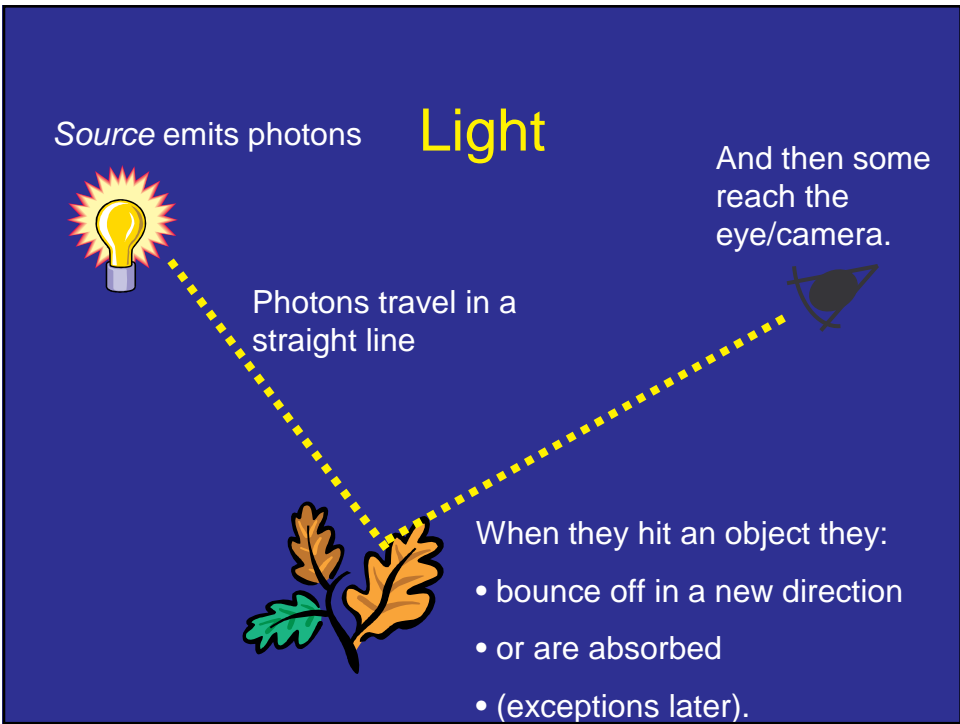


Lighting affects appearance

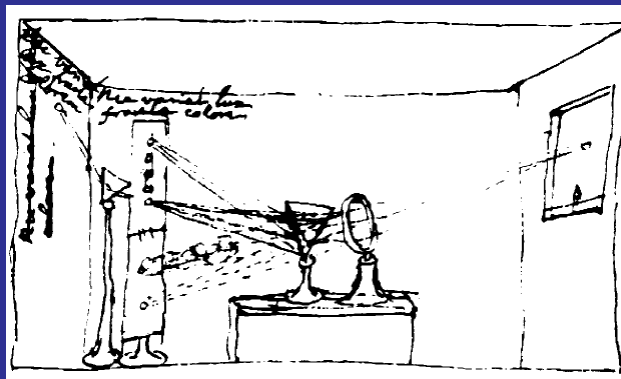




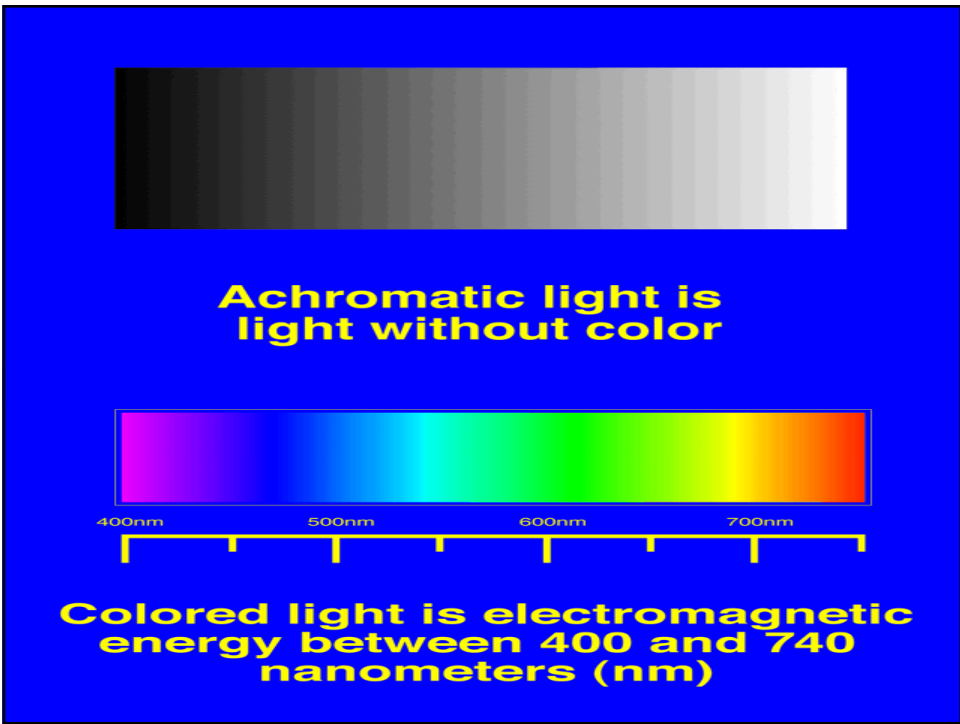
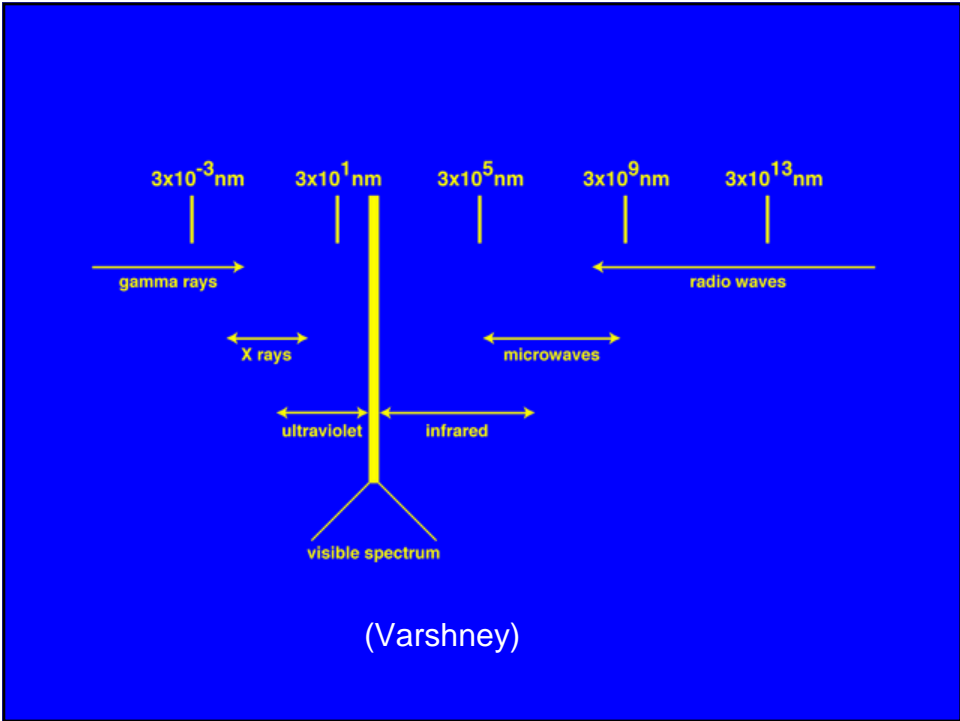
Basic fact: Light is linear

- Double intensity of sources, double photons reaching eye.
- Turn on two lights, and photons reaching eye are same as sum of number when each light is on separately.
- This means we can render lights separately

