

CMSC 330: Organization of Programming Languages

More on Scope
Operational Semantics

Tail Calls

- A *tail call* is a function call that is the last thing a function does before it returns

```
let add x y = x + y
let f z = add z z (* tail call *)
```

```
let rec length = function
  [] -> 0
  | (_::t) -> 1 + (length t) (* not a tail call *)
```

```
let rec length a = function
  [] -> a
  | (_::t) -> length (a + 1) t (* tail call *)
```

Tail Recursion

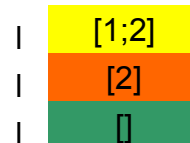
- Recall that in OCaml, all looping is via recursion
 - Seems very inefficient
 - Needs one stack frame for recursive call
- A function is *tail recursive* if it is recursive and the recursive call is a tail call

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Tail Recursion (cont'd)

```
let rec length l = match l with
  [] -> 0
  | (_::t) -> 1 + (length t)
length [1; 2]
```



eax: 2

- However, if the program is tail recursive...
 - Can instead reuse stack frame for each recursive call

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Tail Recursion (cont'd)

```
let rec length a l = match l with
  [] -> a
  | (_:t) -> (length (a + 1) t)
length 0 [1; 2]
```

a 2
| []

eax: 2

- The same stack frame is reused for the next call, since we'd just pop it off and return anyway

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Names and Binding

- Programs use *names* to refer to things
 - E.g., in `x = x + 1`, `x` refers to a variable
- A *binding* is an association between a name and what it refers to
 - `int x;` /* `x` is bound to a stack location containing an `int` */
 - `int f (int) { ... }` /* `f` is bound to a function */
 - `class C { ... }` /* `C` is bound to a class */
 - `let x = e1 in e2` (* `x` is bound to `e1` *)

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Name Restrictions

- Languages often have various restrictions on names to make lexing and parsing easier
 - Names cannot be the same as keywords in the language
 - OCaml function names must be lowercase
 - OCaml type constructor and module names must be uppercase
 - Names cannot include special characters like `;`, `:` etc
 - Usually names are upper- and lowercase letters, digits, and `_` (where the first character can't be a digit)
 - Some languages also allow more symbols like `!` or `-`

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Names and Scopes

- Good names are a precious commodity
 - They help document your code
 - They make it easy to remember what names correspond to what entities
- We want to be able to reuse names in different, non-overlapping regions of the code

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Names and Scopes (cont'd)

- A *scope* is the region of a program where a binding is active
 - The same name in a different scope can refer to a different binding (refer to a different program object)
- A name is *in scope* if it's bound to something within the particular scope we're referring to

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Example

```
void w(int i) {  
    ...  
}  
  
void x(float j) {  
    ...  
}  
  
void y(float i) {  
    ...  
}  
  
void z(void) {  
    int j;  
    char *i;  
    ...  
}
```

- **i** is in scope
 - in the body of **w**, the body of **y**, and after the declaration of **j** in **z**
 - but all those **i**'s are different
- **j** is in scope
 - in the body of **x** and **z**

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Ordering of Bindings

- Languages make various choices for when declarations of things are in scope

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Order of Bindings – OCaml

- `let x = e1 in e2` – `x` is bound to `e1` in scope of `e2`
- `let rec x = e1 in e2` – `x` is bound in `e1` and in `e2`

```
let x = 3 in
  let y = x + 3 in...    (* x is in scope here *)
```

```
let x = 3 + x in ...    (* error, x not in scope *)
```



```
let rec length = function
  [] -> 0
  | (h::t) -> 1 + (length t)  (* ok, length in scope *)
in ...
```

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Order of Bindings – C

- All declarations are in scope from the declaration onward

```
int i;  
int j = i; /* ok, i is in scope */  
i = 3;    /* also ok */
```

```
void f(...) { ... }  
  
int i;  
int j = j + 3; /* error */  
f(...);      /* ok, f declared */
```

```
f(...); /* may be error; need prototype (or oldstyle C) */  
void f(...) { ... }
```

