## **Practice Problems**

Numbered exercises are from the *first edition* of the book.

- 1. Exercise 10.1.
- 2. Exercise 10.4.
- 3. Exercise 10.11.
- 4. Exercise 10.12.
- 5. Exercise 10.13.
- 6. Exercise 10.17.
- 7. Consider textbook RSA encryption with public key 55 and public exponent e = 3.
  - (a) How many elements are in  $\mathbb{Z}_{55}^*$ ?
  - (b) Compute the private exponent d.
  - (c) Compute the encryption of the message m=6.
  - (d) Compute the decryption of the ciphertext c=2.
- 8. Consider El Gamal encryption using the cyclic group  $\mathbb{Z}_{19}^*$ . (Note: this is not a prime-order group, but El Gamal encryption can be defined in any cyclic group—even though it can only secure in prime-order groups.)
  - (a) How many elements are in this group?
  - (b) Find a generator of this group.
  - (c) Find an element in this group that is not a generator.
  - (d) Say a receiver uses your generator from part (b) and chooses private exponent 7. What is the receiver's public key?
  - (e) Using the public key from part (d), what is the encrption of m=2 using randomness r=4?