

# Delay Models in Data Networks

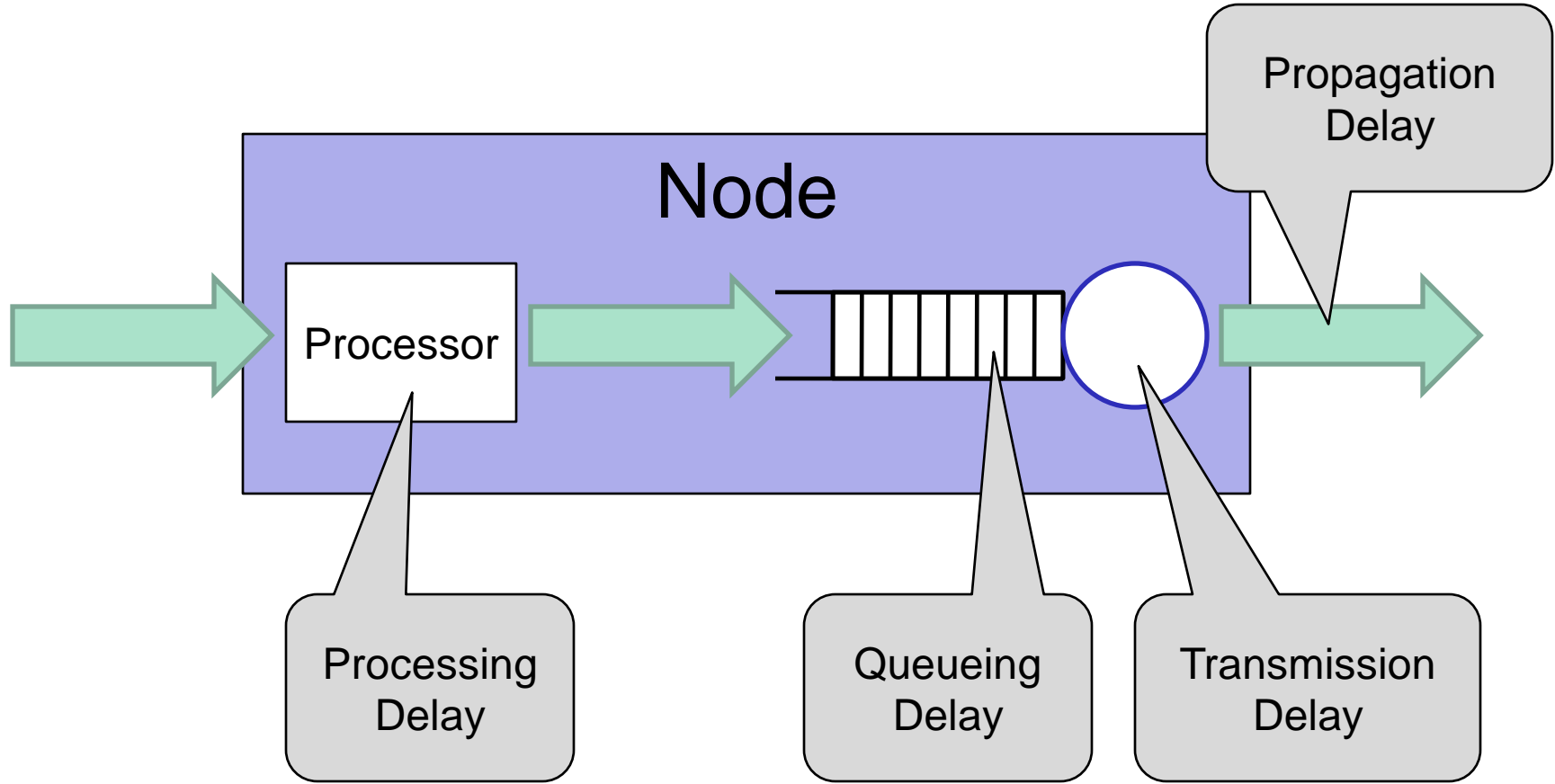


# Sources of Delay

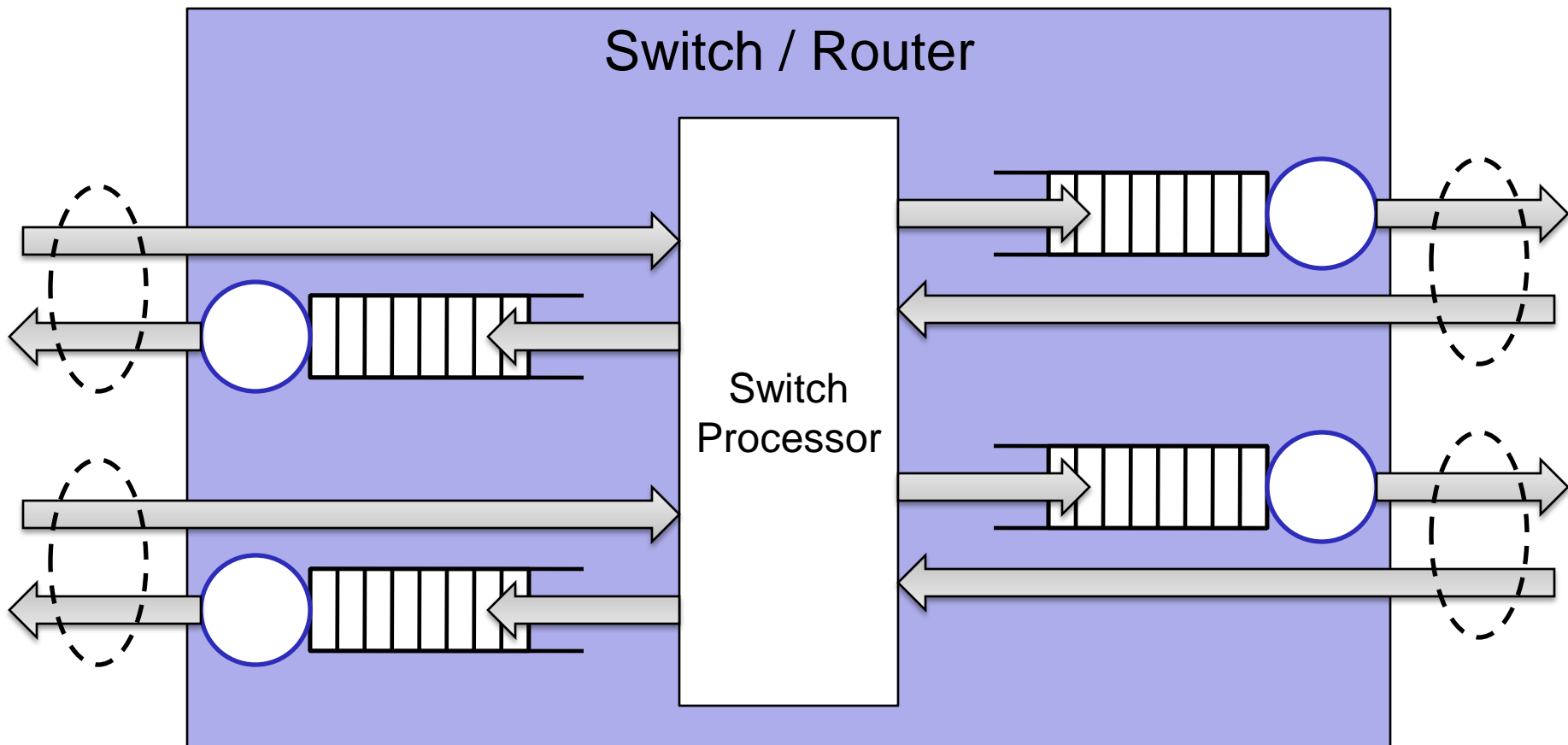
- Processing Delay
  - Time between when a packet is received and scheduled on an outgoing queue
- Queueing Delay
  - Time packet spends in the outgoing queue
- Transmission Delay
  - Time between when the first and last bits are transmitted
- Propagation Delay
  - Time it takes for the last bit to leave the transmitter and arrive at the receiver



# Graphical Representation



# Logical Diagram of Node Internals



# Queueing Theory

- Assume customers (packets) arrive at a queue at random times
  - Inter-arrival time: average time between customers
  - Arrival rate:  $\lambda = (\text{inter-arrival time})^{-1}$
- Each customer (packet) takes a random amount of time to service (transmit)
  - Service time: average time to service each customer
  - Departure rate:  $\mu = (\text{service time})^{-1}$
- Useful Information
  - Average number of customers in the system =  $N$
  - Average number in the queue =  $N_Q = \max(N-1, 0)$
  - Average total delay per customer =  $T$
  - Average wait time  $W = T - 1/\mu$



# Little's Theorem

- On-Board Derivation
- $N = \lambda T$
- $N_Q = \lambda W$



# M/M/1 Queueing System

- Probabilistic queueing system
- M means “memoryless” which means exponentially-distributed arrival and service times
  - Interarrival time  $\sim \exp(\lambda)$
  - Service time  $\sim \exp(\mu)$
  - Note that  $E[\exp(\alpha)] = 1/\alpha$
- Result
  - $\alpha(t) \sim \text{Poisson}(t; \lambda)$
  - Number of arrivals and departures has a Poisson distribution



# Continuous-Time Markov Chains

- Analysis model for M/M/1 systems
- On-board Derivation
- Results:
  - $\rho = \lambda / \mu$
  - $N = \rho / (1 - \rho) = \lambda / (\mu - \lambda)$
  - $T = N / \lambda = 1 / (\mu - \lambda)$
  - $W = \rho / (\mu - \lambda)$
  - $N_Q = \rho^2 / (1 - \rho)$

