

Homework 3

Due at the *beginning* of class on Oct. 6

1. Define $G : \{0, 1\}^n \rightarrow \{0, 1\}^{2n}$ by $G(s) = s\|\bar{s}$ (where \bar{s} denotes the bitwise complement of s). Prove that G is not a pseudorandom generator by describing and analyzing a concrete distinguisher.
2. Define the length-preserving, keyed function F by $F_k(x) = k \oplus x$. Prove that F is not a pseudorandom function by describing and analyzing a concrete distinguisher.
3. In class we discussed the encryption scheme in which a message $M = m_1, m_2, \dots$ is encrypted to give

$$\langle r_1, F_k(r_1) \oplus m_1, r_2, F_k(r_2) \oplus m_2, \dots \rangle,$$

where r_1, r_2, \dots are uniform and independent. We prove that this scheme is CPA-secure if F is a pseudorandom function.

Consider the keyed function F defined by $F_k(x) = k \oplus x$ from the previous problem. Describe how if this F is used in the above encryption scheme, the entire message can be recovered using a ciphertext-only attack and observing a single (sufficiently long) ciphertext.

4. Exercise 3.15. You should provide a short explanation of your answers, but no proofs are needed.