

# Functional Programming in *Mathematica*

## A (very) brief tutorial...

### Preliminaries

Functional programming is a programming paradigm that treats computation as the evaluation of mathematical functions and avoids state and mutable data. It emphasizes the application of functions, in contrast with the imperative programming style that emphasizes changes in state.

---

### General philosophy: Everything is a function

```
Clear[y];  
y = Sqrt[4]
```

```
2
```

```
Clear[z];  
z = Sqrt[x]
```

```
 $\sqrt{x}$ 
```

```
z
```

```
 $\sqrt{x}$ 
```

```
Clear[z];
```

```
z
```

```
z
```

```
??Sqrt
```

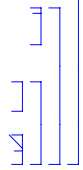
```
Sqrt[z] gives the square root of z. More...
```

```
Attributes[Sqrt] = {Listable, NumericFunction, Protected}
```

## ■ Function Composition

```
Sqrt[Sqrt[16]]
```

```
2
```



## User-Defined Functions

### ■ Pure Functions

```
Function[z, z2]
```

```
Function[z, z2]
```

```
??Function
```

Function[body] or body& is a pure function. The formal parameters are # (or #1), #2, etc. Function[x, body] is a pure function with a single formal parameter x. Function[{x1, x2, ... }, body] is a pure function with a list of formal parameters. **More...**

```
Attributes[Function] = {HoldAll, Protected}
```

```
Function[z, z2][5]
```

```
25
```

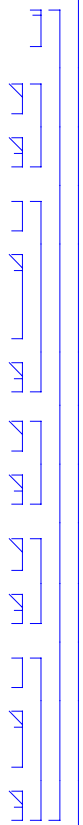
```
(#12 &)[5]
```

```
25
```

```
??#
```

# represents the first argument supplied to a pure function. #n represents the nth argument. **More...**

```
Attributes[Slot] = {NHoldAll, Protected}
```

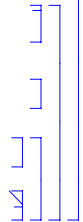


### ■ Defining Complex Functions

```
compFunc[x_] := Sqrt[Sqrt[x]]
```

```
compFunc[16]
```

```
2
```



## Lists

```
x = {4,1,7,1}
```

```
{4, 1, 7, 1}
```

```
y = List[1, 4, 2, 4, 2]
```

```
{1, 4, 2, 4, 2}
```

```
Sort[x]
```

```
{1, 1, 4, 7}
```

```
Sort[y]
```

```
{1, 2, 2, 4, 4}
```

```
??Sort
```

Sort[list] sorts the elements of list into canonical order. Sort[list, p] sorts using the ordering function p. [More...](#)

```
Attributes[Sort] = {Protected}
```

```
Sqrt[{1,2,3,4,5,6}]
```

```
{1,  $\sqrt{2}$ ,  $\sqrt{3}$ , 2,  $\sqrt{5}$ ,  $\sqrt{6}$ }
```

```
??Join
```

Join[list1, list2, ... ] concatenates lists together. Join can be used on any set of expressions that have the same head. [More...](#)

```
Attributes[Join] = {Flat, OneIdentity, Protected}
```

```
Join[x, y]
```

```
{4, 1, 7, 1, 1, 4, 2, 4, 2}
```

```
z = {x, y}
```

```
{{4, 1, 7, 1}, {1, 4, 2, 4, 2}}
```

```
z // TableForm
```

```
4      1      7      1
1      4      2      4      2
```

```
z // MatrixForm
```

```
( {4, 1, 7, 1}
  {1, 4, 2, 4, 2} )
```

```
Function[z, z2][{1, 2, 3}]
{1, 4, 9}

compFunc[{16, 25}]
{2,  $\sqrt{5}$ }
```



