CMSC 330: Organization of Programming Languages

Context-Free Grammars: Pushdown Automaton

Reminders

• Project 2 Due Oct. 12

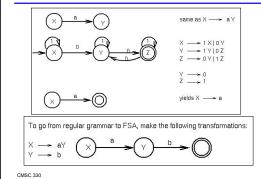
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Regular expressions and CFGs

	Description	Machine
regular languages	regular expressions	DFAs, NFAs
context-free languages	context-free grammars	pushdown automata (PDAs)

- · Programming languages are not regular
 - Matching (an arbitrary number of) brackets so that they are balanced
- Usually almost context-free, with some hacks CMSC 330

Equivalence of DFA and regular grammars



Pushdown Automaton (PDA)

- A pushdown automaton (PDA) is an abstract machine similar to the DFA
 - Has a finite set of states
 - Also has a pushdown stack
- Moves of the PDA are as follows:
 - An input symbol is read and the top symbol on the stack is read
 - Based on both inputs, the machine
 - · Enters a new state, and
 - Writes zero or more symbols onto the pushdown stack
 - Or pops zero or more symbols from the stack
 - String accepted if the stack is empty AND the string has ended

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Power of PDAs

- · PDAs are more powerful than DFAs
 - aⁿbⁿ, which cannot be recognized by a DFA, can easily be recognized by the PDA
 - Stack all a symbols and, for each b, pop an a off the stack.
 - If the end of input is reached at the same time that the stack becomes empty, the string is accepted

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Context-free Grammars in Practice

- Regular expressions are used to turn raw text into a string of tokens
 - E.g., "if", "then", "identifier", etc.
 - Whitespace and comments are simply skipped
 - These tokens are the input for the next phase of compilation
 - Standard tools used include lex and flex
 - · Many others for Java
- · CFGs are used to turn tokens into parse trees
 - This process is called parsing
- Standard tools used include yacc and bison
- Those trees are then analyzed by the compiler, which eventually produces object code

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Parsing

- There are many efficient techniques for turning strings into parse trees
 - They all have strange names, like LL(k), SLR(k), LR(k)...
 - Take CMSC 430 for more details
- We will look at one very simple technique: recursive descent parsing
 - This is a "top-down" parsing algorithm because we're going to begin at the start symbol and try to produce the string

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Example

$$E \rightarrow id = n \mid \{L\}$$

 $L \rightarrow E; L \mid \epsilon$

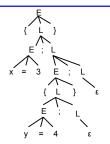
- Here n is an integer and id is an identifier
- · One input might be
 - $\{ x = 3; \{ y = 4; \}; \}$
 - This would get turned into a list of tokens { x = 3 ; { y = 4 ; } ; }
 - And we want to turn it into a parse tree

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Example (cont'd)

$$E \rightarrow id = n \mid \{L\}$$

 $L \rightarrow E ; L \mid \epsilon$
 $\{x = 3; \{y = 4; \}; \}$



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Parsing Algorithm

- Goal: determine if we can produce a string to be parsed from the grammar's start symbol
- · At each step, we'll keep track of two facts
 - What tree node are we trying to match?
 - What is the *next* token (*lookahead*) of the input string?
- · There are three cases:
 - If we're trying to match a terminal and the next token (lookahead) is that token, then succeed, advance the lookahead, and continue
 - If we're trying to match a nonterminal then pick which production to apply based on the lookahead
 - Otherwise, fail with a parsing error

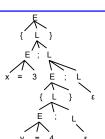
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Example (cont'd)

$$E \rightarrow id = n \mid \{L\}$$

 $L \rightarrow E ; L \mid \epsilon$



{ x = 3 ; { y = 4 ; } ; } lookahead

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Definition of First(γ)

- First(y), for any terminal or nonterminal y, is the set of initial terminals of all strings that y may expand to
 - We'll use this to decide what production to apply