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Order of Bindings – Java

- Declarations are in scope from the declaration onward, except for methods and fields, which are in scope throughout the class

```
class C {  
    void f(){  
        ...g()... // OK  
    }  
  
    void g(){  
        ...  
    }  
}
```

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Shadowing Names

- *Shadowing* is rebinding a name in an inner scope to have a different meaning
 - May or may not be allowed by the language

C

```
int i;

void f(float i) {
    {
        char *i = NULL;
        ...
    }
}
```

OCaml

```
let g = 3;;
let g x = x + 3;;
```

Java

```
void h(int i) {
    {
        float i; // not allowed
        ...
    }
}
```

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Namespaces

- Languages have a “top-level” or outermost scope
 - Many things go in this scope; hard to control collisions
- Common solution seems to be to add a hierarchy
 - OCaml: Modules
 - `List.hd`, `String.length`, etc.
 - `open` to add names into current scope
 - Java: Packages
 - `java.lang.String`, `java.awt.Point`, etc.
 - `import` to add names into current scope
 - C++: Namespaces
 - `namespace f { class g { ... } }, f::g b`, etc.
 - `using namespace` to add names to current scope

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Mangled Names

- What happens when these names need to be seen by other languages?
 - What if a C program wants to call a C++ method?
 - C doesn't know about C++'s naming conventions
- For multilingual communication, names are often mangled into some flat form
 - E.g., `class C { int f(int *x, int y) { ... } }` becomes symbol `__ZN1C3fEPii` in g++
 - E.g., native `valueOf(int)` in `java.lang.String` corresponds to the C function `Java_java_lang_String_valueOf__I`

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Static Scope Recall

- In *static scoping*, a name refers to its closest binding, going from inner to outer scope in the program text
 - Languages like C, C++, Java, Ruby, and OCaml are statically scoped

```
int i;  
{  
  int j;  
  {  
    float i;  
    j = (int) i;  
  }  
}
```

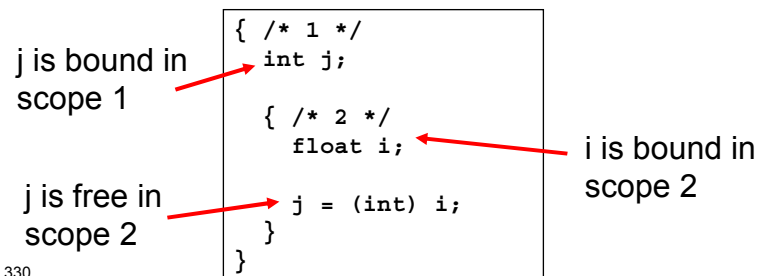
The diagram shows a code snippet with nested scopes. A red arrow points from the `float i;` declaration to the `j = (int) i;` assignment, indicating that the inner `i` is used. Another red arrow points from the outer `int i;` declaration to the `j = (int) i;` assignment, indicating that the outer `i` is used. The code is as follows:

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Free and Bound Variables

- The *bound variables* of a scope are those names that are declared in it
- If a variable is not bound in a scope, it is *free*
 - The bindings of variables which are free in a scope are "inherited" from declarations of those variables in outer scopes in static scoping

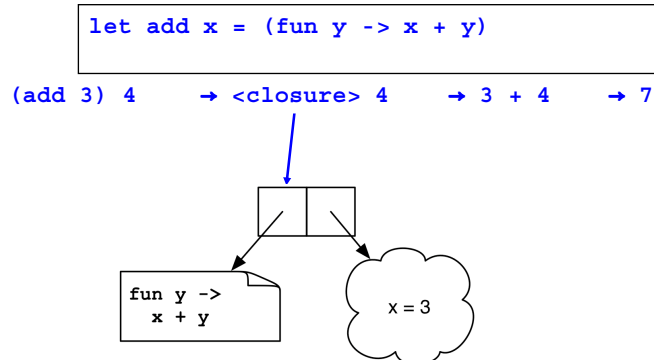


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Static Scoping and Nested Functions

