left(\mathbf{x}_{t} \mid \mathbf{x}_{t-1}\right)$ are known model parameters
$\star p\left(\mathbf{x}_{t-1} \mid \mathbf{o}_{1: t-1}\right)$ is available from the previous time
$\star p\left(\mathbf{o}_{t} \mid \mathbf{o}_{1: t-1}\right)=\int p\left(\mathbf{o}_{t} \mid \mathbf{x}_{t}\right) p\left(\mathbf{x}_{t} \mid \mathbf{o}_{1: t-1}\right) d \mathbf{x}_{t}$ is a normalization constant (so may not need to be evaluated)


## Exact Inference in DBNs



- However, can solve exactly in very few cases:
- Kalman filters: if the system is linear Gaussian
$\star$ If $p\left(\mathbf{x}_{t-1} \mid \mathbf{o}_{1: t-1}\right)$ is Gaussian and the system is linear Gaussian, $p\left(\mathbf{x}_{t} \mid \mathbf{o}_{1: t}\right)$ is Gaussian
$\star$ Very efficient
« Backward smoothing also easily doable
- Grid-based method: if the state space is discrete and finite
* Can compute the integral as a sum exactly


## Approximate Inference in DBNs



- Extended Kalman Filter
- Approximate the process as a linear Gaussian system
- Will fail if the posterior density not close to a Gaussian (e.g. if it is bimodal or heavily skewed)
- Approximate Grid-based methods
- Discretize the continuous state space using a grid
- Need sufficiently dense grid for good approximation
- Suffers from "curse of dimensionality"


## Approximate Inference in DBNs: Particle Filters



- Approximate the state using a set of weighted samples, called particles
- At time $t-1$, approximate $p\left(x_{t-1} \mid o_{1: t-1}\right)$ using $n$ particles:
- $\left\{\mathbf{x}_{t-1}^{1}, w_{t-1}^{1}\right\},\left\{\mathbf{x}_{t-1}^{2}, w_{t-1}^{2}\right\}, \cdots,\left\{\mathbf{x}_{t-1}^{n}, w_{t-1}^{n}\right\}$
- Can estimate any statistic using these particles
- e.g. $E\left(\mathbf{x}_{t-1} \mid \mathbf{o}_{1: t-1}\right) \approx \sum_{i=1}^{n} w_{t-1}^{i} \mathbf{x}_{t-1}^{i}$
- Inference Task: Generate a set of particles corresponding to $p\left(\mathbf{x}_{t} \mid \mathbf{o}_{1: t}\right)$ given $\mathbf{o}_{t}$


## Approximate Inference in DBNs: Particle Filters



- Generate one sample each from: $p\left(\mathbf{x}_{t} \mid \mathbf{x}_{t-1}^{i}, \mathbf{o}_{t}\right)$
- Assign weights as:

$$
w_{t}^{i} \propto w_{t-1}^{i} p\left(\mathbf{o}_{t} \mid \mathbf{x}_{t-1}^{i}\right)=w_{t-1}^{i} \int p\left(\mathbf{o}_{t} \mid \mathbf{x}_{t}^{\prime}\right) p\left(\mathbf{x}_{t}^{\prime} \mid \mathbf{x}_{t-1}^{i}\right) d \mathbf{x}_{t}^{\prime}
$$

- Problems:
- Requires sampling from $p\left(\mathbf{x}_{t} \mid \ldots\right)$ and computing $p\left(\mathbf{o}_{t} \mid \ldots\right)$
- Requires evaluating complex integrals
- Can solve in very few cases:
- $\mathbf{x}_{t}$ is discrete, or
- $p\left(\mathbf{x}_{t} \mid \mathbf{x}_{t-1}^{i}, \mathbf{o}_{t}\right)$ is Gaussian (evolution can still be non-linear)


## Approximate Inference in DBNs: Particle Filters



- Must use importance sampling
- Use an importance density $q()$ to generate samples from
- ...that closely approximates the true density $p()$
- No magic bullet for choosing $q()$
- Degeneracy issues
- After a while, a single particle has all the weight
- Need to resample periodically


## Approximate Inference in DBNs: Particle Filters



- Many other extensions/variations have been considered
- A lot more art than science at this point
- For an approachable introduction, see "A Tutorial on Particle Filters for On-line Nonlinear/Non-Gaussian Bayesian Tracking"; Arulampalam et al.; IEEE Trans. Signal Processing; 2002
- Our discussion heavily borrows from it


## More on graphical models

- Koller and Friedman book (Structured Probabilistic Models) not published yet but you could request authors for a draft.
- Kevin Murphy's brief online introduction (http://www.cs.ubc.ca/~murphyk/Bayes/bnintro.html)
- Graphical models. M. I. Jordan. Statistical Science (Special Issue on Bayesian Statistics), 19, 140-155, 2004. (http:
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## Part II: Applications

