

Introduction Problem •State explosion: number of states in the reachability graph is exponential to number of processes.

Incremental Reachability **Analysis**

- Building a reduced LTS L_qr.
- Reduced LTS must be semantically equivalent to L_a.
- Strong equivalence:
 - 2 LTSs whose behaviors are indistinguishable to an observer, including ??events.

Incremental Reachability **Analysis**

- Observational equivalence:
 - •2 LTSs whose behavior are indistinguishable when ??events are invisible.
- To build reduced LTS
 - Subsystems are successively composed and simplify.
 - Simplify be removing some ??events.
 - Simpler but observationally equivalent LTS

Incremental Reachability **Analysis**

However, paths from the reduced graph cannot be used for deterministic testing.

Annotated LTS

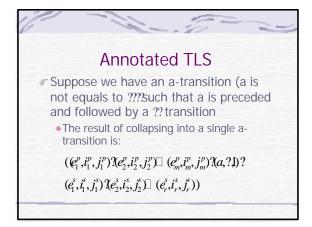
- e-transition (non ?)
 - $(\overline{e},i,?)$ process *i* performs this send event and the identifier of the receiver will be determined during synchronization.
 - (e,?,j) process j performs receive event with the identifier of the sender to be determined during synchronization.
- - Synchronize 2 matching events: (e, i, j)

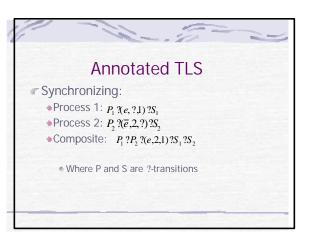
Annotated TLS

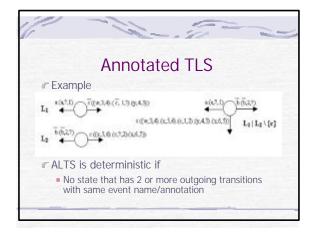
- ALTS reduction:
 - Suppose we have a sequence of ?? transitions:

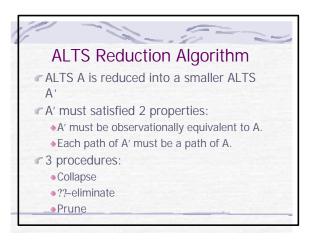
 $?_1(e_1,i_1,j_1)? ?_2(e_2,i_2,j_2)? \square ? ?_m(e_m,i_m,j_m)$

•We can collapse them into a single ?? transition: $((e_1, i_1, j_1)?(e_2, i_2, j_2) \Box (e_m, i_m, j_m))$



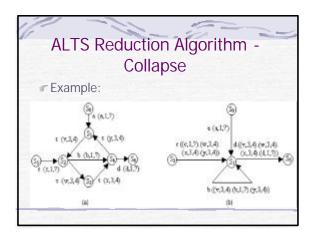


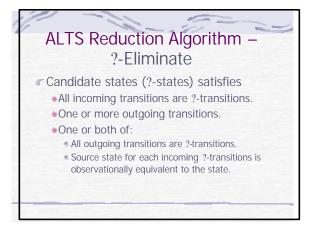


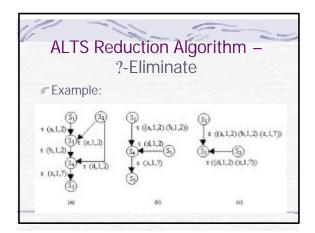


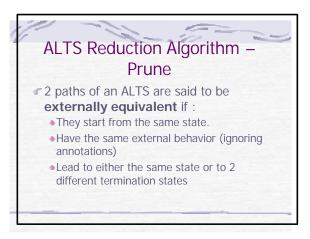
ALTS Reduction Algorithm - Collapse ?k be a sequence of ?-transitions (length k). 2 states are, s_1 , s_2 in the same ?-component if: $s_1 ? ?^{s_1}? s_2 \text{ and}$ $s_2 ? ?^{s_2}? s_1$

ALTS Reduction Algorithm Collapse Pick 1 state from ?-component. Call this the survivor state. The survivor state will remain while we remove the rest. Observable transitions are retained.