- To allow arbitrary nested functions with higher-order functions and static scoping, we needed closures



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Nested Functions (cont'd)

- We need closures for *upward funargs*
 - Functions that are returned by other functions
- If we only have *downward funargs*, then we don't need full closures
 - These are functions that are only passed inward
 - So when they're called, any nonlocal variables they access from outer scopes are still around

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Example

```
let f x =  
  let g y = x + y in  
  g 3
```



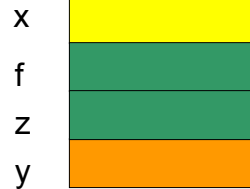
- When **g** is called, **x** is still on the stack

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Example

```
let app f z = f z
let f x =
  let g y = x + y in
  app g 3
```



- When `g` is called, `x` is still on the stack

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Downward Funargs

- It turns out that if we only pass functions downward, there are cheaper implementation strategies for static scoping than closures
- They're called *static links* and *displays*, and they're used by
 - Pascal and Algol-family languages
 - gcc nested functions
- We won't go into details, though (CMSC 430 covers these in exciting detail.)

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Dynamic Scope

- In a language with *dynamic scoping*, a name refers to its closest binding *at runtime*
 - LISP was the common example

Scheme (top-level scope only is dynamic)

```
(define f (lambda () a))  
; defines a no-argument function which returns a  
  
(define a 3)      ; bind a to 3  
(f)               ; calls f and returns 3  
(define a 4)  
(f)               ; calls f and returns 4
```

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Nested Dynamic Scopes

- Full dynamic scopes can be nested
 - Static scope relates to the program text
 - Dynamic scope relates to program execution trace

Perl (the keyword `local` introduces dynamic scope)

```
$1 = "global";  
  
sub A {  
    local $1 = "local";  
    B();  
}  
  
sub B { print "$1\n"; }  
  
B(); A(); B();
```

global
local
global

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Static vs. Dynamic Scope

Static scoping

- Local understanding of function behavior
- Know at compile-time what each name refers to
- A bit trickier to implement

Dynamic scoping

- Can be hard to understand behavior of functions
- Requires finding name bindings at runtime
- Easier to implement (just keep a global table of stacks of variable/value bindings)

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Operational Semantics

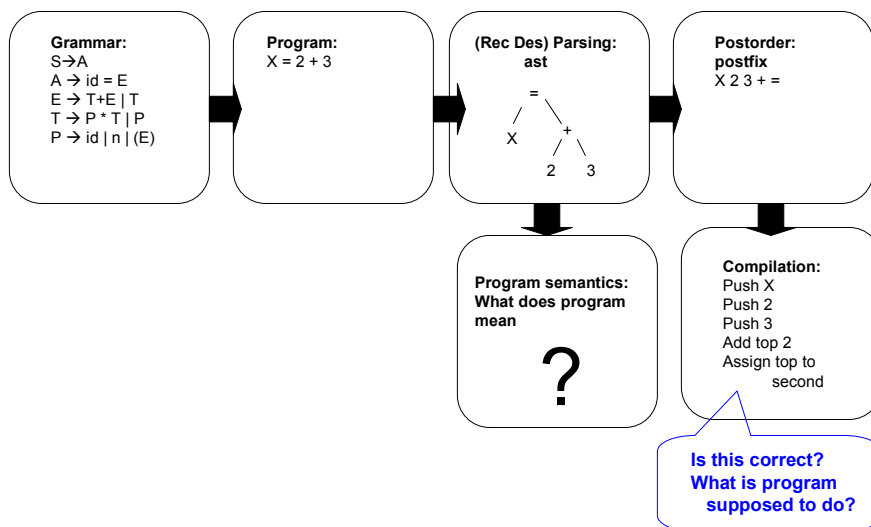
Introduction

- So far we've looked at regular expressions, automata, and context-free grammars
 - These are ways of defining sets of strings
 - We can use these to describe what programs you can write down in a language
 - (Almost...)
 - I.e., these describe the *syntax* of a language
- What about the *semantics* of a language?
 - What does a program “mean”?