## Part II: Outline

## >Selectivity Estimation and Query Optimization

## >Probabilistic Relational Models

>Probabilistic Databases
>Sensor/Stream Data Management
>References

## Selectivity Estimation

- Estimating the intermediate result sizes that may be generated during query processing
> Equivalently, selectivities of predicates over tables
> Key to obtaining good plans during optimization

Customer

| SSN | .. | Income | .. | Homeowner? |
| :---: | :---: | :---: | :---: | :---: |
| .. | .. | 100000 | .. | Yes |
| .. | .. | 11000 | .. | Yes |
|  |  |  |  |  |

Single-table predicates:
income > 90000 and homeowner = yes (on customer)

Purchases

| SSN | Store | .. | Amount |
| :--- | :--- | :--- | :--- |
|  |  |  |  |
|  |  |  |  |
|  |  |  |  |

Multi-table predicates:
p.ssn = c.ssn and c.homeowner = "no" and p.amount > 10000 (over Customer c and Purchases p)

## Selectivity Estimation

> Optimizers make several independence assumptions

- Attribute value independence assumption
$>$ Attributes assumed to be independently distributed
$>$ Rarely true in practice

Customer

| SSN | .. | Income | .. | Homeowner? |
| :---: | :---: | :---: | :---: | :---: |
| .. | .. | 100000 | .. | Yes |
| .. | .. | 11000 | .. | Yes |
| .. | .. | 50000 | .. | No |
| .. | .. | 30000 | .. | No |
| .. | .. | 200000 | .. | Yes |

Estimate

$$
\text { p(income > } 90000 \text { and homeowner = yes) }
$$

as
p(income > 900000) *p(homeowner = yes)

Can result in severe underestimation

In reality:

$$
\begin{array}{r}
p(\text { income }>900000, \text { homeowner }=\text { yes }) \\
\approx p(\text { homeowner }=\text { yes })
\end{array}
$$

## Selectivity Estimation

> Join uniformity assumption
$>$ Tuples from one relation assumed equally likely to join with tuples from other relation
> Real datasets exhibit large skews

Customer
Purchases

| SSN | .. | Income | .. | Homeowner? |
| :---: | :---: | :---: | :---: | :---: |
| .. | .. | 100000 | .. | Yes |
| .. | .. | 11000 | .. | Yes |
| .. | .. | 50000 | .. | No |
| .. | .. | 30000 | .. | No |
| .. | .. | 200000 | .. | Yes |

## Selectivity Estimation

> Errors propagate exponentially [IC'91]
> Optimizers highly sensitive to underestimation
> May choose nested-loop joins
> Proposed solutions:
> Multi-dimensional histograms, wavelets [Pl'97,MVW'98, GKTD'00]
$>$ Expensive to build and maintain
$>$ Suffer from "curse of dimensionality" in high dimensions
> Random sampling [CDN'07]
$>$ Not as storage efficient
$>$ Few matching tuples for high dimensional queries
$>$ Need different sampling techniques for joins [AGPR'99]

## Selectivity Estimation using PGMs

> Eliminating attribute value independence assumption [GTK'01,DGR'01,LWV'03,PMW'03]

Customer

| SSN | age | Income | zipcode | Home <br> owner? |
| :---: | :---: | :---: | :---: | :---: |
| .. | .. | 100000 | .. | Yes |
| .. | .. | 11000 | .. | Yes |
| .. | .. | 50000 | .. | No |
| .. | .. | 30000 | .. | No |
| .. | .. | 200000 | .. | Yes |



## Selectivity Estimation using PGMs

> Eliminating attribute value independence assumption [GTK'01,DGR'01,LWV'03,PMW'03]

Customer

| SSN | age | Income | zipcode | Home <br> owner? |
| :---: | :---: | :---: | :---: | :---: |
| .. | .. | 100000 | .. | Yes |
| .. | .. | 11000 | .. | Yes |
| .. | .. | 50000 | .. | No |
| .. | .. | 30000 | .. | No |
| .. | .. | 200000 | .. | Yes |



## Selectivity Estimation using PGMs

> Eliminating join uniformity assumption ??

## Part II: Outline

## >Selectivity Estimation and Query Optimization

## >Probabilistic Relational Models

>Probabilistic Databases
>Sensor/Stream Data Management
>References

## Probabilistic Relational Models

> Real-world data often has highly relational structure
> There are entities and relationships between them etc
> Bayesian networks treat each one individually
> Will need a huge Bayesian network if we want to represent the uncertainties in such data
> PRMs: Generalization of PGMs to relational framework [FGKP'99]
> Allows dependence over attributes in different relations through joins
> Significantly enrich both Bayesian networks and relational model

## Relational Schema


$>$ Describes the types of objects and relations in the database

## Probabilistic Relational Model



## PRM: Semantics

Primary Keys


Fixed relational skeleton
Objects and links between them
Non-key (descriptive) attributes uncertain

## PRM: Semantics



PRM defines distribution over instantiations of attributes

## PRM: Semantics



Any aggregate function can be used:

## PRMs: Inference/ Generalizations

> Inference
$>$ Option 1: Construct and use the ground Bayesian network
$>$ Allows exact inference
$>$ Too large for any reasonable dataset
> Option 2: Approximate inference
$>$ E.g. using loopy belief propagation
> Generalizations
> Link uncertainty [GGFKT'02]
> Finer granularity dependencies using class hierarchies [dGK'00]
> Undirected dependencies
$>$ Relational Markov networks [TAK'02]
$>$ Relational dependency networks [ND'04]
> Exciting research area with huge potential impact in databases !!

