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# Structural Coverage of Functional Testing

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#### Abstract

A large, commercially developed FORTRAN program was modified to produce structural coverage metrics. The modified program was executed on a set of functionally generated acceptance tests and a large sample of operational usage cases. The resulting structural coverage metrics are combined with fault and error data to evaluate structural coverage in the SEL environment.

We can show that in this environment the functionally generated tests seem to be a good approximation of operational use. The relative proportions of the exercised statement subclasses (executable, assignment, CALL, DO, IF, READ, WRITE) changes as the structural coverage of the program increases. We propose a method for evaluating if two sets of input data exercise a program in a similar manner.

We also provide evidence that implies that in this environment, faults revealed in a procedure are independent of the number of times the procedure is executed and that it may be reasonable to use procedure coverage in software models that use statement coverage. Finally, the evidence suggests that it may be possible to use structural coverage to aid the management of the acceptance test process.

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# 1. Introduction

The goal of this study has been to understand and improve the acceptance test process in the NASA Goddard Space Flight Center SEL environment [SEL82a]. Towards this end, an SEL program has been modified to produce structural coverage metrics. The instrumented program, the MAL language preprocessor, is a subset of the RADMAS satellite attitude maintenance system [STL82]. It has 68 functions and subroutines, 10k source lines of code and 4k executable statements. The program was modified to measure both procedure coverage and statement coverage. Coverage is also computed for the statement subclasses: assignment statements, CALL, DO, IF, READ, and WRITE.

The modified program was executed on a set of ten functionally generated acceptance tests and on sixty typical operational usage cases [CSC78]. Error, fault and failure data<sup>#</sup> were collected from the system test through operation phases [SEL82b]. Each execution of an acceptance test or an operational usage case provides a structural coverage statistic. These structural coverage statistics are first examined individually to understand the static properties of the acceptance test process. Randomly generated sequences of acceptance tests and operational usage cases are then examined in an attempt to understand the dynamic properties of structural growth. Finally the coverage data are combined with the error, fault and failure data to understand how faults are revealed.

<sup>\*</sup> We have tried to follow the IEEE Standard Glossary of Software Engineering Terminology definitions of error, fault and failure: An error is the "human action that results in software containing a fault." A fault is "a manifestation of an error." A failure is "a departure of program operation from program requirements" [IEEE83]. Some of the sources we cite were written before the standard; their use of error may differ from the standard.

# 2. Goals of the Study

The first goal of this study was to characterize structural coverage in the SEL environment. The first questions address the simple, static properties of structural coverage for the different kinds of inputs. Question I.D compares two kinds of structural coverage: procedure and statement coverage. It would be a useful result if we could show that procedure coverage can be substituted for statement coverage in software models since procedure coverage is easier to measure than statement coverage. The final question addresses the dynamic properties of structural coverage: the structural coverage growth of a set of input cases.

Some testing strategies ([Duran80] and [Dyer82]) and software reliability models [Brooks80] require a method for showing that two sets of inputs exercise a program in a similar fashion. This motivated goal II: "Can different input sets be differentiated using structural coverage metrics?" Questions II.A-II.D explore several methods of doing this.

The purpose of the functional tests is to reveal faults in the program yet some faults are still revealed in operation. What classes of faults does functional testing miss? Does operational use exercise the code differently than the functional tests? How is this related to structural coverage? This motivated the next goal: "How are faults and structural coverage related?" Questions III.A - III.D analyze the SEL error, fault, and failure data with respect to structural coverage [SEL82b].

Finally in Section IV these ideas are combined to suggest an improved method of managing acceptance tests.

I. Characterize structural coverage in the SEL environment.

- I.A. What is the statement coverage of functional testing? What is the procedure coverage of functional testing?
- I.B. What is the statement coverage of operational use? What is the procedure coverage of operational use?
- I.C. What are the intersection / union of functional testing and operational use?
- I.D. Can procedure coverage be substituted for statement coverage in software models?

I.E. What are the properties of structural coverage growth?

II. Differentiate different input sets using their structural coverage.

**II.A.** Are heavily exercised procedures more likely to contain a fault?

II.B. Using Venn diagram?

- II.C. Using nonparametric statistics?
- II.D. Using number of executions of prime sections of code?

III. Relate errors, faults, failures and structural coverage.

**III.A.** Are more heavily exercised procedures more likely to contain a revealed fault?

III.B. Are faults related to time to isolate?

III.C. Are faults related to time to understand and implement?

III.D. Are faults related to type of error?

- IV. Use structural coverage to aid the management of acceptance tests.
  - IV.A. Can structural coverage be used to suggest new acceptance tests?

IV.B. Can structural coverage be used to improve reliability models?

Figure 1.

# 3. Data and Analysis

This section contains a description of the data and their analysis paralleling the outline in figure 1.

# 3.1. Structural Coverage in the SEL

Question:

What is the statement coverage of functional testing? What is the procedure coverage of functional testing?

The acceptance tests we used are functional or "black box" tests [Howden81], [Myers79]. Since exhaustive sampling of the input subdomains is impractical, a few sample inputs from a few subdomains are chosen that the testers feel are likely to reveal faults [CSC78]. There are 17 acceptance tests.

Table 1 shows the structural coverage of the acceptance tests. Test 1 exercised 33 out of 68 possible procedures. It exercised 1069 of the 4300 executable statements. In total the 17 tests exercised 51 procedures and 2408 executable statements (Union). There were 778 executable statements that were exercised by every test case (Intersection). These numbers are interpretated as percentages of the maximum in table 2.