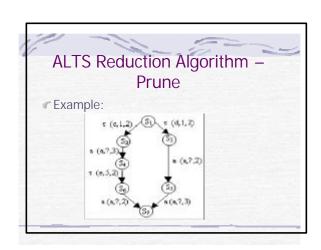


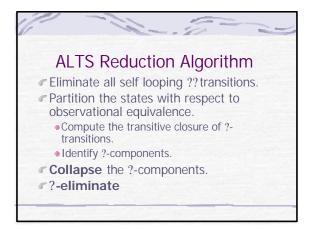


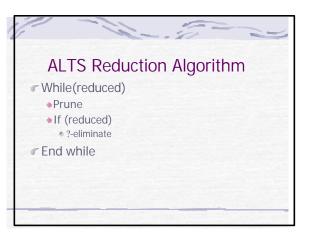




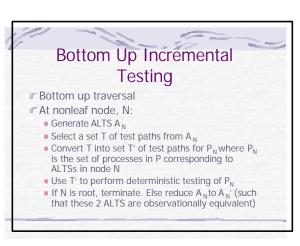
ALTS Reduction Algorithm — Prune Suppose s has e-transitions to s' and s" and s' and s" are observational equivalent. For every path that starts at s and has an e-transition to s', there is at least one externally equivalent path that also starts at s and has an e-transition into s". Delete one of the transitions. After deleting, some other states may become unreachable. These states are also removed.

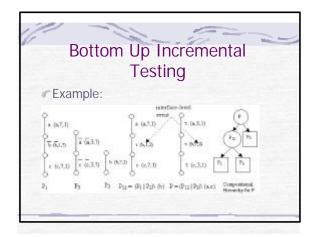




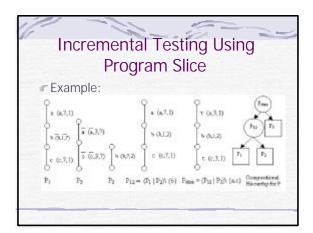


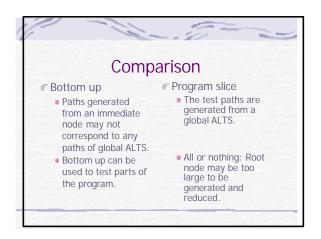
Bottom Up Incremental Testing For intermediate node, N: Synchronizations are at interface level if they occur among immediate children of N. Lower-level synchronizations occur within each immediate child of N.

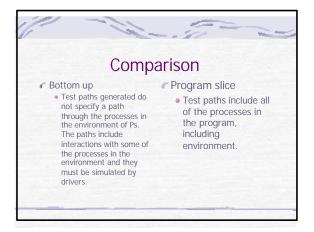


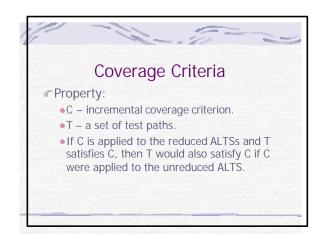


Incremental Testing Using Program Slice After constructing A_N we replace each interface-level transition label ??of A_N with a non-??label. Bottom up traversal and reduction of intermediate nodes until root node is reached. The interface level synchronizations of A_N remain in the ALTS. The resulting root represents a slice of program P. The paths selected focus on the coverage of interface level transitions of node N.

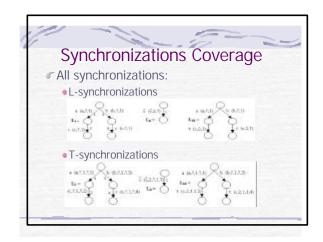








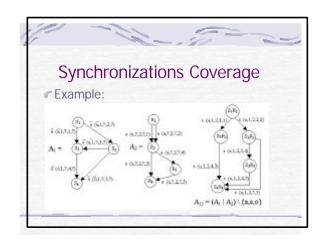


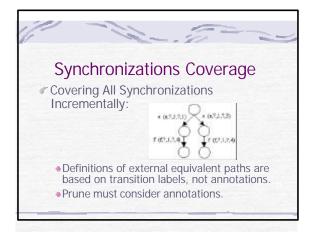


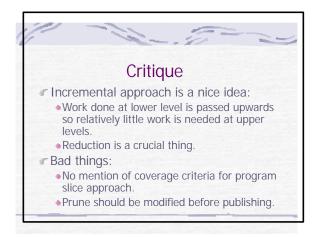












Conclusion

- Incremental approach to testing of concurrent programs.
- Advantages:

 - Alleviates state explosion problems.Supports incremental development and testing.
 - Focuses on faults in the interactions of concurrent processes.