## Lets try to do Assignment 3

```
SetDirectory["c:\\data"]
c:\data

Application = "Word"
Word

depthArray = << ("FaultDepths_Terp" <> Application <> ".txt")
{1, 1, 3, 2, 1, 4, 1, 2, 2, 3, 2, 2, 1, 1, 2, 3, 1, 2, 1, 2, 4, 3, 2, 1, 2, 5, 2, 1, 4, 1, 2,
5, 2, 2, 4, 1, 3, 1, 1, 2, 1, 1, 2, 3, 3, 2, 2, 3, 1, 1, 5, 3, 1, 5, 1, 4, 2, 5, 3, 1,
2, 2, 1, 1, 3, 3, 1, 3, 4, 4, 1, 3, 4, 2, 2, 3, 2, 5, 1, 2, 2, 3, 2, 2, 1, 1, 3, 1,
3, 2, 3, 1, 1, 3, 1, 1, 1, 4, 3, 1, 3, 1, 2, 2, 3, 1, 1, 4, 5, 2, 2, 2, 2, 2, 1, 2,
4, 5, 2, 1, 1, 1, 4, 1, 5, 4, 2, 3, 4, 4, 1, 1, 3, 3, 3, 2, 1, 2, 2, 4, 3, 1, 1, 1,
2, 1, 2, 5, 1, 3, 3, 1, 1, 3, 3, 1, 2, 1, 2, 2, 3, 2, 1, 3, 2, 5, 1, 4, 5, 1, 2, 3,
2, 4, 1, 2, 2, 1, 4, 4, 1, 2, 1, 2, 1, 5, 3, 5, 1, 2, 4, 3, 1, 2, 4, 1, 3, 2, 1, 2}
```

```
depths = Union[depthArray]
{1, 2, 3, 4, 5}

totalPerDepth = Map[Length[Cases[depthArray, #]] &, depths]
{67, 59, 38, 22, 14}

Apply[Plus, totalPerDepth]
200

<<Graphics`Graphics`
gr = BarChart[N[totalPerDepth], Frame -> True, ImageSize -> {200, Automatic}]
- Graphics -
```

| Depth | Count |
|-------|-------|
| 1     | 67    |
| 2     | 59    |
| 3     | 38    |
| 4     | 22    |
| 5     | 14    |













```
Map[Apply[Plus, #]&, Transpose[smokeMatrix]]
```

```
{1, 2, 0, 1, 1, 0, 1, 1, 1, 1, 2, 0, 1, 2, 2, 0, 2, 1, 1, 1, 2, 2, 2, 1, 2, 2, 1, 2, 0, 1,
 1, 0, 1, 0, 0, 2, 1, 1, 2, 2, 2, 1, 1, 2, 1, 1, 1, 1, 1, 2, 1, 0, 1, 2, 1, 1, 1, 2, 1,
 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 0, 1, 1, 1, 1, 1, 0, 1, 2, 1, 1, 3, 1, 1, 1, 1, 2,
 2, 2, 0, 2, 1, 1, 2, 1, 1, 1, 1, 2, 3, 1, 2, 0, 0, 1, 0, 2, 0, 1, 1, 2, 1, 0, 2, 2,
 0, 0, 1, 1, 1, 1, 1, 1, 2, 0, 1, 1, 0, 1, 1, 1, 1, 0, 1, 1, 1, 1, 1, 0, 2, 1, 1, 1,
 2, 2, 1, 1, 2, 1, 1, 1, 1, 2, 2, 1, 0, 1, 2, 2, 1, 2, 1, 3, 1, 0, 2, 0, 0, 2, 2, 1,
 2, 1, 0, 2, 1, 1, 0, 1, 1, 3, 1, 1, 0, 1, 1, 1, 1, 2, 1, 1, 1, 1, 1, 2, 2, 0, 1}
```

```
??Position
```

Position[expr, pattern] gives a list of the positions at which objects matching pattern appear in expr. Position[expr, pattern, levspec] finds only objects that appear on levels specified by levspec. Position[expr, pattern, levspec, n] gives the positions of the first n objects found. **More...**

```
Attributes[Position] = {Protected}
```

```
Options[Position] = {Heads -> True}
```

```
zeros = Position[Map[Apply[Plus, #]&, Transpose[smokeMatrix]], 0]
```

```
{{3}, {6}, {12}, {16}, {29}, {32}, {34}, {35}, {52}, {72}, {78},
 {91}, {104}, {105}, {107}, {109}, {114}, {117}, {118}, {126}, {129},
 {134}, {140}, {157}, {166}, {168}, {169}, {175}, {179}, {185}, {199}}
```

```
Range[Length[Transpose[smokeMatrix]]]
```

```
{1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21,
 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 37, 38, 39, 40,
 41, 42, 43, 44, 45, 46, 47, 48, 49, 50, 51, 52, 53, 54, 55, 56, 57, 58, 59,
 60, 61, 62, 63, 64, 65, 66, 67, 68, 69, 70, 71, 72, 73, 74, 75, 76, 77, 78,
 79, 80, 81, 82, 83, 84, 85, 86, 87, 88, 89, 90, 91, 92, 93, 94, 95, 96, 97,
 98, 99, 100, 101, 102, 103, 104, 105, 106, 107, 108, 109, 110, 111, 112,
 113, 114, 115, 116, 117, 118, 119, 120, 121, 122, 123, 124, 125, 126,
 127, 128, 129, 130, 131, 132, 133, 134, 135, 136, 137, 138, 139, 140,
 141, 142, 143, 144, 145, 146, 147, 148, 149, 150, 151, 152, 153, 154, 155,
 156, 157, 158, 159, 160, 161, 162, 163, 164, 165, 166, 167, 168, 169, 170,
 171, 172, 173, 174, 175, 176, 177, 178, 179, 180, 181, 182, 183, 184, 185,
 186, 187, 188, 189, 190, 191, 192, 193, 194, 195, 196, 197, 198, 199, 200}
```

```
??Delete
```

