## Finite state machines: flip-flop

Flip-flop can be modeled as a finite-state machine


D flip-flop
State: 1 bit (q)
Input: 1 bit (D)
Output: current state (z)

| q | D | $\mathrm{q}^{+}$ | z | T |
| :---: | :---: | :---: | :---: | :---: |
| 0 | 0 | 0 | 0 | 0 |
| 0 | 1 | 1 | 0 | 1 |
| 1 | 0 | 0 | 1 | 1 |
| 1 | 1 | 1 | 1 | 0 |

In state 0:
input 0 gives new state 0 (reset) input 1 gives new state 1 (set)

In state 1:
input 0 gives new state 0 (reset) input 1 gives new state 1 (set)

Could implement this in the obvious way with a D flip-flop, or use a T flip-flop!

Finite state machines: flip-flop
T flip-flop:


State: 1 bit (q) Input: 1 bit (T)
Output: current state (z)

| q | T | $\mathrm{q}^{+}$ | z | D |
| :---: | :---: | :---: | :---: | :---: |
| 0 | 0 | 0 | 0 | 0 |
| 0 | 1 | 1 | 0 | 1 |
| 1 | 0 | 1 | 1 | 1 |
| 1 | 1 | 0 | 1 | 0 |

In state 0:
In state 1:
input 0 gives new state 0 (hold) input 1 gives new state 1 (toggle)
input 0 gives new state 1 (hold) input 1 gives new state 0 (toggle)

Note that we can implement either type of flip-flop with the other type and some combinational circuit

Finite state machines: flip-flop
JK flip-flop:


State: 1 bit (q) Input: 2 bits (JK)
Output: current state (z)

| q | J | K | $\mathrm{q}^{+}$ | $\mathbf{z}$ |  |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 0 | 0 | 0 | 0 | 0 | hold |
| 0 | 0 | 1 | 0 | 0 | reset |
| 0 | 1 | 0 | 1 | 0 | set |
| 0 | 1 | 1 | 1 | 0 | toggle |
| 1 | 0 | 0 | 1 | 1 | hold |
| 1 | 0 | 1 | 0 | 1 | reset |
| 1 | 1 | 0 | 1 | 1 | set |
| 1 | 1 | 1 | 0 | 1 | toggle |

Input is $\mathbf{2}$ bits, so there are $\mathbf{4}$ outgoing arcs from each state, but $\mathbf{2}$ pairs are equivalent This can be implemented with either a T or D flip-flop

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