## Part II: Outline

## >Selectivity Estimation and Query Optimization (continued)

## >Probabilistic Relational Models

>Probabilistic Databases
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## Selectivity Estimation using PGMs

> Eliminating join uniformity assumption [GTK'01]
> Using a Probabilistic Relational Model

Customer
Purchases

| SSN | .. | Income | .. | Homeowner? |
| :---: | :---: | :---: | :---: | :---: |
| .. | .. | 100000 | .. | Yes |
| .. | .. | 11000 | .. | Yes |
| .. | .. | 50000 | .. | No |
| .. | .. | 30000 | .. | No |
| .. | .. | 200000 | .. | Yes |


> Can estimate selectivities of joint predicates across relations

## Selectivity Estimation using PGMs

> Eliminating join uniformity assumption [GTK'01]
> Using a Probabilistic Relational Model
> Caveat:
> Should not use them blindly
$>$ Need to add and reason about a new join indicator variable
> Called a Statistical Relational Model
> Details in Getoor, Tasker, Koller; SIGMOD 2001.

## Discussion and Open Problems

> Approximate query processing?
$>$ Can use the proposed techniques as they are
$>$ However, no guarantees on the accuracy of results
$>$ Optimize accuracy for a given storage
$>$ To obtain guarantees, optimize for accuracy alone
$>$ May result in large CPDs
> Using learned PGMs during optimization
> Optimizers get better selectivity estimates, but otherwise unaware of the modeling
> May be beneficial to explore tighter integration

## Discussion and Open Problems

> Can exploit new types of query plans
> Based on horizontal partitioning of the relations [BBDW'05,DGHM'05,P'05]
> Use different plans for different partitions of relations based on attribute values
> Adaptive query processing
>PGMs ideal for learning the distribution properties
$>$ Significantly fewer parameters $\rightarrow$ easier to learn
> Many research challenges

## Part II: Outline

# >Selectivity Estimation and Query Optimization 

>Probabilistic Relational Models
>Probabilistic Databases
>Sensor/Stream Data Management
>References

## Probabilistic Databases

> Motivation: Increasing amounts of uncertain data
> From sensor networks
$>$ Imprecise data, data with confidence/accuracy bounds
$>$ Human-observed data
$>$ Statistical modeling/machine learning
$>$ Many models provide a distribution over a set of labels (e.g. classification models, HMMs)
> Approximate/vague queries
> Information extraction
> "Probability theory" provides a strong foundation to reason about this
> Caveat: It is not always clear if the underlying uncertainty measure follows probability theory semantics

## Probabilistic Databases

> Goal: Managing and querying data annotated with probabilities using databases
> Types of uncertainties
> Existence uncertainty
$>$ Don't know if a tuple exists in the database for sure
$>$ E.g. a sensor may detect a bird, but not 100\% sure
$>$ Attribute-value uncertainty
$>$ The value of an attribute is not known for sure
$>$ Instead a distribution over the possible values is provided
$>$ E.g. a sensor detects a bird for sure, but it may be a sparrow or a dove or something else
> Much work in recent years on both [DS'07]

## Correlations in Probabilistic Databases

> Much of the probabilistic data is naturally correlated
$>$ E.g. sensor data, data integration [AFM'06]
> Even if not..
$>$ Correlations get introduced during query processing

## Example Probabilistic Database

> Example from Dalvi and Suciu [2004]
Possible worlds


| instance | probability |
| :---: | :---: |
| $\{\mathrm{s} 1, \mathrm{~s} 2, \mathrm{t} 1\}$ | 0.12 |
| $\{\mathrm{~s} 1, \mathrm{~s} 2\}$ | 0.18 |
| $\{\mathrm{~s} 1, \mathrm{t} 1\}$ | 0.12 |
| $\{\mathrm{~s} 1\}$ | 0.18 |
| $\{\mathrm{~s} 2, \mathrm{t} 1\}$ | 0.08 |
| $\{\mathrm{~s} 2\}$ | 0.12 |
| $\{\mathrm{t} 1\}$ | 0.08 |
| $\}$ | 0.12 |