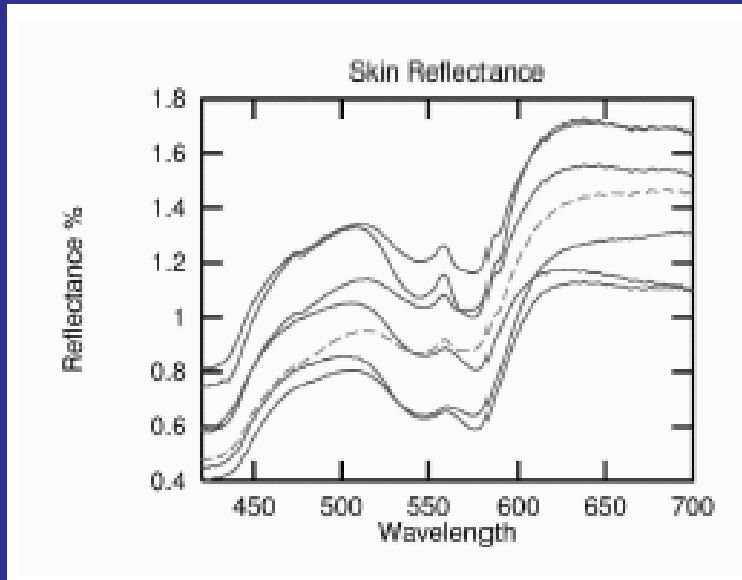
Newton's drawing:



(Wandell)

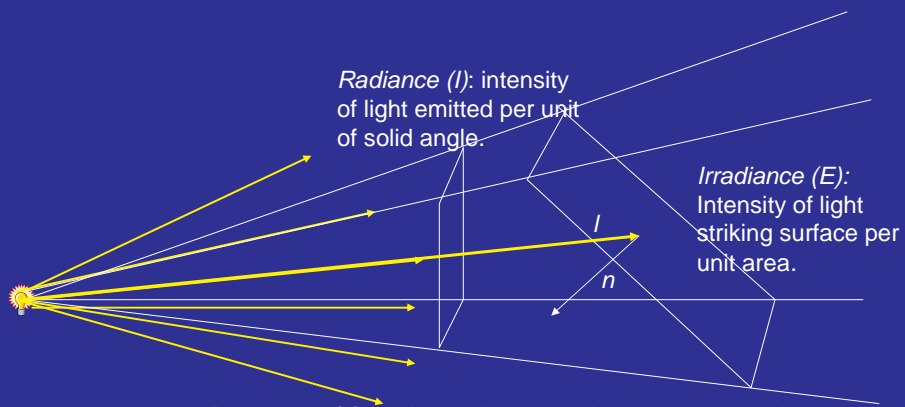


Color is a function



(Angelopoulou)

Light Intensity



Radiance (I): intensity of light emitted per unit of solid angle.

Irradiance (E): Intensity of light striking surface per unit area.

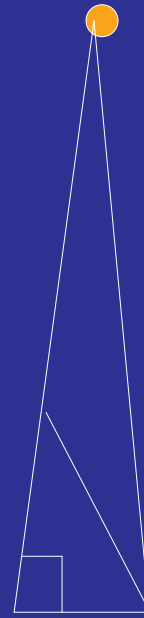
Because of foreshortening, as $\langle l, n \rangle$ decreases, the same light is spread over more and more area. In this picture,

$$E = I \cdot \langle n, l \rangle$$

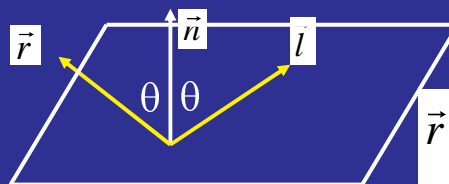
Intensity of light also decreases with square of distance.

Why is intensity linearly related to cosine theta?

Let's just take a 1D example. Imagine a distant point source. All light it emits passes through a circle a distance r from the point, with a length $2\pi r$. Now, imagine a small patch of material of length 1 . The light striking this patch also strikes a part of the circle. If the patch is very small, the angle between the light ray and the circle is a right angle. So if the patch is length 1 , the part of the circle that the patch shadows is $\cos \theta$. The total light striking the patch is $\cos(\theta)/2\pi r$, which grows linearly with $\cos(\theta)$.



Light Reflection: Mirror



$$\vec{r} + \vec{l} = 2(\vec{l} \cdot \vec{n})\vec{n}$$

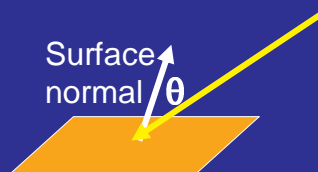
$$\vec{r} = 2(\vec{l} \cdot \vec{n})\vec{n} - \vec{l}$$

Light Reflection: Lambertian

- Amount of light striking surface proportional to $\cos \theta$
 - Angle between light direction and surface normal.
- Equal brightness in all directions
- Albedo is fraction of light reflected.
- Diffuse objects (chalk, cloth, matte paint).
- Brightness doesn't depend on viewpoint.