Please note that we did not measure the structural coverage of either system or unit tests. Statements which were not exercised during acceptance test might have been exercised during previous testing. Structural coverage measures were not available during either system or unit test. Procedures were not tested with the goal of achieving high

# structural coverage.

#### Question:

What is the statement coverage of operational use? What is the procedure coverage of operational use?

We obtained 60 input cases that we claim are representative of SEL operational usage. These are 60 samples of actual operational usage cases. This is significantly different from other definitions of operational usage where typically the input domain is divided into subdomains, with each subdomain being assigned a probability of execution. Input cases are then chosen using the probabilities of execution [Brown75], [Duran78], and [Dyer82]. Our definition of operational usage lacks both the definition of subdomains and the assignment of probabilities. These probabilities are difficult to compute and verify. Rigorously derived or otherwise, these operational usage cases define how the program was exercised.

The statement and procedure coverage of operational usage is displayed in tables 3-4.

#### Question:

What are the intersection / union of functional testing and operational use?

Table 5 compares the structural coverage of functionally generated acceptance tests and operational usage. Together they exercised 55 procedures and and 2768 executable statements. Their intersection (the statements exercised by both sets of inputs) contains 51 procedures and 2397 executable statements. There are 360 executable statements that

are exercised by operational usage but not by acceptance test; 11 statements that are exercised by acceptance test but not by operational usage. Table 6 shows the raw numbers interpreted as percentages.

Some interesting observations can be made. The I/O statements, especially the WRITE statements, are less likely to be executed than most other statement subclasses. This is reasonable considering the role WRITE statements play in debugging and error condition handling code. Also, as statement coverage increases, different statements subclasses are more likely to be exercised. In table 6 the line labeled "OpU-A" describes the statements that are executed in operational use but not in acceptance test. Operational usage exercised 8.4% of the code that acceptance test never exercised. This 8.4% is not an even cross section of the statement subclasses. One would reasonably expect the 8.4% to be similar for different statement subclasses but this is not so. 12.1% of the IF statements are executed; half again as much as might be expected.

While this is an interesting result in its own right, this also has some significance to software reliability models. Assuming that statements from different statement subclasses have different likelyhoods of being a "fault," then this result seems to imply that a representative reliability model should have a hazard function (see [Myers79]) that varies over time.

# Question:

Can procedure coverage be substituted for statement coverage in software models?

Statement coverage is easy to measure but it is costly in terms of execution time; procedure coverage is much cheaper to measure. Showing that procedure coverage could be substituted for statement coverage in software models would be a useful result. We have not tried to substitute procedure coverage for statement coverage in software models to demonstrate our hypothesis, but rather we have discovered a result that seems to support this possibility.

Each execution of the instrumented program produced both a procedure coverage statistic and seven statement coverage statistics (the number of assignment statements, executable statements, CALLs, DOs, IFs, READs, and WRITES exercised). Plots 1-14 show procedure coverage versus the different kinds of statement coverage for both operational usage and acceptance test. The plots seem to be linear. This is unremarkable; the more procedures that are exercised, the more statements are exercised. What is interesting is the tightness of the linear fit. In the limited range we examined, the values are never more than  $\pm 200$  statements from the estimate for acceptance test and  $\pm 300$  statements for the operational usage cases.

# Question:

What are the properties of structural coverage growth?

For a set of input cases, structural coverage monotonically increases with the execution of each new input case (bound above by the number of reachable statements). This section examines the growth of structural coverage. It is important for two reasons:

(1) It provides a way to see if two sets of input cases exercise the program the same way. This provides a way to compare the

equivalence of operational use and acceptance testing.

(2) It provides useful data for the reliability models. Assuming that increased coverage implies a higher failure rate, then anything we learn about the growth of structural coverage can be applied to the calculation of the reliability models' hazard functions.

With 17 acceptance tests and 60 operational usage cases, there are clearly too many sequences to exhaustively examine. In a personal communication, Amrit Goel proposed a solution: examine the structural coverage of a large, but manageable number of sequences. Plots 15-16 show the structural coverage growth of 100 permutations of both acceptance tests and operational usage, with median and quartiles superimposed. Note that the acceptance test plots must all end at the point (17, 2408).

A variety of models were fitted to the structural coverage growth data in an attempt to learn more about structural coverage growth. A good mathematical model of structural coverage growth would provide insight into structural growth. Models were fitted to the first half of a sequence to evaluate their usefulness as predictors and to the entire sequence to evaluate their ability to characterize structural coverage growth. Plots of the residuals were examined visually to estimate goodness of fit.

The best fit was obtained using Goel and Okumoto's NHPP model [Goel80b]. The NHPP model was originally defined as a reliability model. Given a history of faults revealed over time, it predicts the number of faults revealed by time t. It is being used here as a model of structural coverage growth. Restated in terms of structural coverage

growth, the model is:

$$m(t) = a(1-e^{-bt})$$

where m(t) is the number of statements executed after test t. a predicts the maximum number of statements to be executed. b defines the steepness of the curve. Given m(1) through  $m(t_{max})$ , a and b can be calculated. Note the following properties:

$$m(0) = 0$$
  

$$m(t_{max}) = SC(t_{max})$$
  

$$\lim_{t \to 0} m(t) = a$$

# = maximum statement coverage

It is the best of the models attempted, but its results are imperfect even when a variety of data transformations are applied. Plots 17-24 show some of the fitted models and their residuals. This remains an area of future research.