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Roadmap: Compilation of program



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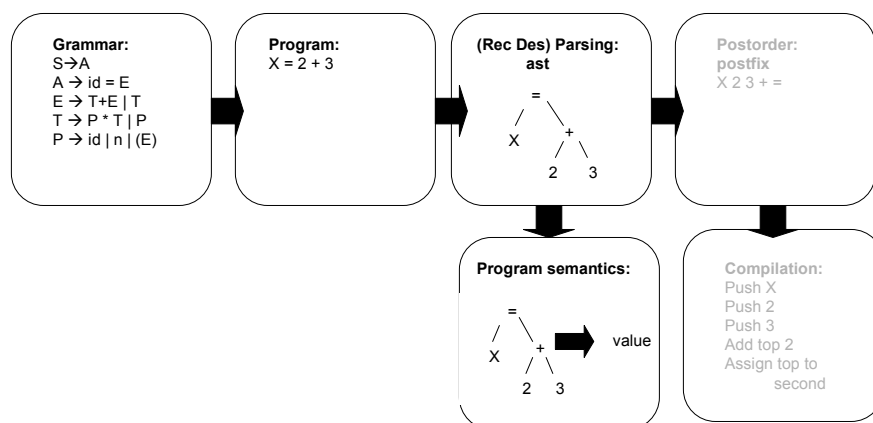
Operational Semantics

- There are several different kinds of semantics
 - *Denotational*: A program is a mathematical function
 - *Axiomatic*: Develop a logical proof of a program
 - Give predicates that hold when a program (or part) is executed
- We will briefly look at *operational semantics*
 - A program is defined by how you execute it on a mathematical model of a machine
- We will look at a subset of OCaml as an example

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Roadmap: Semantics of a program



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Evaluation

- We're going to define a relation $E \rightarrow v$
 - This means “expression E evaluates to v ”
- So we need a formal way of defining programs and of defining things they may evaluate to
- We'll use grammars to describe each of these
 - One to describe abstract syntax trees E
 - One to describe OCaml values v

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OCaml Programs

- $E ::= x \mid n \mid \text{true} \mid \text{false} \mid [] \mid \text{if } E \text{ then } E \text{ else } E$
 $\mid \text{fun } x = E \mid E E$
 - x stands for any identifier
 - n stands for any integer
 - true and false stand for the two boolean values
 - $[]$ is the empty list
 - Using $=$ in fun instead of \rightarrow to avoid some confusion later

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Values

- $v ::= n \mid \text{true} \mid \text{false} \mid [] \mid v::v$
 - n is an integer (*not* a string corresp. to an integer)
 - Same idea for *true*, *false*, *[]*
 - $v1::v2$ is the pair with $v1$ and $v2$
 - This will be used to build up lists
 - Notice: nothing yet requires $v2$ to be a list
 - **Important:** Be sure to understand the difference between *program text* S and *mathematical objects* v .
 - E.g., the text 3 evaluates to the mathematical number 3
 - To help, we'll use different colors and italics
 - This is usually not done, and it's up to the reader to remember which is which

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Grammars for Trees

- We're just using grammars to describe trees

$E ::= x \mid n \mid \text{true} \mid \text{false} \mid [] \mid \text{if } E \text{ then } E \text{ else } E$

$\mid \text{fun } x = E \mid E E$

$v ::= n \mid \text{true} \mid \text{false} \mid [] \mid v::v$

```
type ast =  
  Id of string  
  | Num of int  
  | Bool of bool  
  | Nil  
  | If of ast * ast * ast  
  | Fun of string * ast  
  | App of ast * ast
```

Given a program, we saw last time how to convert it to an ast (e.g., recursive descent parsing)

```
type value =  
  Val_Num of int  
  | Val_Bool of bool  
  | Val_Nil  
  | Val_Pair of value *  
    value
```

Goal: For any ast, we want an operational rule to obtain a value that represents the execution of ast

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Operational Semantics Rules

$n \rightarrow n$

$\text{true} \rightarrow \text{true}$

$\text{false} \rightarrow \text{false}$

$[] \rightarrow []$

- Each basic entity evaluates to the corresponding value

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Operational Semantics Rules (cont'd)

- How about built-in functions?