This surface appears to be foreshortened according to $\cos \theta$. So, if light striking a pixel at any angle is the same, the amount of light must increase with $\cos \theta$. That is, more light in direction of surface normal.



Lambertian + Point Source

$$\vec{l} = l \cdot \hat{l} \quad \left\{ \begin{array}{l} \hat{l} \text{ is direction of light} \\ l \text{ is intensity of light} \end{array} \right.$$

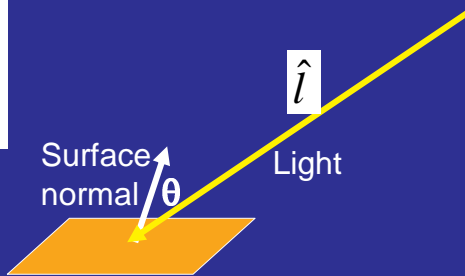
$$i = \max(0, \lambda(\vec{l} \cdot \hat{n}))$$

i is radiance

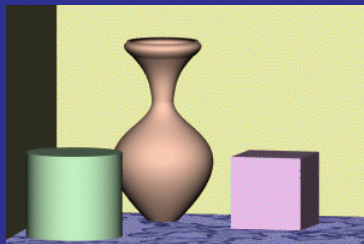
λ is *albedo*

\hat{n} is surface normal

Note: color depends on surface. With mirror, color only depends on light.



Lambertian Examples



Scene

(Oren and Nayar)



Lambertian sphere as the light moves.

(Steve Seitz)

Ambient

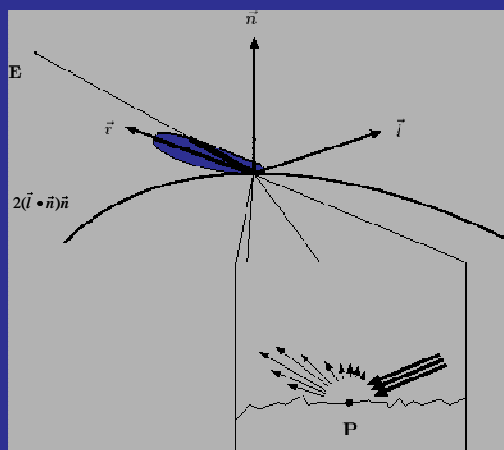
- Assume Lambertian surface normal receives equal light from all directions.

$$i = a\lambda$$

- Diffuse lighting, no cast shadows.
- Ambient (and point) light can be colored

Specular surfaces

- Brightness depends on viewing direction.
- Specularity is spread out.
 - Mirror, smooth light all bounces same way.
 - Slightly rougher, direction of bounce varies.
 - Diffuse, many bounces



(<http://graphics.cs.ucdavis.edu/GraphicsNotes/Shading/Shading.html>)

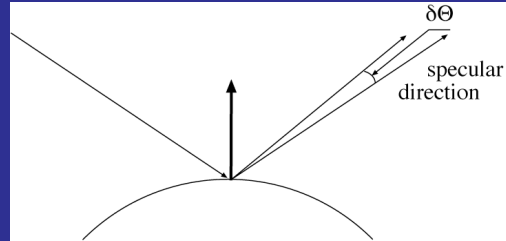
Phong's model

- Empirical model (eg., hack)
- Phong's model

– reflected energy falls off as:

$$\cos^n(\delta\theta)$$

- n very big, this is like mirror.
- As n gets smaller, specularity more spread out.
- Good model for plastic
- Specularity color of source.