In summary, we have used structural coverage to provide insight into how functional acceptance test and operational usage exercise a program's code; to suggest results that effect reliability models; to suggest a relationship between procedure coverage and statement coverage; and to move toward understanding statement coverage growth.

# 3.2. Comparison of Inputs Using Structural Coverage Metrics

Does functional testing have the same coverage profile as operational usage, or more generally, can structural coverage be used to compare two sets of program inputs? This question is interesting for two reasons:

- (1) Some testing models require input sets that are "representative" of operational usage [Brown75]. Structural coverage could provide a way of measuring this.
- (2) Many reliability models, when using past failure data to predict failure rate or number of failures, assume that the past inputs are similar to the present inputs. Structural coverage could provide a method for confirming this.

#### Question:

Can the Venn diagram technique be used to differentiate input sets?

In section 3.1 we compared functional test sets with operational usage using a Venn diagram technique (tables 5-6). We used this to show differences in the way operational usage exercised the program. Could this be extended to other input sets? For example, it seems plausible that tests generated with the goal of high branch coverage would execute different code than tests generated by test mutation on arithmetic expressions [DeMillo78] or that boundary value functional tests would exercise different sections of code than statistical predictions of operational usage. We hypothesize that the code in the different sections of the Venn diagram would reflect the properties of the two sets of tests.

# Question:

Can input sets be differentiated using nonparametric tests of structural coverage?

Acceptance test and operational usage were statistically compared

using both the Mann-Whitney and Kruskal-Wallis tests<sup>\*</sup>. The proposed hypotheses were: "For each of the structural coverage classes (procedures, executable statements, assignment statements...) the population represented by the 60 operational usage cases is similar to the population represented by the acceptance test cases."

Table 7 shows the Kruskal-Wallis H statistic. It shows the result of the test (reject or fail to reject) and the appropriate significance level for each statement class. Table 8 shows the results for the Mann-Whitney U statistic. The column "low U" shows which population had the lower central tendency.

The tests failed to reject the hypotheses for all statement types except READs. Since there are so few READ statements, a small, random difference in the tests could falsely manipulate the statistic. The other statement classes are less susceptible to small changes and represent a better population to examine.

The tests fail to reject the hypotheses that the two populations are similar, meaning that in this case, operational use and acceptance test cannot be distinguished by their structural coverage numbers.

Question:

Can the number of executions of prime sections of code be used to differentiate input sets?

<sup>\*</sup> The Mann-Whitney and Kruskal-Wallis tests were chosen because they are nonparametric tests; they make no assumptions about the distributions of source populations. The Mann-Whitney test is most sensitive to differences in "location (central tendency)." The Kruskal-Wallis test is sensitive to differences in "location or dispersion or skewness." [Siegel56].

Are statements executed as thoroughly by acceptance test as they are by operational usage? For each statement in the program, it is possible to count how many times it was exercised by a particular acceptance test or operational usage case. (This differs from the number of times it was executed). If acceptance test and operational usage are similar, then the percentage of acceptance test cases that executed a statement should be similar to the percentage of operational usage cases.

The two percentages were calculated for each prime section of code. The plotted data are shown in scatter plot 25. The regression line has slope 0.921 and intercept 0.032. The r square value is 0.863.

Since the plot does not show any imbalance, one could conclude that acceptance test and operational usage exercise the code equally thoroughly. It is a future goal of this research to replace this empirical judgement by a statistical test.

To summarize, we proposed three methods for comparing sets of program inputs: Venn diagram comparison of executed statements, statistical comparison, and thoroughness of execution of prime sections code. These methods may be able to differentiate input sets, a result that would be useful for understanding reliability models and some testing strategies.

# 3.3. Error, Faults, and Failures and Structural Coverage

The SEL has been collecting data on software development for 7 years [SEL82a]. Error, fault and failure data are collected using the "Change Report From" or CRF (see figure 2). A CRF is filed whenever a change, enhancement or fault repair is made to a subroutine or data

file. This study examines the fields "time to isolate the error," "the time to understand and implement," and the section "type of error\*."

There were eight faults found during operation. Each fault could be repaired by changing code in one procedure. One procedure contained two faults. With these data, we can address these questions:

Question:

Were heavily exercised sections of code more likely to contain faults?

These data are shown in table 9. A mark is entered for each of the 68 subroutines. The vertical axis describes the number of times the subroutine was exercised in operational usage. The subroutines that contained the faults are marked with "#".

Half of the procedures were exercised by more than 90% of the operational usage cases. About half of the revealed faults occurred in this group of procedures (3 of 8). With these data we reject the hypothesis that more heavily exercised subroutines are more likely to contain a revealed fault.

Tables 10-12 show faults categorized by time to isolate, time to understand, and number of times the procedure was exercised.

Question:

Is procedure coverage related to time to isolate?

<sup>\*</sup> Time to isolate the error is classified as taking: less than one hour, one hour to one day, greater than one day, never found. Time to understand and implement the change is classified as taking: less than one hour, one hour to one day, one day to three days, or greater than three days. Faults are categorized as originating in the: requirements, functional specification, design (either involving data or expression), external environment, use of language, clerical or other.