Definition of First(y), cont'd

- For a terminal a, First(a) = { a }
- For a nonterminal N:
 - If N → ε, then add ε to First(N)
 - If $N \rightarrow \alpha_1 \alpha_2 \dots \alpha_n$, then (note the α_i are all the symbols on the right side of one single production):
 - Add First($\alpha_1\alpha_2$... α_n) to First(N), where First(α_1 α_2 ... α_n) is defined as
 - First(α_1) if $\epsilon \notin First(\alpha_1)$
 - Otherwise (First(α_1) ϵ)U First(α_2 ... α_n)
 - If $\epsilon \in First(\alpha_i)$ for all i, $1 \le i \le k$, then add ϵ to First(N)

Examples

```
E \rightarrow id = n \mid \{L\}
                                         E \rightarrow id = n | \{L\} | \epsilon
 L \rightarrow E; L \mid \epsilon
                                        L \rightarrow E; L \mid \epsilon
                                         First(id) = { id }
 First(id) = { id }
 First("=") = { "=" }
                                         First("=") = { "=" }
 First(n) = \{ n \}
                                        First(n) = \{ n \}
                                         First("{")= { "{" }
 First("{")= { "{" }
 First("}")= { "}" }
                                         First("}")= { "}" }
 First(";")= { ";" }
                                         First(";")= { ";" }
                                         First(E) = \{ id, "\{", \epsilon \} \}
 First(E) = { id, "{" }
First(L) = \{ id, "\{", \epsilon \} \}
                                         First(L) = \{ id, "\{", "; ", \epsilon_{i} \} \}
```

Implementing a Recursive Descent Parser

- · For each terminal symbol a, create a function parse a, which:
 - If the lookahead is a it consumes the lookahead by advancing the lookahead to the next token, and returns
 - Otherwise fails with a parse error if the lookahead is not
- For each nonterminal N, create a function parse_N
 - This function is called when we're trying to parse a part of the input which corresponds to (or can be derived
 - parse_S for the start symbol S begins the process

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Implementing a Recursive Descent Parser, con't.

- The body of parse_N for a nonterminal N does the following:
 - Let $N \rightarrow \beta_1 \mid ... \mid \beta_k$ be the productions of N
 - Here $\beta_{\scriptscriptstyle I}$ is the entire right side of a production- a sequence of terminals and nonterminals
 - Pick the production $N \rightarrow \beta_i$ such that the lookahead is in First(β_i)
 - It must be that $First(\beta_i) \cap First(\beta_i) = \emptyset$ for $i \neq j$
 - If there is no such production, but $N \to \epsilon$ then return
 - · Otherwise, then fail with a parse error
- Suppose β_i = $\alpha_1 \alpha_2 ... \alpha_n$. Then call parse_ $\alpha_1()$; ...; parse_ α_n () to match the expected right-hand side, and return

Example

```
let parse_term t =
E \rightarrow id = n \mid \{L\}
                          if !lookahead = t
                             then lookahead := <next token>
L \rightarrow E; L \mid \epsilon
                             else raise <Parse error>
                 let rec parse E () =
                    if lookahead = 'id' then begin
                      parse_term 'id';
                      parse term '=';
                     parse_term 'n'
                    else if lookahead = '{' then begin
                     parse_term '{';
                      parse L ();
                     parse term '}';
(not quite
valid OCaml)
                    else raise <Parse error>;
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```

Example (cont'd)

```
E → id = n | {L}

L → E; L | E

mutually recursive with previous let rec

and parse L () =

if lookahead = 'id'|| lookahead = '{' then begin parse E ();

parse L ()

end

(* else return (not an error) *)
```

Things to Notice

- If you draw the execution trace of the parser as a tree, then you get the parse tree
- This parsing strategy may fail on certain grammars because the First sets overlap
 - This doesn't mean the grammar is not usable in a parser, just not in this type of parser
- Consider parsing the grammar E → n + E | n
 - First(E) = n = First(n), so we can't use this technique
 - Exercise: Rewrite this grammar so it becomes amenable to our parsing technique
- This is a *predictive* parser because we use the lookahead to determine exactly which production to use

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More on Limitations

- How about the grammar S → Sa | ε
 - First(Sa) = a, so we're ok as far as which production
 - But the body of parse_S() has an infinite loopif (lookahead = "a") then parse_S()
 - This technique cannot handle left-recursion
 - Exercise: rewrite this grammar to be right-recursive

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Expr Grammar for Top-Down Parsing

