## HW 5 CMSC 452. Morally DUE March 4

1. (0 points) What is your name? Write it clearly. Staple your HW. When is the midterm? Where is the midterm? When is the Final?
2. (60 points)
(a) Show that $\left\{a^{2 n} b^{3 n} \mid n \in \mathbf{N}\right\}$ is not regular.
(b) Show that $\left\{w \mid 3 n_{a}(w)=2 n_{b}(w)\right\}$ is not regular.
(c) Show that $\left\{a^{n^{4}} \mid n \in \mathbf{N}\right\}$ is not regular.
3. (40 points) Show that the set of all functions from the Natural to the Primes is uncountable. (HINT: Assume, by way of contradiction, that there is a LIST Of all functions from Naturals to primes: $f_{1}, f_{2}, f_{3}, \ldots$. YOU need to CONSTRUCT a function $f$ from Naturals to Primes that is NOT on this list. YOU will want to define $f(i)$ so that $f(i) \neq f_{i}(i)$. KEY- still make sure that $f$ goes from naturals to primes.)