Time to isolate the change seems to be independent of procedure coverage.

#### Question:

Is procedure coverage related to time to understand and implement?

Increased usage seems to be associated with longer time to understand and implement a change. This might be explained by suggesting that the lightly exercised procedures contain fairly simple code while the heavily exercised code is, by necessity, more complicated and requires more time to modify.

# Question:

Is procedure coverage related to type of error?

Table 12 lists the faults classified by type and procedure coverage in operational usage. There are too few faults to reveal any interesting patterns.

In summary, we have tried to relate statement coverage to: "time to isolate an error," "time to understand an error," and "type of error." The data begins to suggest a relationship between "time to understand an error" and structural coverage. There were too few errors to make any firm statements about "time to isolate an error" and "type of error." This remains a promising area of study.

# 4. Structural Coverage and the Management of Acceptance Tests

Combined with failure data, structural coverage could aid the design of acceptance tests. Imagine a manager in charge of designing acceptance tests for a group of similar projects or for various releases

of a single project. With the failure data from the previous project or release and the structural coverage of both the acceptance and operational usage cases he can suggest new acceptance tests for the next release. He could require tests to exercise unexercised sections of code. He could require new acceptance tests to explain the code missed by acceptance test but exercised in operational usage. If he is using a testing methodology or reliability model that requires inputs that are representative of operational usage, he can use these data to select more representative tests.

We see structural coverage being used by a manager in an iterative fashion:

- (1) Gather structural coverage data on acceptance tests and release the project.
- (2) Gather structural coverage data and failure data on operational usage. Use these data to adjust reliability models.
- (3) Use structural coverage data to: suggest new tests and evaluate how the old tests were created.
- (4) Restart the cycle with the new acceptance tests.

# 5. Conclusions and Criticisms

#### We conclude:

(1) We may be able to compare sets of inputs using statistical tests and Venn diagram techniques. This would be useful for examining some testing methods and reliability models. (2) The structural coverage growth of different statement subclasses grows at different rates. This insight might be of interest to reliability model developers.

The data seem to imply:

- (1) Faults are independent of number of executions. We can (in our environment) reject the hypothesis that heavily exercised procedures are more likely to contain more revealed faults.
- (2) Procedure coverage may be used for statement coverage.
- (3) Management of the acceptance test process is possible.This study can be criticized on a number of points:
- (1) There are too few faults to make any forceful statements about errors, faults, failures and structural coverage. (But then again we cannot fault NASA/GSFC for having programs with too few faults.)
- (2) While the data suggests that it may be possible to differentiate test sets using structural coverage, we have never provided an example that shows that it can!
- (3) This study does not address the order in which the functional tests were used, the order of the operational usage cases or which operational usage cases revealed the faults.
- (4) The study did not produce a good model of structural coverage growth.

These points will be addressed when the study is replicated in the summer and fall of 1984. The program being studied is DERBY [CSC83], a large (300 routines, 50k source lines of code), satellite simulator.

The new project is larger and should have more faults. With the new project, we will gather more thorough information on the order of system tests, acceptance tests, operational usage cases, plus the exact input that reveals a failure. The results of this new study should answer many of the questions raised by this study.

# 6. Acknowledgments

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# CHANGE REPORT FORM

NUMBER\_\_\_\_\_

ROJECT N	AME CURRENT DATE
REASON	SECTION A - IDENTIFICATION Why was the change made?
DESCRIP	TION: What change was made?
EFFECT:	What components (or documents) are changed? (Include version)
EFFORT:	What additional components (or documents) were examined in determining what change was needed?
What was	(Month Day Year) Need for change determined on Change started on
	1 hour or less,1 hour to 1 day,1 day to 3 days,more than 3 days
	SECTION B - TYPE OF CHANGE (How is this change best characterized?)
	correction
🗍 Planne	enhancement D Optimization of time/space/accuracy
Impien	nentation of requirements change
	ement of clarity, maintainability, or documentation
	ement of user services
	Was more than one component affected by the change? Yes No
	FOR ERROR CORRECTIONS ONLY
	SECTION C - TYPE OF ERROR (How is this error best characterized?)
🗆 Require	ements incorrect or misinterpreted
🛛 Functio	onal specifications incorrect or misinterpreted
- Design	error, involving several components
-Ci Error i	n the design or implementation of a single component 🛛 Other (Explain in E)
	FOR DESIGN OR IMPLEMENTATION ERRORS ONLY
if the	error was in design or implementation:
The err	or was a mistaken assumption about the value or structure of data
The err	or was a mistake in control logic or computation of an expression

#### FOR ERROR CORRECTIONS ONLY

# SECTION D - VALIDATION AND REPAIR

What activities were used to validate the program, detect the error, and find its cause?

	Activities Used for Program Validation	Activities Successful in Detecting Error Symptoms	Activities Tried to Find Cause	Activities Successful in Finding Cause
Pre-accuptance test runs				
Acceptance testing				
Post-acceptance use				
Inspection of output				
Code reading by programmer				
Code reading by other person				
Talks with other programmers				
Speciał debug code				
System error messages				
Project specific error messages				
Reading documentation				
Trace	•			
Dump				
Cross reference/attribute list				
Proof technique				
Other (Explain in E)	· · · · ·		· · ·	

What was the time used to isolate the cause?

\_\_\_\_one hour or less, \_\_\_\_one hour to one day, \_\_\_\_more than one day, \_\_\_\_never found

If never found, was a workaround used? Yes No (Explain in E)

Was this error related to a previous change?

