

**HW 11 CMSC 389. DUE Jan 20**  
**REMINDER- OPTIONAL PROJECT DUE JAN 20**  
**THIS HW IS TWO PAGES LONG**

1. (0 points) READ my NOTES SECRET SHARING- PARTICULARLY VERIFIABLE.
2. (30 points) Zelda wants to share a secret with  $A_1, A_2, A_3, A_4$  so that if 3 of them get together they can find out the secret but any 2 cannot. She uses the mod field 11. Assume that  $A_1$  gets 6,  $A_2$  gets 9 and  $A_3$  gets 1. (I am not telling you  $A_4$ 's share.) For each of the following either solve it OR tell me why it can't be solved.
  - (a)  $A_1, A_2, A_3$  all get together. Can they find out the secret? If so then find it out and tell me. If not then tell me why not.
  - (b)  $A_1, A_2, A_3$  all get together. Can they find out what  $A_4$ 's share was? If so then find it out and tell me. If not then tell me why not.
  - (c)  $A_1, A_2$  all get together. Can they find out the secret? If so then find it out and tell me. If not then tell me why not.
  - (d)  $A_1, A_2$  all get together. Can they find out what  $A_4$ 's share was? If so then find it out and tell me.
3. (30 points) Zelda wants to do VERIFIABLE Secret Sharing with  $A_1, A_2, A_3, A_4$  so that if 2 of them get together they can find out the secret but any 1 cannot. She uses the mod field  $p$  where  $p$  is large. But alas,  $A_4$  has a computer that can solve Discrete Log problems mod  $p$ . Alice gives out the shares and the appropriate powers of  $g$ . For each of the following statements state TRUE or FALSE and EXPLAIN your answer.
  - (a)  $A_4$  learn the secret.
  - (b)  $A_4$  learn  $A_1$ 's share.
  - (c)  $A_4$  give a false value of  $f(4)$  and have the other players not realize this.

**THERE IS A SECOND PAGE**

4. (40 points) (Read the notes on non-threshold secret sharing) Zelda wants to share a secret with  $A_1, A_2, A_3, A_4$  so that if  $A_1$  AND any two of  $A_2, A_3, A_4$  want to find the secret they can, but (1) any set that does not include  $A_1$  CANNOT get the secret, (2) Any set that is  $A_1$  and just ONE of  $\{A_2, A_3, A_4\}$  CANNOT get the secret. Show how Zelda CAN do this with shares of size  $|s|$ . Make up a HW problem on this that I can give to my next Winters class and also provide the solution. Make it so that next years class will see a clean problem and a clean solution. The kind you would want to see.