$(+) n m \rightarrow n + m$

- We're applying the $+$ function
 - (we put parens around it because it's not in infix notation; will skip this from now on)
 - Ignore currying for the moment, and pretend we have multi-argument functions
- On the right-hand side, we're computing the mathematical sum; the left-hand side is source code
- But what about $+(+ 3 4) 5$?
 - We need recursion

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Rules with Hypotheses

- To evaluate $+ E_1 E_2$, we need to evaluate E_1 , then evaluate E_2 , then add the results
 - This is call-by-value

$$\frac{E_1 \rightarrow n \quad E_2 \rightarrow m}{+ E_1 E_2 \rightarrow n + m}$$

- This is a “natural deduction” style rule
- It says that if the *hypotheses* above the line hold, then the *conclusion* below the line holds
 - i.e., if E_1 executes to value n and if E_2 executes to value m , then $+ E_1 E_2$ executes to value $n+m$

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Error Cases

$$\frac{E_1 \rightarrow n \quad E_2 \rightarrow m}{+ E_1 E_2 \rightarrow n + m}$$

- Because we wrote n, m in the hypothesis, we mean that they must be integers
- But what if E_1 and E_2 aren't integers?
 - E.g., what if we write $+ \text{false true}$?
 - It can be parsed, but we can't execute it
- We will have no rule that covers such a case
 - Convention: If there is not rule to cover a case, then the expression is erroneous
 - A program that evaluates to a stuck expression produces a run time error in practice

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Trees of Semantic Rules

- When we apply rules to an expression, we actually get a tree
 - Corresponds to the recursive evaluation procedure
 - For example: $+ (+ 3 4) 5$

$$\begin{array}{c}
 3 \rightarrow 3 \quad 4 \rightarrow 4 \\
 \hline
 (+ 3 4) \rightarrow 7 \quad 5 \rightarrow 5 \\
 \hline
 + (+ 3 4) 5 \rightarrow 12
 \end{array}$$

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Rules for If

$$\begin{array}{c}
 E_1 \rightarrow \text{true} \quad E_2 \rightarrow v \\
 \hline
 \text{if } E_1 \text{ then } E_2 \text{ else } E_3 \rightarrow v
 \end{array}$$

$$\begin{array}{c}
 E_1 \rightarrow \text{false} \quad E_3 \rightarrow v \\
 \hline
 \text{if } E_1 \text{ then } E_2 \text{ else } E_3 \rightarrow v
 \end{array}$$

- Examples
 - if false then 3 else 4 $\rightarrow 4$
 - if true then 3 else 4 $\rightarrow 3$
- Notice that only one branch is evaluated

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Rule for ::

$$\frac{E_1 \rightarrow v_1 \quad E_2 \rightarrow v_2}{:: E_1 E_2 \rightarrow v_1 :: v_2}$$

- So :: allocates a pair in memory
- Are there any conditions on E_1 and E_2 ?
 - No! We will allow E_2 to be anything
 - OCaml's type system will disallow non-lists

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Rules for Identifiers

$$x \rightarrow ???$$

- Let's assume for now that the only identifiers are parameter names
 - Ex. `(fun x = + x 3) 4`
 - When we see `x` in the body, we need to look it up
 - So we need to keep some sort of *environment*
 - This will be a map from identifiers to values