\_\_\_\_\_Yes (Change Report #/Date\_\_\_\_\_) \_\_\_\_No \_\_\_\_Can't tell

When did the error enter the system?

\_\_\_\_requirements \_\_\_\_\_functional specs \_\_\_\_\_design \_\_\_\_\_coding and test \_\_\_\_\_other \_\_\_\_\_can't tell

# SECTION E - ADDITIONAL INFORMATION

Please give any information that may be helpful in categorizing the error or change, and understanding its cause and its ramifications.

580-2 (5/78).

Name:

Authorized: \_

\_\_\_\_ Date: \_\_\_\_



# Plot 1. Assignment Statement Coverage vs Procedure Coverage for 17 Acceptance Tests.

(2) 91 (0) → (Ch 12)



Plot 2. CALL Statement Coverage vs Procedure Coverage for 17 Acceptance Tests.

() Ørstent (t



Plot 3. Do Statement Coverage vs Procedure Coverage for 17 Acceptance Tests.

A 0



Plot 4. Executable Statement Coverage vs Procedure Coverage for 17 Acceptance Tests.

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Plot 5. IF Statement Coverage vs Procedure Coverage for 17 Acceptance Tests.



Plot 6. READ Statement Coverage vs Procedure Coverage for 17 Acceptance Tests.

(Y M ATO N



# Plot 7. WRITE Statement Coverage vs Procedure Coverage for 17 Ac-ceptance Tests.

36-----



Plot 8. Assignment Statement Coverage vs Procedure Coverage for 60 Operational Usage Cases.

非行うちょうにもうにもの



Plot 9. CALL Statement Coverage vs Procedure Coverage for 60 Operational Usage Cases.

# U Berner VI

slope = 8.251 intercept = -192.712 r square = 0.797
std err = 21.364 T statistic = 15.192 correlation = 0.894
There are 60 data points. Use T(58) for significance test.



Plot 10. Do Statement Coverage vs Procedure Coverage for 60 Operational Usage Cases.

#1000

- -



Plot 11. Executable Statement Coverage vs Procedure Coverage for 60 Operational Usage Cases.



Plot 12. IF Statement Coverage vs Procedure Coverage for 60 Operational Usage Cases.

# 144 A



Plot 13. READ Statement Coverage vs Procedure Coverage for 60 Operational Usage Cases.

\* . . . . . .

slope = 0.251 intercept = 1.565 r square = 0.293
std err = 2.014 T statistic = 4.908 correlation = 0.542
There are 60 data points. Use T(58) for significance test



Plot 14. WRITE Statement Coverage vs Procedure Coverage for 60 Operational Usage Cases.

#36~~~


Plot 15. Structural Coverage of 100 Permutations of 60 Operational Usage Cases. (median, 10th, and 90th percentiles superimposed)



Plot 16. Structural Coverage of 100 Permutations of 10 Acceptance Tests. (median, 10th, and 90th percentiles superimposed)



Plot 17. NHPP Model Fitted to the First 5 Values of the 100 Operational Growth Sequences. (residuals)



Plot 18. NHPP Model Fitted to the First 5 Values of the 100 Operational Growth Sequences. (plot of a vs b)



Plot 19. NHPP Model Fitted to the First 10 Values of the 100 Operational Growth Sequences. (residuals)



Plot 20. NHPP Model Fitted to the First 10 Values of the 100 Operational Growth Sequences. (plot of a vs b)



Plot 21. NHPP Model Fitted to the First 15 Values of the 100 Operational Growth Sequences. (residuals)



Plot 22. NHPP Model Fitted to the First 15 Values of the 100 Operational Growth Sequences. (plot of a vs b)







Plot 24. NHPP Model Fitted to the First 20 Values of the 100 Operational Growth Sequences. (plot of a vs b)



slope = 0.921 intercept = 0.032 r square = 0.863
std err = 0.129 T statistic = 83.652 correlation = 0.929
There are 1115 data points. Use T(1113) for significance test.

Plot 25. Comparison of Execution Coverage of Acceptance Test and Operational Usage.

\_\_\_\_\_\_

			Statement				<u></u>	
1			the MAL					
		by 1	and the second	rk Test		· ·		
Case	Procs	Exec	Assign	Calls	Do	If	Reads	Writes
1   2	33 30	1069 913	530 446	76 84	52 37	246 203	6	13 10
1 3	33	1067	529	76	52	246	6	13
4	30	932	456	84	39	209	6	11
5	30 33	1049	519	1 77	51	241	6	12
6   7	37 30	1304 928	632 455	110 84	62 39	288 208	11	22 10
8	36	1228	622	10,1	61	278	6	14
9	30	928	455	84	39	208	6	10
10 	44	1677	821	161	71	368	11	21
11	46	1786	855	216	76	375	9	16
12	38	1285	640	102	58	285	9	20
13	40	1448	691	166	57	324	1 1	12
14   15	45 45	1675 1959	819 957	169 209	70 85	367 414	9	20
	45	425	721	209	60	414	ני ו	25
16	45	1764	861	177	73	383	12	24 1
17	45	1728	840	171	71	379	12	24
Union	51	2408	1187	286	108	490	14	30
Intersect	29	778	389	42	35	186	6	10
Maximum	68	4300	1870	418	157	753	34	206

Table 1.

