## Homework 6, Due WED July 23, 2014 NOTE- THIS HW IS TWO PAGES LONG.

- 1. (0 points) What is your name? Write it clearly. STAPLE your HW.
- 2. (30 points) For each of the following NIM game determine exactly when Player I wins. (That is, we want a statement like Player I wins iff  $n \equiv BLAH, BLAH \pmod{BLAH}$ .

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- (a) NIM(1,2)
- (b) NIM(1,3)
- (c) NIM(1,4)
- (d) NIM(1,5)
- (e) NIM(1,6)
- (f) NIM(1,7)
- 3. (20 points) Use your answer to the last problem to solve the following: Let  $a \ge 1$ . Then Player I wins NIM(1,a) iff n BLAH BLAH... (NOTEthere may be cases depending on properties of a- such as if a is prime then the condition is XXX, and if a is NOT prime the then condition is YYY. The XXX, YYY may themselves depend on a.)

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- 4. (20 points)
  - (a) Consider the 1-pile NIM game where you can remove a SQUARE number of stones. Find the Grundy Numbers for n = 0, ..., 25.
  - (b) Consider the 1-pile NIM game where you can remove a PRIME number of stones. Find the Grundy Numbers for n = 0, ..., 25. (NOTE- 1 is NOT a prime.)
  - (c) Consider the following 2-pile NIM game: From pile ONE you can remove a SQUARE number of stones, from pile TWO you can remove a PRIME number of stones. Position (a, b) means that pile ONE has a and pile TWO has b. For each of hte following positions say who wins (This will use the Grundy Numbers you computed in the earlier part of this problem.)
    - i. (15,19)
    - ii. (20,22)
    - iii. (15,22)
    - iv. (19,22)
    - v. (10,25)
- 5. (20 points) Consider the following 2-pile NIM game: From pile ONE you can remove a SQUARE number of stones, from pile TWO you can remove a CUBE number of stones. Write a program in psuedocode that will, given n, determine which player wins the game with a in pile ONE and b in pile TWO for all a, b with  $a + b \leq 2n$ . (This DOES NOT use Grundy Numbers.)