

Problem Set 1

Due by Feb. 25, 11:59 PM

Make sure to **check the HW1 FAQ** (linked from the course webpage) before your final submission: this page will include clarifications and possible hints, format requirements for the various submitted files, and submission instructions.

- (Warmup.) Create a program to encrypt using the one-time pad. Specifically:
 - Create a program `OTPgen.java` that takes as input a positive integer $n < 500$ (representing the desired message length) and generates a random key of the appropriate length. You should output the key in hexadecimal format to a file `OTPkey.txt`. (You may assume that n is a multiple of 8.)
 - Create a program `OTPenc.java` that reads a key from `OTPkey.txt` and a message from an ASCII file `OTPmsg.txt` and encrypts the message using the given key. Output the ciphertext in hexadecimal format to a file `OTPciphertext.txt`. You should return an error if the message and key lengths do not “match”.
 - Create a program `OTPdec.java` that reads a key from `OTPkey.txt` and a ciphertext from a hex file `OTPciphertext.txt` and decrypts the ciphertext using the given key. Output the message in ASCII format to a file `OTPdecrypt.txt`. You should return an error if the ciphertext and key lengths do not “match”.
- You will write a program to perform ECB-, CBC-, and CTR-mode encryption using DES and AES. (Note: you will *write your own program* as explained below, even though the JCE already provides this functionality.)
 - The JCE does not provide a direct way to access the DES or AES block ciphers. (Instead, it only supports calls for doing encryption using these block ciphers.) However, you can access the DES block cipher via:

```
Cipher DEScipher = Cipher.getInstance("DES/ECB/NoPadding");
```

and similarly for AES. **Explain in 1–2 sentences why this gives access to the underlying block cipher.**

- Create a program called `keygen.java` that takes a single command-line argument (“-DES” or “-AES”) indicating the cipher to use. This program should generate a random key and write it to a file called `key.txt` in hexadecimal format. I want you to generate this key yourself using `SecureRandom`, not using the built-in method for generating cipher keys.¹

¹Recall that a DES key is 64 bits long, yet only 56 of these are random; the remainder are check bits. Make sure that you generate a *random* but valid DES key.

- Create a program `encrypt.java`. This program should take two command line arguments; the first (“-DES” or “-AES”) indicating the cipher, and the second (“-ECB”, “-CBC”, or “-CTR”) indicating the mode. This program should read a key from the hex file `key.txt` and a plaintext from the ASCII file `msg.txt`, and output a ciphertext to the hex file `ctext.txt`. It should output an error if the file length (in bits) is not a multiple of block length of the cipher being used.
- Create a third program `decrypt.java` that takes the same command-line arguments as above, and recovers the plaintext given the key and the ciphertext.

After you have completed the above, please answer the following questions:

- (a) How long (in bits) is the ciphertext you generate when using DES in each of the 3 modes you implemented, as a function of the length of the plaintext? What about when using AES?
- (b) Compute the fraction of 0’s in the keys generated by your `keygen.java` program.² Generate 1000 keys and compute the average fraction of 0s across all these keys. How do the results compare to what you would expect if your key was truly generated at random?
- (c) Now run a simple statistical test on *ciphertexts*. Specifically, encrypt a plaintext file consisting of 6400 A’s and compute the fraction of 0s in the ciphertext; repeat this 1000 times (with a fresh key every time) and plot the frequency with which the fraction of 0s in the ciphertext is < 5%, 5–15%, . . . , 85–95%, > 95%. Do this for both DES and AES, in both ECB and CBC mode. Explain your results. Do they indicate a weakness in any of the ciphers/encryption modes?
- (d) Consider encrypting the following block of text:

The following files are available: AA1, top secret; A4, top secret; B5, unclassified; Iraq.txt, top secret; DC, top secret; end.

(The text has exactly 128 ASCII characters.) What could an eavesdropping adversary learn if this text were encrypted using DES in ECB mode? What about CBC mode? (Feel free to encrypt it yourself to help answer this question.)

3. Consider the following authentication protocol between two parties Alice and Bob who share a key k in advance. (Note: we did not yet cover authentication protocols in detail. For this problem, the level of security we are looking for is that an adversary should be unable to impersonate Alice to Bob, even after eavesdropping on multiple executions of the protocol between the two parties.)
 - (a) Bob chooses a random value $r \in \{0, 1\}^{128}$ and sends it to Alice.
 - (b) Alice computes $c \leftarrow E_k(r)$ and sends c to Bob.
 - (c) Bob computes $r' = D_k(c)$ and accepts if and only if $r' = r$.

Answer the following questions:

²Note that when checking a DES key, you should ignore the parity-check bits and only look at the random 56-bit portion of the key.

- (a) Show an encryption scheme that is secure against chosen-plaintext attacks, but would lead to an insecure protocol if plugged into the above.
- (b) Show an encryption scheme that is not secure against chosen-plaintext attacks, but would lead to a secure protocol if plugged into the above.
- (c) What is the “right” primitive to use in this setting? Suggest how to design a secure variant of the above protocol using this primitive.