			Stateme	nt Cover	age			
1			of the MAI	• · · · ·			`	
1			17 Benchr					ĺ
		the second s	Percentag	and the second se	the second s	<u>ند بي رو بر محمد المكامل اليكار</u>		
Case	Procs	Exec	Assign	Calls	Do	If	Reads	Writes
1	1 48.5	24.9	28.3	18.2	l 33.1	32.7	17.6	6.3
2	44.1	21.2	23.9	20.1	23.6	27.0	1 17.6	4.9
3	48.5	24.8	28.3	18.2	33.1	32.7	1 17.6	6.3
4	44.1	21.7	24.4	20.1	24.8	27.8	1 17.6	5.3
5	48.5	24.4	27.8	18.4	32.5	32.0	17.6	5.8
6	54.4				   •• •			
1 7	44.1	30.3	33.8	26.3	39.5	38.2	32.4	10.7
8	52.9	28.6	24.3	20.1	24.8	27.6	17.6	4.9
9	44.1	21.6	24.3	20.1	38.9 24.8	36.9	17.6	6.8
10	64.7	39.0	43.9	38.5	45.2	48.9	17.6	4.9
			-+J•J		-12-2	40.9	32.4	10.2
11	67.6	41.5	45.7	51.7	48.4	49.8	26.5	7.8
12	55.9	29.9	34.2	24.4	36.9	37.8	26.5	9.7
13	58.8	33.7	37.0	39.7	36.3	43.0	20.6	5.8
14	66.2	39.0	43.8	40.4	44.6	48.7	26.5	9.7 j
15	66.2	45.6	51.2	50.0	54.1	55.0	38.2	12.1
1 16	66.2	41.0	46.0	42.3	46.5	50.9	35.3	11 7
17	66.2	40.2	44.9	40.9	45.2	50.9	35.3	11.7
1								
Union	75.0	56.0	63.5	68.4	68.8	65.1	41.2	14.6
Intersect	42.6	18.1	20.8	10.0	22.3	24.7	17.6	4.9

Table 2.

		<u></u>		ent Cove				
		by	of the M 60 Operat:					
Case	Procs	Exec	Assign	Calls	Do	If	Reads	Writes
1 2 3 4 5 6 7 8 9 10	39 43 45 37 37 36 33 39 37 37	1368 1712 1830 1262 1252 1098 1012 1359 1246 1252	660 832 896 625 618 536 486 652 619 618	125 193 184 86 120 84 94 129 84 120	52 80 78 57 53 50 39 52 56 53	324 381 411 278 276 2 <b>5</b> 8 236 331 275 276	10 10 13 14 10 9 9 9 14 10	14 19 22 24 15 14 13 13 23 15
11 12 13 14 15 16 17 18 19 20	44 37 35 35 46 37 37 37 37	1743 1249 1295 1286 1136 1794 1272 1252 1270 1249	831 616 666 545 853 637 618 635 616	196 120 81 106 217 86 120 86 120	76 53 68 68 45 76 57 53 57 53	382 275 306 305 272 378 278 276 278 276 278 275	11 10 10 9 12 14 10 14 10	19 15 19 19 14 19 24 15 24 15
21 22 23 24 25 26 27 28 29 30	37 43 30 39 34 37 37 37 43	1118 1657 994 986 1361 1235 1123 1260 1270 1779	532 807 505 496 646 638 529 626 635 857	113 155 62 66 132 76 104 85 86 192	39 68 42 53 67 52 57 57 80	253 363 242 241 322 288 265 276 278 413	7 14 8 8 10 10 9 14 14 14	9 25 13 13 14 19 14 24 24 24 20
31 32 33 35 36 37 38 39 40	37 30 33 21 39 37 44 37 44 38	1218 997 1070 561 1424 1250 1743 1262 1749 1258	593 500 538 299 681 619 831 629 832 612	121 66 63 21 164 85 196 86 199 117	50 41 49 25 60 56 76 57 77 55	282 247 264 108 305 275 382 278 383 298	9 8 9 8 10 14 11 14 11 10	13 13 15 11 15 24 19 23 19 15

Table 3.

				nt.)				
Case	Procs	Exec	Assign	Calls	Do	If	Reads	Writes
41	39	1290	638	101	58	286	12	23
42	36	1351	695	87	71	326	9	18
43	37	1246	619	84	56	275	14	23
44	45	1736	838	172	71	382	15	27
45	45	2002	971	213	86	435	16	28
46	44	1685	819	162	71	371	14	24
47	39	1292	640	101	58	286	12	23
48	45	1683	817	170	70	370	12	23
49	45	1970	956	210	86	417	16	-28
50	45	1772	859	178	73	386	15	27
51	39	1337	635	127	54	317	10	16
52	37	1271	635	86	58	280	14	23
53	34	1184	585	109	46	267	9	15
54	40	1355	650	126	52	333	9	13
55	40	1456	689	167	57	327	10	15
56	37	1250	617	120	53	275	10	15
57	37	1248	603	115	54	302	9	14
58	37	1272	637	86	57	278	14	24
59	34	1048	516	72	50	242	9	15
50	20	527	273	19	24	106	8	11
UNION	55	2757	1345	327	120	581	19	36
INTERSECT	19	442	228	16	19	86	7	9
MAXIMUM	68	4300	1870	418	157	753	34	206
<u></u>								