Delete[expr, n] deletes the element at position n in expr. If n is negative, the position is counted from the end. Delete[expr, {i, j, ...}] deletes the part at position {i, j, ...}. Delete[expr, {{i1, j1, ...}, {i2, j2, ...}, ...}] deletes parts at several positions. **More...**

```
Attributes[Delete] = {Protected}
```

```
smokeFaultsFound = Delete[Range[Length[Transpose[smokeMatrix]]], zeros]
```

```
{1, 2, 4, 5, 7, 8, 9, 10, 11, 13, 14, 15, 17, 18, 19, 20, 21, 22, 23, 24,
 25, 26, 27, 28, 30, 31, 33, 36, 37, 38, 39, 40, 41, 42, 43, 44, 45, 46, 47,
 48, 49, 50, 51, 53, 54, 55, 56, 57, 58, 59, 60, 61, 62, 63, 64, 65, 66, 67,
 68, 69, 70, 71, 73, 74, 75, 76, 77, 79, 80, 81, 82, 83, 84, 85, 86, 87, 88,
 89, 90, 92, 93, 94, 95, 96, 97, 98, 99, 100, 101, 102, 103, 106, 108, 110,
 111, 112, 113, 115, 116, 119, 120, 121, 122, 123, 124, 125, 127, 128, 130,
 131, 132, 133, 135, 136, 137, 138, 139, 141, 142, 143, 144, 145, 146, 147,
 148, 149, 150, 151, 152, 153, 154, 155, 156, 158, 159, 160, 161, 162, 163,
 164, 165, 167, 170, 171, 172, 173, 174, 176, 177, 178, 180, 181, 182, 183,
 184, 186, 187, 188, 189, 190, 191, 192, 193, 194, 195, 196, 197, 198, 200}
```

```
Length[Delete[Range[Length[Transpose[smokeMatrix]]], zeros]]
```

```
169
```

```
smokeDepths = Map[{1, #} &, depthArray[[smokeFaultsFound]]]
```

```
{{{1, 1}, {1, 1}, {1, 2}, {1, 1}, {1, 1}, {1, 2}, {1, 2}, {1, 3}, {1, 2}, {1, 1},
  {1, 1}, {1, 2}, {1, 1}, {1, 2}, {1, 1}, {1, 2}, {1, 4}, {1, 3}, {1, 2}, {1, 1},
  {1, 2}, {1, 5}, {1, 2}, {1, 1}, {1, 1}, {1, 2}, {1, 2}, {1, 1}, {1, 3}, {1, 1},
  {1, 1}, {1, 2}, {1, 1}, {1, 1}, {1, 2}, {1, 3}, {1, 3}, {1, 2}, {1, 2}, {1, 3},
  {1, 1}, {1, 1}, {1, 5}, {1, 1}, {1, 5}, {1, 1}, {1, 4}, {1, 2}, {1, 5}, {1, 3},
  {1, 1}, {1, 2}, {1, 2}, {1, 1}, {1, 1}, {1, 3}, {1, 3}, {1, 1}, {1, 3}, {1, 4},
  {1, 4}, {1, 1}, {1, 4}, {1, 2}, {1, 2}, {1, 3}, {1, 2}, {1, 1}, {1, 2}, {1, 2},
  {1, 3}, {1, 2}, {1, 2}, {1, 1}, {1, 1}, {1, 3}, {1, 1}, {1, 3}, {1, 2}, {1, 1},
  {1, 1}, {1, 3}, {1, 1}, {1, 1}, {1, 1}, {1, 4}, {1, 3}, {1, 1}, {1, 3}, {1, 1},
  {1, 2}, {1, 1}, {1, 4}, {1, 2}, {1, 2}, {1, 2}, {1, 2}, {1, 1}, {1, 2}, {1, 2},
  {1, 1}, {1, 1}, {1, 1}, {1, 4}, {1, 1}, {1, 5}, {1, 2}, {1, 3}, {1, 4}, {1, 1},
  {1, 1}, {1, 3}, {1, 3}, {1, 2}, {1, 1}, {1, 2}, {1, 2}, {1, 3}, {1, 1}, {1, 1},
  {1, 1}, {1, 2}, {1, 1}, {1, 2}, {1, 5}, {1, 1}, {1, 3}, {1, 3}, {1, 1}, {1, 1},
  {1, 3}, {1, 3}, {1, 1}, {1, 1}, {1, 2}, {1, 2}, {1, 3}, {1, 2}, {1, 1}, {1, 3},
  {1, 2}, {1, 1}, {1, 1}, {1, 2}, {1, 3}, {1, 2}, {1, 4}, {1, 2}, {1, 2}, {1, 1},
  {1, 4}, {1, 1}, {1, 2}, {1, 1}, {1, 2}, {1, 5}, {1, 3}, {1, 5}, {1, 1}, {1, 2},
  {1, 4}, {1, 3}, {1, 1}, {1, 2}, {1, 4}, {1, 1}, {1, 3}, {1, 2}, {1, 2}}
```

```
depths
```

```
{1, 2, 3, 4, 5}
```

```
smokePerDepth = Map[Length[Cases[depthArray[[smokeFaultsFound]], #]] &, depths]
```

```
{63, 54, 31, 13, 8}
```