## Correlations during query processing

> Example from Dalvi and Suciu [2004]

|  |  |  |  |  |  |  | ${ }_{B}$ |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  | A | B | C | D | prob |
|  | A | B | prob |  | A | B | C | D | prob |
|  |  |  |  | $i 1$ | m | 1 | 1 | p | 0.24 |
| s1 | m | 1 | 0.6 | $i 2$ | n | 1 | 1 | p | 0.20 |
| s2 | n | 1 | 0.5 |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |
|  | C | D | prob |  | $\Pi_{D}($ |  |  |  |  |
| $t 1$ | 1 | p | 0.4 |  |  | C | D |  |  |
|  |  |  |  |  | $r$ | 1 | p |  |  |

## Correlations in Probabilistic Databases

> Much of the probabilistic data is naturally correlated

- E.g. sensor data, data integration
> Even if not.
$>$ Correlations get introduced during query processing
> Can use PGMs to capture such correlations


## Example: Mutual Exclusivity

Possible worlds

|  | S |  | prob | instance | probability |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | A | B |  | \{s1, s2, t1\} | 0 |
| s1 | m | 1 | 0.60.5 | \{s1, s2\} | 0.3 |
| s2 | n | 1 |  | \{s1, t1\} | 0 |
| $T$ |  |  | prob | \{s1\} | 0.3 |
|  |  |  | \{s2, t1\} | 0.2 |
| $t 1$ | C | D |  | \{s2\} | 0 |
|  | 1 | p |  | 0.4 | \{t1\} | 0.2 |
|  |  |  | \{\} |  | 0 |


| $\boldsymbol{x}_{\mathbf{s 1} \boldsymbol{1}}$ | $\boldsymbol{x}_{\boldsymbol{t 1}}$ | $\boldsymbol{f 1 ( )}$ |
| :---: | :---: | :---: |
| 0 | 0 | 0 |
| 0 | 1 | 0.4 |
| 1 | 0 | 0.6 |
| 1 | 1 | 0 |


| $\boldsymbol{X}_{\mathbf{s 2}}$ | $\boldsymbol{f 2 ( )}$ |
| :---: | :---: |
| 0 | 0.5 |
| 1 | 0.5 |

Possible worlds (if desired) computed using inference

## Query Evaluation [SD' 07]

> Introduce new factors as new tuples generated

|  | - $s$ |  |
| :---: | :---: | :---: |
|  | A | B |
| s1 | m | 1 |
| s2 | n | 1 |
|  |  |  |
|  | c | D |
| $t 1$ | 1 | p |



## Query Evaluation [SD’ 07]

> Introduce new factors as new tuples generated

| $\boldsymbol{X}_{\mathbf{s} \mathbf{1}}$ | $\boldsymbol{X}_{\boldsymbol{t 1}}$ | $\boldsymbol{X}_{\boldsymbol{i 1} 1}$ | $\boldsymbol{f}^{\boldsymbol{A N D}}$ |
| :---: | :---: | :---: | :---: |
| 0 | 0 | 0 | 1 |
| 0 | 1 | 0 | 1 |
| 1 | 0 | 0 | 1 |
| 1 | 1 | 0 | 0 |
| 0 | 0 | 1 | 0 |
| 0 | 1 | 1 | 0 |
| 1 | 0 | 1 | 0 |
| 1 | 1 | 1 | 1 |



## Query Evaluation [SD’ 07]

> Introduce new factors as new tuples generated

| $x_{i 1}$ | $x_{i 2}$ | $x_{r}$ | for |
| :---: | :---: | :---: | :---: |
| 0 | 0 | 0 | 1 |
| 0 | 1 | 0 | 0 |
| 1 | 0 | 0 | 0 |
| 1 | 1 | 0 | 0 |
| 0 | 0 | 1 | 0 |
| 0 | 1 | 1 | 1 |
| 1 | 0 | 1 | 1 |
| 1 | 1 | 1 | 1 |



## Query Evaluation [SD’ 07]

> Query evaluation ミ Inference !!
> Can use variable elimination or junction tree..
> Can also use approximate inference algorithms


## Discussion

> Similar to intensional semantics [FR'97,DS'04]
Except this exposes the structure of the problem
$>$ Can exploit for more efficient execution
> "Safe plans" on independent tuples generate tree-structured models
$>$ Highly efficient inference

## Part II: Outline

## >Selectivity Estimation and Query Optimization

>Probabilistic Relational Models
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>References

## Motivation

> Unprecedented, and rapidly increasing, instrumentation of our every-day world


Wireless sensor networks


## Sensor Data Management: Challenges

> Data streams generated at very high rates
> Strong spatio-temporal correlations in the data
> In-network, distributed processing tasks
> Global inference needed to achieve consistency
$>$ Need for higher-level modeling over the data
$>$ Typically imprecise, unreliable and incomplete data
$>$ Measurement noises, failures, biases ...
> Application often need higher-level, hidden variables
>Pattern recognition, forming stochastic descriptions..