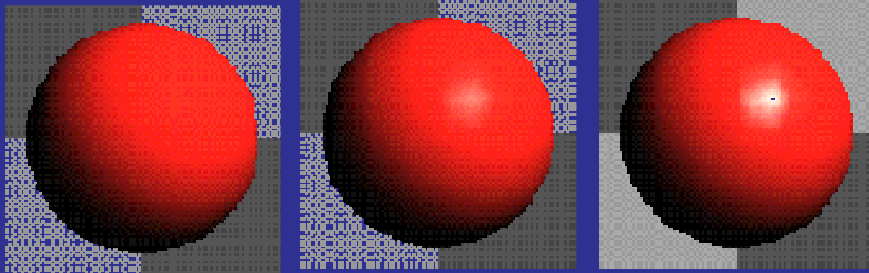


(Forsyth & Ponce)

Lambertian + specular

- Two parameters: how shiny, what kind of shiny.
 - Many objects combine shiny and diffuse material
 - Wood with veneer; glossy paint, plastic, greasy skin.
 - Some fraction of light reflected as diffuse, some as specular.

Lambertian+Specular+Ambient

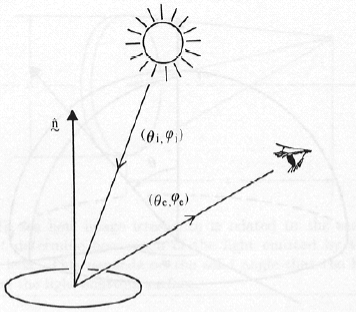


(<http://graphics.cs.ucdavis.edu/GraphicsNotes/Shading/Shading.html>)

More complex reflectances

- Physically realistic models
 - ▲ Torrance Sparrow models roughness of surfaces and shadowing of microfacets.
 - Specular peak can deviate from mirror direction.
 - Can produce much greater specularity at low incident angles.
 - ▲ Fresnel term. Specularity varies with incident angle.
 - Glass only specular as angle approaches 90 degrees.
- Models built from observation.
 - ▲ Measurement for every lighting direction and viewing direction.
 - ▲ A function describing this is called a *BRDF*
 - ▲ 4D function (can be reduced to 3D if there is rotational symmetry).

BRDF



Horn, 1986
Figure 10-7. The bidirectional reflectance distribution function is the ratio of the radiance of the surface patch as viewed from the direction (θ_e, ϕ_e) to the irradiance resulting from illumination from the direction (θ_i, ϕ_i) .

$$BRDF = f(\theta_i, \phi_i, \theta_e, \phi_e) = \frac{L(\theta_e, \phi_e)}{E(\theta_i, \phi_i)}$$

BRDF Not Always Appropriate



BRDF



BSSRDF

<http://graphics.stanford.edu/papers/bssrdf/>
(Jensen, Marschner, Levoy, Hanrahan)

Luminescence

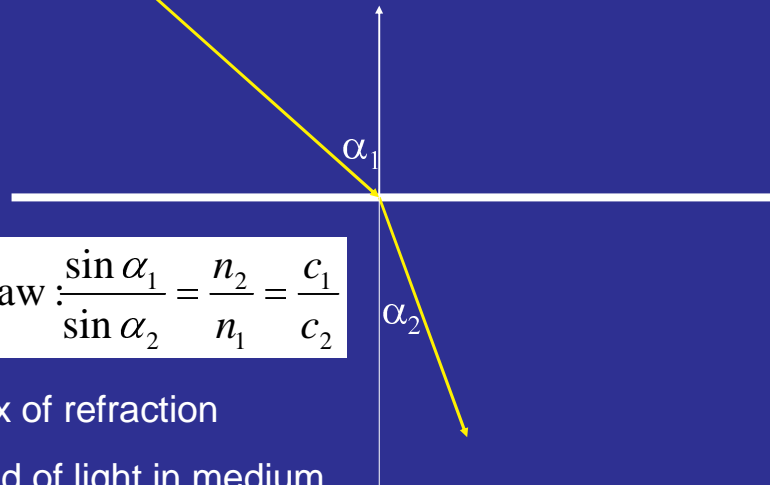
- Surface shifts color of light.
- Can reflect more light of a color than is present in source.
- This is why objects can glow in “black” light.

Transparency

- Some fraction of light passes through material.
- Varying this fraction for different colors produces colored, transparent objects.



Refraction



$$\text{Snell's Law: } \frac{\sin \alpha_1}{\sin \alpha_2} = \frac{n_2}{n_1} = \frac{c_1}{c_2}$$

n is index of refraction

c is speed of light in medium.

Illumination Attenuation

Light scatters from particles in the air. Fog or hazy air has more particles, more scattering.