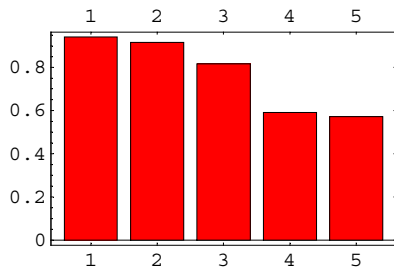
```
Apply[Plus, smokePerDepth]
```

```
169
```

```
N[smokePerDepth / totalPerDepth]
```

```
{0.940299, 0.915254, 0.815789, 0.590909, 0.571429}
```

```
gr = BarChart[N[smokePerDepth / totalPerDepth],
  Frame → True, ImageSize → {200, Automatic}];
```




---

## Comp Tests

---

## Putting it all Together

### ■ Initialization

```
<<Graphics`Graphics`
SetDirectory["c:\\data"]
c:\data
```

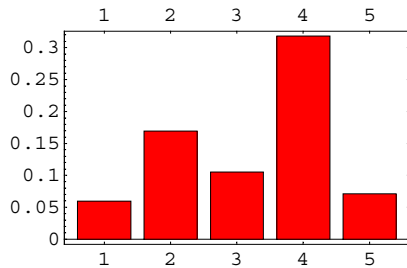
### ■ Parameters

```
type="Comp"
Comp
Application="Word"
Word
```

### ■ Computation

```
depthArray = << ("FaultDepths_Terp" <> Application <> ".txt");
depths = Union[depthArray];
totalPerDepth = Map[Length[Cases[depthArray, #]] &, depths];
matrix = << (type <> "_Terp" <> Application <> ".txt");
zeros = Position[Map[Apply[Plus, #] &, Transpose[matrix]], 0];
faultsFound = Delete[Range[Length[Transpose[matrix]]], zeros];
```

```
foundDepths = Map[{1, #} &, depthArray[[faultsFound]]];  
faultsPerDepth = Map[Length[Cases[depthArray[[faultsFound]], #]] &, depths];  
gr = BarChart[N[faultsPerDepth/totalPerDepth],  
Frame → True, ImageSize → {200, Automatic}]
```



- Graphics -

---

## Putting it in One Function

### ■ Initialization

```
<<Graphics`Graphics`  
SetDirectory["c:\\data"]  
c:\data
```

### ■ Parameters

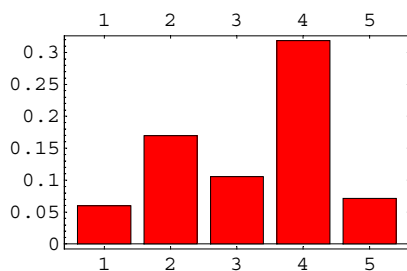
```
type="Comp"  
Comp  
Application="Word"  
Word
```