<b></b>			Stat	ement Co	verage			
			of the	MAL Prep	rocessor			
		by	60 Opera					
Case	Procs	Exec	Assign	Calls	Maximum) Do	If	Reads	Writes
	1		TOOTRI	Jarra	1		I IIIIII	41.TCG2
1	57.4	31.8	35.3	29.9	33.1	43.0	29.4	6.8
2	63.2	39.8	44.5	46.2	51.0	50.6	29.4	9.2
3 4	66.2 54.4	42.6 29.3	47.9 33.4	44.0 20.6	49.7 36.3	54.6 36.9	38.2	10.7 11.7
	54.4	29.1	33.0	28.7	33.8	36.7	29.4	7.3
5 6	52.9	25.5	28.7	20.1	31.8	34.3	26.5	6.8
7	48.5	23.5	26.0	22.5	24.8	31.3	26.5	6.3
8	57.4	31.6	34.9	30.9	33.1	44.0	26.5	6.3
9 10	54.4 54.4	29.0 29.1	33.1 33.0	20.1	35.7 33.8	36.5 36.7	41.2 29.4	11.2
					JJ•0		67.7	1+3
11	64.7	40.5	44.4	46.9	48.4	50.7	32.4	9.2
12	54.4	29.0	32.9	28.7	33.8	36.5	29.4	7.3
13 14	51.5 51.5	30.1 29.9	35.6 35.3	19.4 19.4	43.3 43.3	40.6	29.4 29.4	9.2 9.2
15	51.5	26.4	29.1	25.4	28.7	36.1	26.5	6.8
16	67.6	41.7	45.6	51.9	48.4	50.2	35.3	9.2
17	54.4	29.6	34.1	20.6	36.3	36.9	41.2	11.7
18 19	54.4 54.4	29.1 29.5	33.0 34.0	28.7 20.6	33.8 36.3	36.7 36.9	29.4 41.2	7.3
20	54.4	29.0	32.9	20.0	33.8	36.5	29.4	11.7 7.3
21	54.4	26.0	28.4	27.0	24.8	33.6	20.6	4.4
22 23	63.2 44.1	38.5 23.1	43.2 27.0	37.1 14.8	43.3 26.8	48.2 32.1	41.2 23.5	12.1
24	44.1	22.9	26.5	15.8	26.8	32.0	23.5	6.3
25	57.4	31.7	34.5	31.6	33.8	42.8	29.4	6.8
26	50.0	28.7	34.1	18.2	42.7	38.2	29.4	9.2
27 28	54.4 54.4	26.1 29.3	28.3 33.5	24.9 20.3	33.1 36.3	35.2 36.7	26.5 41.2	6.8 11.7
29	54.4	29.5	34.0	20.5	36.3	36.9	41.2	11.7
30	63.2	41.4	45.8	45.9	51.0	54.8	29.4	9.7
31	en h	<u> </u>	21 7	78 0	21 0	37 F	26 E	6.2
31 32	54.4 44.1	28.3 23.2	31.7 26.7	28.9 15.8	31.8 26.1	37.5	26.5 23.5	6.3 6.3
33	48.5	24.9	28.8	15.1	31.2	35.1	26.5	7.3
34	30.9	13.0	16.0	5.0	15.9	14.3	23.5	5.3
35	57.4	33.1	36.4	39.2	38.2	40.5	29.4	7.3
36 37	54.4 64.7	29.1 40.5	33.1 44.4	20.3 46.9	35.7 48.4	36.5 50.7	41.2 32.4	11.7 9.2
38	54.4	29.3	33.6	20.6	36.3	36.9	41.2	11.2
39	64.7	40.7	44.5	47.6	49.0	50.9	32.4	9.2
40	55.9	29.3	32.7	28.0	35.0	39.6	29.4	7.3

Table 4.

	•								
				•					
	<u> </u>			Stateme	nt Covera	ige	iii		T
			0 hr 60	f the MAL	. Preproc	essor			
			by 60	Operatic Percentag	nal Usea te of Max	ge Cases imum)	•		
			• •		cont.)				
	Case	Procs	Exec	Assign	Calls	Do	If	Reads	Writes
	41	57.4	30.0	34.1	24.2	36.9	38.0	35.3	11.2
	42	52.9	31.4	37.2	20.8	45.2	43.3	26.5	8.7
	43 44	54.4	29.0	33.1	20.1	35.7	36.5	41.2	11.2
•	44	66.2 66.2	40.4	44.8 51.9	41.1	45.2	50.7	44.1	13.1
	46	64.7	39.2	43.8	51.0 38.8	54.8 45.2	57.8 49.3	47.1 41.2	13.6 11.7
	47	57.4	30.0	34.2	24.2	36.9	38.0	35.3	11.2
	48	66.2	39.1	43.7	40.7	44.6	49.1	35.3	11.2
	49 50	66.2 66.2	45.8 41.2	51.1 45.9	50.2 42.6	54.8 46.5	55.4	47.1	13.6
					72.0	40.5	51.3	44.1	13.1
	51	57.4	31.1	34.0	30.4	34.4	42.1	29.4	7.8
	52 53	54.4 50.0	29.6	34.0	20.6	36.9	37.2	41.2	11.2
	54	58.8	27.5 31.5	31.3 34.8	26.1 30.1	29.3 33.1	35.5	26.5	7.3
	55	58.8	33.9	36.8	40.0	36.3	43.4	29.4	7.3
	56 57	54.4	29.1	33.0	28.7	33.8	36.5	29.4	7.3
	58	54.4 54.4	29.0 29.6	32.2 34.1	27.5 20.6	34.4 36.3	40.1	26.5 41.2	6.8
	59	50.0	24.4	27.6	17.2	31.8	32.1	26.5	11.7
	60	29.4	12.3	14.6	4.5	15.3	14.1	23.5	5.3
	UNION	80.9	64.1	71.9	78.2	76.4	77.2	55.9	17.5
Į	INTERSECT	27.9	10.3	12.2	3.8	12.1	11.4	20.6	4.4
						· · ·			