## Sensor Data Management

> A statistical/probabilistic model of the data must be incorporated in the sensor data processing
> Probabilistic graphical models are a natural
> Can capture and exploit the spatial and temporal nature of the underlying process
> Minimize the number of parameters
$>$ Amenable to distributed processing

## Outline

$>$ A generic temporal model for sensor stream data
> Applications
> Online estimation and filtering
> Inferring hidden variables
>Model-based query processing
>In-network inference
>Miscellaneous

True temperature


## SENSOR

 NETWORK

## SENSOR

 NETWORK

## Markov Property

Interpretation: $\left\{X_{i, t+1}\right\}$ independent of $\left\{X_{i, t-1}\right\}$ given $\left\{X_{i, t}\right\}$


## SENSOR



State evolution can be modeled as a Dynamic Bayesian Network


## Parameters?

(1) System model

Prior: $p\left(x_{1,0}, x_{2,0}, x_{3,0}\right)$
Evolution: $p\left(x_{1, t}, x_{2, t}, x_{3, t} \mid x_{1, t-1}, x_{2, t-1}, x_{3, t-1}\right)$


## Parameters?

(2) Measurement model

$$
p\left(O_{1, t}, O_{2, t}, O_{3, t} \mid x_{1, t}, x_{2, t}, x_{3, t}\right)
$$

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## Application: Online Estimation and Filtering

> Using linear Gaussian dynamical systems
> E.g. Kalman Filters
> Task: Estimating velocity and location from noisy GPS readings


## Application: Online Estimation and Filtering

> Using linear Gaussian dynamical systems
> E.g. Kalman Filters
> Task: Estimating velocity and location from noisy GPS readings

$$
\begin{aligned}
& p\left(v_{t} \mid v_{t-1}\right)=N\left(v_{t-1}, \sigma_{v}\right) \\
& p\left(x_{t} \mid x_{t-1}, v_{t}\right)=N\left(x_{t-1}+v_{t}, \sigma_{x}\right) \\
& p\left(o_{t} \mid x_{t}\right)=N\left(x_{t}, \sigma_{o}\right) \\
& \text { Prior: } p\left(v_{0}\right), p\left(x_{0}\right)
\end{aligned}
$$



## Application: Online Estimation and Filtering

> Using linear Gaussian dynamical systems
> E.g. Kalman Filters
> Closed-form equations for state estimation [Kalman'60]
> Because of the linear Gaussian assumption
> LDS Applications:
> Autopilot
> Inertial guidance systems
> Radar tracker
> Economics...
> In databases:
> Adaptive stream resource management [JCW'04]
> Approximate querying in sensor networks [DGHHM'04]

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## Application: Inferring Hidden Variables

> Inferring "transportation mode"/ "activities" [P+04]
> Using easily obtainable sensor data (GPS, RFID proximity data)
$>$ Can do much if we can infer these automatically
office



## Application: Inferring Hidden Variables

> Inferring "transportation mode"/ "activities" [P+04]
> Using easily obtainable sensor data (GPS, RFID proximity data)
$>$ Can do much if we can infer these automatically


## Application: Inferring Hidden Variables

Use a dynamic Bayesian network to model the system state

Time $=t \quad$ Time $=t+1$
Transportation Mode: Walking, Running, Car, Bus

True velocity and location

Observed location

## Application: Inferring Hidden Variables

Given a sequence of observations $\left(O_{t}\right)$, infer most likely $M_{t}$ 's that explain it.
Alternatively, could provide a probability distribution on the possible $M_{t}$ 's.

$$
\text { Time }=t \quad \text { Time }=t+1
$$

Transportation Mode:
Walking, Running, Car, Bus

True velocity and location

Observed location

## Outline

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# Application: Model-based Query Processing [DGMHH' 04, SBEMY' 06] 



| Observation Plan |  | Data |
| :---: | :---: | :---: |
| \{[temp, 1], |  | 1, temp = 22.73, |
| [voltage, 3], |  | 3 , voltage $=2.73$ |
| [voltage, 6]\} | 1 | 6 , voltage $=2.65$ |

SENSOR NETWORK

Application: Model-based Query Processing [DGMHH' 04, SBEMY' 06]


## Advantages:

Exploit correlations for efficient approximate query processing
Handle noise, biases in the data
Predict missing or future values

## Outline

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## Application: In-network Inference [PGM’ 05]

> Often need to do in-network, distributed inference
$>$ Target tracking through information fusion
> Optimal control (for actuation)
$>$ Distributed sensor calibration (using neighboring sensors)
> In-network regression or function fitting


## Application: In-network Inference [PGM' 05]

> Often need to do in-network, distributed inference
$>$ Target tracking through information fusion
> Optimal control (for actuation)
> Distributed sensor calibration (using neighboring sensors)
> In-network regression or function fitting
> Obey a common structure:
> Each sensor has/observes some local information
$>$ Information across sensors is correlated
> The information must be combined together to form a global picture
$>$ The global picture (or relevant part thereof) should be sent to each sensor