```
\begin{split} E \rightarrow T & E' \\ E' \rightarrow \epsilon \mid + E \\ T \rightarrow P & T' \\ T' \rightarrow \epsilon \mid * T \\ P \rightarrow n \mid (E) \end{split}
```

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 Notice we can always decide what production to choose with only one symbol of lookahead

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Tradeoffs with Other Approaches

- · Recursive descent parsers are easy to write
 - The formal definition is a little clunky, but if you follow the code then it's almost what you might have done if you weren't told about grammars formally
 - They're unable to handle certain kinds of grammars
- More powerful techniques need tool support, such as yacc and bison (which can be slower)
- · Recursive descent is good for a quick hack
 - Though using the tools is pretty fast if you're familiar with them

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General parsing algorithms

- As with NFA, we can also have a NDPDA
 - NDPDA are more powerful than DPDA
 - NDPDA can recognize even length palindromes over {0,1}*, but a DPDA cannot. Why? (Hint: Consider palindromes over {0,1}*2{0,1}*)
 - (Remember that DFA and NFA do accept the same sets.)
- Knuth in 1965 showed that the deterministic PDAs were equivalent to a class of grammars called LR(k) [Left-to-right parsing with k symbol lookahead]
 - Create a PDA that decides whether to stack the next symbol or pop a symbol off the stack by looking k symbols ahead.
 - symbol off the stack by looking k symbols ahead.

 This is a deterministic process, and for k=1 is efficient.
- LR(k), SLR(k) [Simple LR(k)], and LALR(k) [Lookahead LR(k)] are all techniques used today to build efficient parsers.
 - Recursive descent is a form of LL(k) parsing
 - More in CMSC 430 ...

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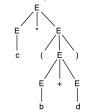
What's Wrong with Parse Trees?

- · Parse trees contain too much information
 - E.g., they have parentheses and they have extra nonterminals for precedence
 - This extra stuff is needed for parsing
- But when we want to reason about languages, it gets in the way (it's too much detail)

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Abstract Syntax Trees (ASTs) • An abstract syntax tree is a more compact,

 An abstract syntax tree is a more compact, abstract representation of a parse tree, with only the essential parts



parse

c + d

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ASTs (cont'd)

- Intuitively, ASTs correspond to the data structure you'd use to represent strings in the language
 - Note that grammars describe trees (so do OCaml datatypes which we'll see later)
 - $E \rightarrow a | b | c | E+E | E-E | E*E | (E)$



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The Compilation Process

source program target program

Lexing Parsing AST Code Generation

regexps CFGs (may not actually be constructed)

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Producing an AST

 To produce an AST, we modify the parse() functions to construct the AST along the way

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:

Producing an AST (cont'd)

```
type ast =
    Assn of string * int
    Block of ast list

let rec parse_E () =
    if lookahead = 'id' then
    let id = parse_term 'id' in
    let _ = parse_term '=' in
    let n = parse_term 'n' in
    Assn(id, int of string n)
    else if lookahead = '{' then begin
    let _ = parse_term '{' in
    let 1 = parse_L () in
    let _ = parse_term '}' in
    Block l
    end
    else raise <Parse error>;
```

Producing an AST (cont'd)

```
type ast =
Assn of string * int
Block of ast list

and parse_L () =
if lookahead = 'id' then
let = parse_E () in
let _ = parse_term ';' in
let l = parse_L () in
e::1
else []
```