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Semantics with Environments

- Extend rules to the form $A; E \rightarrow v$
 - Means in environment A , the program text E evaluates to v
- Notation:
 - We write \bullet for the empty environment
 - We write $A(x)$ for the value that x maps to in A
 - We write $A, x:v$ for the same environment as A , except x is now v
 - x might or might not have mapped to anything in A
 - We write A, A' for the environment with the bindings of A' added to and overriding the bindings of A
 - The empty environment can be omitted when things are clear, and in adding other bindings to an empty environment we can write just those bindings if things are clear

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Rules for Identifiers and Application

$$A; x \rightarrow A(x)$$

no hypothesis means
"in all cases"

$$A; E_2 \rightarrow v \quad A, x:v; E_1 \rightarrow v'$$

$$A; (\text{fun } x = E_1) E_2 \rightarrow v'$$

- To evaluate a user-defined function applied to an argument:
 - Evaluate the argument (call-by-value)
 - Evaluate the function body in an environment in which the formal parameter is bound to the actual argument
 - Return the result

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Example: (fun x = + x 3) 4 = ?

$$\frac{\begin{array}{c} \bullet, x:4; x \rightarrow 4 \quad \bullet, x:4; 3 \rightarrow 3 \\ \hline \bullet, x:4; + x 3 \rightarrow 7 \end{array}}{\bullet; (\text{fun } x = + x 3) 4 \rightarrow 7}$$

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Nested Functions

- This works for cases of nested functions
 - ...as long as they are fully applied
- But what about the true higher-order cases?
 - Passing functions as arguments, and returning functions as results
 - We need closures to handle this case
 - ...and a closure was just a function and an environment
 - We already have notation around for writing both parts

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Closures

- Formally, we add closures $(A, \lambda x.E)$ to values
 - A is the environment in which the closure was created
 - x is the parameter name
 - E is the source code for the body
- λx will be discussed next time. Means a binding of x in E .
- $v ::= n \mid \text{true} \mid \text{false} \mid [] \mid v::v \mid (A, \lambda x.E)$

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Revised Rule for Lambda

$$\frac{}{A; \text{fun } x = E \rightarrow (A, \lambda x.E)}$$

- To evaluate a function definition, create a closure when the function is created
 - Notice that we don't look inside the function body

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Revised Rule for Application

$$\frac{A; E_1 \rightarrow (A', \lambda x. E) \quad A; E_2 \rightarrow v}{A, A', x:v; E \rightarrow v'} \quad A; (E_1 E_2) \rightarrow v'$$

- To apply something to an argument:
 - Evaluate it to produce a closure
 - Evaluate the argument (call-by-value)
 - Evaluate the body of the closure, in
 - The current environment, extended with the closure's environment, extended with the binding for the parameter

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Example

$$\begin{aligned} & \bullet; (\text{fun } x = (\text{fun } y = + x y)) \rightarrow (\bullet, \lambda x. (\text{fun } y = + x y)) \\ & \bullet; 3 \rightarrow 3 \\ & \frac{x:3; (\text{fun } y = + x y) \rightarrow (x:3, \lambda y. (+ x y))}{\bullet; (\text{fun } x = (\text{fun } y = + x y)) \ 3 \rightarrow (x:3, \lambda y. (+ x y))} \end{aligned}$$

Let <previous> = (fun x = (fun y = + x y)) 3

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Example (cont'd)

•; <previous> → (x:3, $\lambda y. (+ x y)$)

•; 4 → 4

x:3, y:4; (+ x y) → 7

•; (<previous> 4) → 7

Why Did We Do This? (cont'd)

- Operational semantics are useful for
 - Describing languages
 - Not just OCaml! It's pretty hard to describe a big language like C or Java, but we can at least describe the core components of the language
 - Giving a *precise* specification of how they work
 - Look in any language standard – they tend to be vague in many places and leave things undefined
 - Reasoning about programs
 - We can actually prove that programs do something or don't do something, because we have a precise definition of how they work