## Application: In-network Inference [PGM’ 05]

> Naïve option:
> Collect all data at the centralized base station - too expensive
> Using graphical models
> Form a junction tree on the nodes directly
> Use message passing (or loopy propagation [CP'03]) to form a global consistent view


## Application: In-network Inference [PGM’ 05]

> Naïve option:
> Collect all data at the centralized base station - too expensive
> Using graphical models:
$>$ Form a junction tree on the nodes directly
> Use message passing (or loopy propagation [CP'03]) to form a global consistent view


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## Applications: Miscellaneous

> Data compression [CDHH'06]
$>$ Central task in sensor networks
$>$ Collect all observed data at the base station at specified frequency
> Challenge: How to exploit the correlations
>Probabilistic graphical models ideally suited:
$>$ Can capture the correlations/pattern
$>$ Allow for local checking of constraints/correlations
> Fault/anomaly detection
> Distributed regression
> Sensor calibration

## Part II: Outline

## >Selectivity Estimation and Query Optimization

>Probabilistic Relational Models
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## Part III: Graphical models for Information

 extraction and data integration
# Graphical models for Information extraction and data integration 

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## Information Extraction (IE) \& Integration

The Extraction task: Given,

- E: a set of structured elements
- S: unstructured source S extract all instances of $E$ from $S$

The integration task: Given

- database of existing inter-linked entities

Resolve which entities are the same.
■ Many versions involving many source types

- Actively researched in varied communities
- Several tools and techniques
- Several commercial applications


## IE from free format text

- Classical Named Entity Recognition
- Extract person, location, organization names

According to Robert Callahan, president of Eastern's flight attendants union, the past practice of Eastern's parent, Houston-based Texas Air Corp., has involved ultimatums to unions to accept the carrier's terms

■Several applications
-News tracking

- Monitor events
-Bio-informatics
- Protein and Gene names from publications
-Customer care
-Part number, problem description from emails in help centers


## Text segmentation

House

| number | Building | Road | City |
| ---: | :--- | :--- | :--- | :--- |
| 4089 | Whispering Pines | Nobel Drive | Zip |
| San Diego | CA | 92122 |  |

Author

Year Title Journal<br>Volume<br>P.P. Wangikar, T.P. Graycar, D.A. Estell, D.S. Clark, J.S. Dordick (1993) Protein and Solvent Engineering of Subtilising BPN' in Nearly Anhydrous Organic Media J.Amer. Chem. Soc. 115, 12231-12237.

## Information Extraction (IE)

- Many different uses
- Disease outbreaks from news articles
- Addresses/Qualifications from resumes for HR DBs
- Titles/Authors/Venue/Year from citations
- Room attributes from hotel websites
- Many approaches
- Rules-based -------- Statistical learners
- Varying levels of difficulty
- Wrappers for machine generated pages
- 
- Fact extraction from speech transcripts


## Graphical models in Extraction \& Dedup

- State of the art: Conditional Random Fields
- IE Models
- Basic IE model (Chain)
- IE with collective labeling of repeated words
- De-duplication models
- Basic pair-wise model
- Collective de-duplication of relational data
- Collective de-duplication of multiple networked entities


## Conditional Random Fields

Special undirected graphical model

1. Conditional distribution $\operatorname{Pr}(\mathbf{y} \mid \mathbf{x})$ where $\mathbf{y}=y_{1} y_{2 . . .} y_{n}$
2. Graph: over the interdependent components of $\mathbf{y}$
3. Potentials: weighted sum of features over $\mathbf{x}$

[Lafferty et al 2001]

## Chain model

## My review of Fermat's last theorem by S. Singh

| $\boldsymbol{t}$ | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\boldsymbol{x}$ | My | review | of | Fermat's | last | theorem | by | S. |
| $\boldsymbol{y}$ | Other | Other | Other | Title | Title | Title | other | Author |
|  | Author |  |  |  |  |  |  |  |

$$
\begin{gathered}
y_{1}-y_{2}-y_{3}-y_{4}-y_{5} \underbrace{-y_{6}}-y_{7}-y_{8}-y_{9} \\
\mathbf{f}\left(y_{i}, y_{i-1}, i, \mathbf{x}\right)
\end{gathered}
$$

## Features

- Feature vector for each position

- Examples
$f_{2}\left(y_{i}, \mathbf{x}, i, y_{i-1}\right)=1$ if $y_{i}$ is Person $\& x_{i}$ is Douglas

$$
f_{3}\left(y_{i}, \mathbf{x}, i, y_{i-1}\right)=1 \text { if } y_{i} \text { is Person \& } y_{i-1} \text { is Other }
$$

- Parameters: weight for each feature (vector)

$$
\mathbf{W}=W_{1} W_{2} \ldots W_{|\mathbf{f}|} \text { Machine learnt }
$$

## Features in typical extraction tasks

- Words
- Orthographic word properties
- Capitalized? Digit? Ends-with-dot?
- Part of speech
- Noun?
- Match in a dictionary
- Appears in a dictionary of people names?
- Appears in a list of stop-words?
- Fire these for each label and
- The token,
- W tokens to the left or right, or
- Concatenation of tokens.