	Comparison of Statement Coverage of the MAL Preprocessor by 17 Acceptance Test Cases and 60 Operational Usage Cases.											
Case	Procs	Exec	Assign	Calls	Do	If	Reads	Writes				
Acpt Usage	51	2408 2757	1187   1345 	286 327	108 120	490 581	14 19	30 36				
Union I Intersect	55 51	2768 2397	1353 1179	327 286	120 108	581 490	19 14	36 30				
А-ОрИ ОрИ-А	0	11 360	8 166	0 41	0 12	0 91	0	0 6				

## Table 5.

Comparison of Statement Coverage of the MAL Preprocessor by 17 Acceptance Test Cases and 60 Operational Usage Cases. (by percentage of Maximum)												
Case	Procs	Exec	Assign	Calls	Do	If	Reads	Writes				
Acpt Usage	75.0 80.9	56.0 64.1	63.5 71.9	68.4 78.2	68.8 76.4	65.1	41.2 55.9	14.6 17.5				
Union Intersect	80.9 75.0	64.4 55.7	72.4 63.0	78.2 68.4	76.4 68.8	77.2	55.9 41.2	17.5 14.6				
A-OpU OpU-A	0.0	0.3 8.4	0.4 8.9	0.0 9.8	0.0 7.6	0.0	0.0 14.7	0.0 2.9				

Table 6.

Kruskal-Wallis Comparison of Acceptance Test and Operational Usage Coverage. HO: populations are the same.									
Coverage Type	H	Result							
Procedure	0.076	ftr @ 0.1							
Executable Statement	0.218	ftr @ 0.1							
Assignment	0.076	ftr @ 0.1							
Call	0.005	ftr @ 0.1							
Do	0.005	ftr @ 0.1							
If	0.362	ftr @ 0.1							
Read	11.657	reject @ 0.001							
Write	2.608	ftr @ 0.1							

Table 7.

Mann-Whitney Comparison of Acceptance Test and Operational Usage Coverage. HO: populations are the same.										
Coverage Type		low U	Result							
Procedure	487.5	AT	ftr @ 0.1							
Executable Statement	472.0	AT	ftr @ 0.1							
Assignment	487.5	AT I	ftr @ 0.1							
Call	504.0	AT j	ftr @ 0.1							
Do	504.0	OpU	ftr @ 0.1							
If	461.0	AT	ftr @ 0.1							
Read	232.0	AT	reject @ 0.01							
Write	378.5	AT	ftr @ 0.1							

Table 8.

	Pro	cec	lures	s Class:	lfi	ed b	У	the	
Number	of	Ti	mes	Procedu	re	was	E	xercised	1
	Tota	al	Oper	rational	LΕ	xecu	ti	ons	

(Faulty procedures are starred.) (Unexecuted procedures are u's)

	Pr	.00	ec	lur	es
100%	×	*	¥	p	р
	P	р	р	р	р
	P	р	р	р	р
	P	р	р	р	р
	P	р	р	р	р
	P	р			
90%	P	р	р		
80%	*	¥	р	р	
70%	P				
60%	P	р	р	р	
50%	×	р	р	р	
40%	*	р	р	р	р
	P				
30%	P	р	р		
20%					
10%	×.	р	р	р	р
	P	р			
0%	u	u	u	u	u
	u	u	u	u	u
	l u	u	u		

Table 9.

	Time to Isolate the Change vs Number of Times Procedure was Exercised / Total Operational Executions. (Effort to Understand and Implement in Parenthesis)					
100% 90%	(1h < 1d)	(1h < 1d) (1d < 3d)		···		
80% 70% 60%		(1h < 1d)	(1d < 3d)			
50% 40%	(1h < 1d) (1 hour < )					
30% 20%						
10%	< 1 hour	(1h < 1d) 1 hour < 1 day	> 1 day	never found		

Table 10.

	Number	derstand and Imple of Times Procedure otal Operational Ex	was Exercised /	99999999999999999999999999999999999999
	(Effort t	o Isolate the Caus	e in Parenthesis)	
100%		(1 h < 1 d) (1 hour < )	(1 h < 1 d)	
90% 80% 70%		(1 h < 1 d)	( >1 day)	
60% 50% 40%	(1 hour < )	(1 hour < )		
30% 20%	(Thour ()			
10%	< 1 hour	(1 h < 1 d) 1 hour < 1 day	1 day < 3 days	> 3 days

Table 11.

	<u></u>	Number of	f Times	Procedu	sification re was Exe Execution	rcised /		
	Req.		Design		Extern.	Lang.	Cler.	Other
		Specs.	Data	Exp	Env.			
100% 90% 80% 70%		x	x	x,x		x		
60% 50%						x		
40% 30% 20%					X			
10%			x					

Table 12.