## ■ Computation

```
Clear[plotHistogram];
plotHistogram[type_, Application_] :=
Module[{},
  depthArray = Get[("FaultDepths_Terp"<>Application<>".txt")];
  depths=Union[depthArray];
  totalPerDepth= Map[Length[Cases[depthArray, #]]&, depths];
  matrix = Get[(type <> "_Terp"<>Application<>".txt")];
  zeros = Position[Map[Apply[Plus, #]&, Transpose[matrix]], 0];
  faultsFound = Delete[Range[Length[Transpose[matrix]], zeros];
  foundDepths=Map[{1, #}&, depthArray[[faultsFound]];
  faultsPerDepth=Map[Length[Cases[depthArray[[faultsFound]], #]]&, depths];
  BarChart[N[faultsPerDepth/totalPerDepth], Frame->True,
    ImageSize->{200, Automatic}]

```

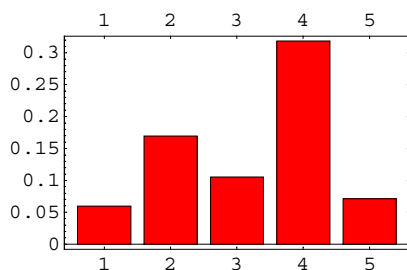
```
plotHistogram["Comp", "Word"]
```

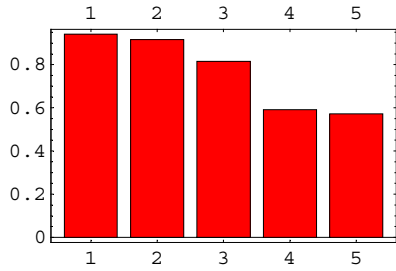


- Graphics -

## Invoking the Function

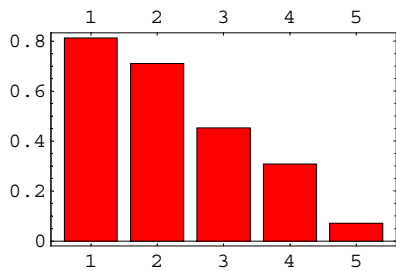
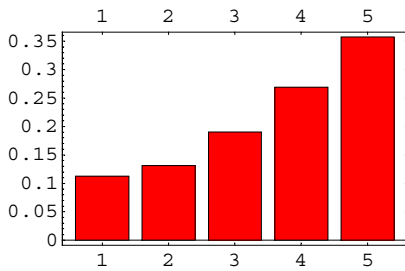
```
Map[plotHistogram#[[1]], #[[2]]&, {"Comp", "Word"}, {"Smoke", "Word"}]
```





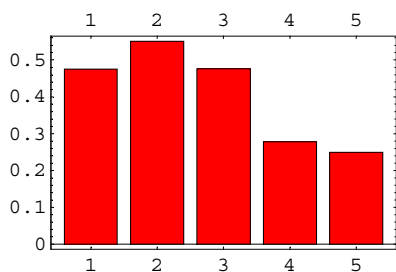
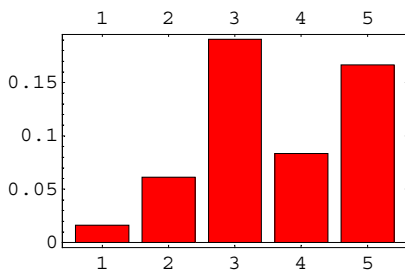
{- Graphics -, - Graphics -}

```
Map[plotHistogram#[[1]], #[[2]]]&, {"Comp","Paint"}, {"Smoke", "Paint"}]
```



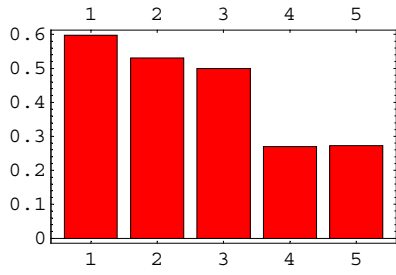
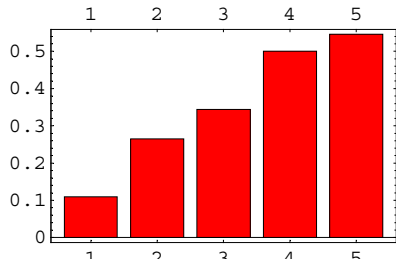
{- Graphics -, - Graphics -}

```
Map[plotHistogram#[[1]], #[[2]]]&, {"Comp","Present"}, {"Smoke", "Present"}]
```



{- Graphics -, - Graphics -}

```
Map[plotHistogram[#[[1]], #[[2]]&, {"Comp", "SpreadSheet"}, {"Smoke", "SpreadSheet"}]]
```



{ - Graphics -, - Graphics - }