## Examples: features with weights (publications).

| $\#$ | Name | Person | Location | Other |
| :--- | :--- | :--- | :--- | :--- |
| 1 | $\mathrm{x}_{\mathrm{i}}$ is noun | 1.2 | 1.2 | -0.5 |
| 4 | "at" in $\left\{\mathrm{x}_{\mathrm{i}-1}, \mathrm{x}_{\mathrm{i}-2}\right\}$ | -0.3 | 3 | 0.2 |
| 7 | $\mathrm{x}_{\mathrm{i}-1} \mathrm{x}_{\mathrm{i}}$ in people names dictionary | 3 | -0.4 | 0 |
| 10 | $\mathrm{x}_{\mathrm{i}-1}$ is single caps \& dot. | 2.1 | -1.0 | -0.1 |
| 13 | $\mathrm{y}_{\mathrm{i}-1}$ is Location | -1.5 | 0.3 | 1.0 |
| . | .. |  |  |  |
| . |  |  |  |  |
| 100000 | .. |  |  |  |

A large number

## Typical numbers

- Seminars announcements (CMU):
- speaker, location, timings
- SVMs for start-end boundaries
- 250 training examples
- F1: 85\% speaker, location, 92\% timings (Finn \& Kushmerick '04)
- Jobs postings in news groups
- 17 fields: title, location, company,language, etc
- 150 training examples
- F1: 84\% overall (LP2)
(Lavelli et al 04)


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## Collective labeling

- Y has character.
- Mr. X lives in Y.
- X buys Y Times daily.


Associative potentials $\phi_{e}(i, i)>\phi_{e}(i, j)$

Other applications of associative potentials
Social network analysis: "friends of smokers are smokers" Image segmentation: "nearby pixels get the same label" Spam detection: "spam pages are pointed to by spams"

## Starting graphs (..of an extraction task from addresses)



## Graph after collective edges



Part III: Information Extraction and Data Integration

## Algorithms for collective inference

- Exact: intractable
- Approximate
- Loopy Belief Propagation
- Message passing (MP) on edges of the graph
- [Bunescu \& Mooney ’04], [Sutton \& McCallum '04]
- Gibbs Sampling
- [Finkel \& Manning. '05]
- Greedy local search (ICM)
- [Lu \& Getoor'03]
- A special two-pass variant: [Krishnan \& Manning '06]
- Generic techniques, no guarantees


## Associative Markov Networks

- Graph with only associative edge potentials and node potentials

- Optimal for $m=2.1 / 2$ approximation for $m>2$
- Min-cut with $\alpha$-expansion (Boykov '99)
- LP-based metric labeling algorithms (Klienberg \& Tardos ‘02)
- BP with TRW-S message schedules (Kolmogorov \& Wainwright, ‘05)

Not directly usable Slow Worse guarantees

## Generalized Belief propagation

BP on clusters of cliques and chains with single node separators


- Basic MP step: Compute max-marginals for a separator node $\rightarrow$ MAP for each label of the node.
- MAP algorithms for chains $\boldsymbol{\rightarrow}$ easy and efficient.
- MAP algorithms for cliques $\rightarrow$ combinatorial algorithms can be used for this. (Gupta et al 2007)


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## Basic dedup problem

- Given a pair of records $x_{1}, x_{2}$, predict " $y$ " to denote if they are the same or not.

$$
\begin{aligned}
& X_{1} \text { Johnson Laird, Philip N. (1983). Mental models. } \\
& \text { Cambridge, Mass.: Harvard University Press. } \\
& X_{2} \text { P. N. Johnson-Laird. Mental Models: Towards a } \\
& \text { Cognitive Science of Language, Inference, and } \\
& \text { Consciousness. Cambridge University Press, } 1983
\end{aligned}
$$

- CRF: $\operatorname{Pr}\left(\mathrm{y} \mid \mathrm{x}_{1}{ }^{\prime} \mathrm{x}_{2}\right)$ where
- Features: list of similarity functions between record pairs.
- Graph: trivial single node graph


## Multi Attribute Similarity

|  | $f_{1} \quad f_{2} \ldots f_{n}$ |  |
| :---: | :---: | :---: |
| Record 1 D | $1.0 \begin{array}{llll} & 0.4 & & 0.2\end{array}$ | 1 |
| Record 2 |  |  |
| Record 1 N | $0.0 \quad 0.1 \ldots 0.3$ | 0 |
| Record 3 |  |  |
| Record 4 D | $0.3 \begin{array}{lllll} & 0.4 & & 0.4\end{array}$ | 1 |
| Record 5 |  |  |

All-Ngrams*0.4 + AuthorTitleNgram*0.2
-0.3 YearDifference $+1.0^{*}$ AuthorEditDis
$+0.2^{*}$ PageMatch $-3>0$

## Learners:

Support Vector Machines (SVM) Logistic regression, Linear regression, Perceptron

| 0.0 | 0.1 | $\ldots$ | 0.3 | $?$ |
| :--- | :--- | :--- | :--- | :--- |
| 1.0 | 0.4 | $\ldots$ | 0.2 | $?$ |
| 0.6 | 0.2 | $\ldots$ | 0.5 | $?$ |
| 0.7 | 0.1 | $\ldots$ | 0.6 | $?$ |
| 0.3 | 0.4 | $\ldots$ | 0.4 | $?$ |
| 0.0 | 0.1 | $\ldots$ | 0.1 | $?$ |
| 0.3 | 0.8 | $\ldots$ | 0.1 | $?$ |
| 0.6 | 0.1 | $\ldots$ | 0.5 | $?$ |


$|$| 0.6 | 0.2 | $\ldots$ | 0.5 | 0 |
| :---: | :---: | :---: | :---: | :---: |
| 0.7 | 0.1 | $\ldots$ | 0.6 | 0 |
| 0.3 | 0.4 | $\ldots$ | 0.4 | 1 |
| 0.0 | 0.1 | $\ldots$ | 0.1 | 0 |
| 0.3 | 0.8 | $\ldots$ | 0.1 | 1 |
| 0.6 | 0.1 | $\ldots$ | 0.5 | 1 |

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## De-duplication of relational records

Collectively de-duplirate entities and its many attributes

| Record | Title | Author | Venue |
| :---: | :---: | :---: | :---: |
| $b_{1}$ | "Record Linkage using CRFs" | "Linda Stewart" | KDD-2003" |
| $b_{2}$ | "Record Linkage using CRFs" | "Linda Stewart" | "9th SIGIL |
| $b_{3}$ | "Learning Boolean Formulas" | "Bill | "KD |
| $b_{4}$ | "Learning of Boolean Expressions" | "William Johnson" | 9 th SIGI |

Associate variables for predictions for each attribute $k$ each record pair ( $\mathrm{i}, \mathrm{j}$ ) $\quad A_{\mathrm{ij}}{ }_{\mathrm{ij}}$
for each record pair $\quad R_{i j}$ from Parag \& Domingos 2005

## Graphical model

## Potentials

- Independent scores
- $\mathrm{s}_{\mathrm{k}}\left(\mathrm{A}^{\mathrm{k}}, \mathrm{a}_{\mathrm{i}}, \mathrm{a}_{\mathrm{j}}\right)$ Attribute-level
- Any classifier on various text similarities of attribute pairs
- $s\left(R, b_{i}, b_{j}\right)$ Record-level
- Any classifier on various similarities of all $k$ attribute pairs
- Dependency scores
- $d_{k}\left(A^{k}, R\right)$ : record pair, attribute pair



## Joint de-duplication steps

- Jointly pick 0/1 labels for all record pairs Rij and all $K$ attribute pairs $A^{\mathrm{k}}{ }_{\mathrm{ij}}$ to maximize sum of potentials
- Typical graphical model inference problem
- Efficient algorithm possible because of special forms of potentials
- dependency scores associative
- $d k(1,1)+d k(0,0)>=d k(1,0)+d k(0,1)$


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## Collective linkage: set-oriented data

| P1 | D White, J Liu, A Gupta |
| :--- | :--- |
| P2 | Liu, Jane \& J Gupta \& White, Don |
| P3 | Anup Gupta |
| P4 | David White |



## Scoring functions

- $\mathrm{S}\left(\mathrm{A}_{\mathrm{ij}}\right)$ Attribute-level
- Text similarity
- $S\left(A_{i j}, N_{i j}\right)$ Dependency with labels of co-author set
- Fraction of co-author set assigned label 1.
- Score: $\alpha \mathrm{s}\left(\mathrm{A}_{\mathrm{ij}}\right)+(1-\alpha) \mathrm{s}\left(\mathrm{A}_{\mathrm{ij}}, \mathrm{N}_{\mathrm{ij}}\right)$


## Inference Algorithm

Exact inference hard

- MCMC algorithm in (Bhattacharya and Getoor, 2007)


## Concluding remarks

- Graphical models provide a unified and flexible modeling of many extraction and integration tasks
- Much work is still needed in converting these to methods of choice in commercial systems
- Scalable algorithms
- Skillful integration of manual rules with statistical methods
- Feedback on when the statistical method failes
- Robust feature design so as to not overfit on the training data.

