CMSC 430
Homeworks 1 and 2

For homework 1, do problems 1-6. Homework 2 will be assigned toward the end of February after we have discussed LALR grammars.

1. Describe the languages denoted by the following regular expressions:
   (a) $(0(0|1)*)0$
   (b) $((\varepsilon(0|1)*)*)$
   (c) $(0|1)^*0(0|1)(0|1)$

2. Write regular expressions for the following languages:
   (a) All strings of 0’s and 1’s that do not contain the substring 011.
   (b) All strings of 0’s and 1’s that do not contain the subsequence 011.

3. For the regular expressions $(a|b)^*$ and $(a^*|b^*)^*$:
   (a) Construct an NFA using Thompson’s construction algorithm
   (b) Show the sequence of moves in parsing "ababab"
   (c) Convert the NFA to a DFA using subset construction algorithm
   (d) Minimize the DFA using the partitioning algorithm

4. Write a grammar for the following language. Are the grammars ambiguous?:
   (a) All strings of 0’s and 1’s that have the same number of 0’s and 1’s.
   (b) All strings of 0’s and 1’s that have more 0’s than 1’s.
   (c) All balanced pairs of left and right parentheses (e.g., "()", "((()))").

5. Consider the grammar
   $S ::= (L) | a$
   $L ::= L, S | S$
   For each of the following strings "(a,a)" and "(a,(a,a))"
   (a) Find the parse tree
   (b) Find the leftmost derivation
   (c) Find the rightmost derivation

6. Consider the grammar
   $S ::= aSbS | bSaS | \varepsilon$
   (a) Show grammar is ambiguous by constructing two leftmost derivations for "abab"
   (b) Show grammar is ambiguous by constructing two rightmost derivations for "abab"

7. Consider the grammar
   $S ::= (L) | a$
   $L ::= L, S | S$
   (a) Eliminate left recursion from the grammar
   (b) Build a non-backtracking recursive descent parser, given the following code:

   ```
   tok; // current token
   match(x) { // matches token
     if (tok != x) // if wrong token
       error(); // exit with error
       tok = getToken(); // get new token
   }

   parser() {
     tok = getToken(); // initialize
     S(); // start symbol
     match("\$"); // match EOF
   }
   (c) Show an example parse of the string "(a,a)"

8. Consider the grammar
   $S ::= AS | b$
   $A ::= SA | a$
   (a) Construct the set of LR(0) items for the grammar
   (b) Construct the set of LR(1) items for the grammar
(c) Construct the LR(1) action/goto tables for the grammar

(d) List any shift/reduce or reduce/reduce conflicts. What is the effect if we always shift for a shift/reduce conflict? What is the effect if we always reduce for a shift/reduce conflict?

(e) Show an example parse of the string "abab"

9. Consider the grammar
\[ S ::= Aa | bAc | Bc | bBa \]
\[ A ::= d \]
\[ B ::= d \]

(a) Show that the grammar is not LALR(1)

10. Consider the following grammar, which generates expressions formed by applying "+" to integer and floating point constants. When two integers are added, the result is integer, otherwise, it is a float.
\[ E ::= E + T \mid T \]
\[ T ::= \text{num} \mid . \text{num} \]

(a) Give a syntax-directed definition to determine the type of each subexpression. Assign each symbol an attribute "type".
(b) Derive a parse tree for the expression "5 + 4 + 3.2 + 1". Annotate the parse tree, showing the computation of the "type" attribute for each grammar symbol.

12. Consider the following grammar, which generates expressions for a number of operators. Suppose the type of each operator is a range of integers.
\[ E ::= E + E \mid E * E \mid ... \]

(a) Write the type-checking rules which calculates the range for each subexpression.

13. Consider the following lexically nested C code:

```c
int a, b;
int foo() { int a, c; }
int bar() { int a, d; /* HERE */ }
```

(a) How can symbol tables represent the state of each scope at the point marked HERE? Draw a diagram.
(b) What symbols are visible/not visible at point HERE?

14. Translate the arithmetic expression
\[ a * - (b + c) \]

into

(a) a syntax tree
(b) postfix notation
(c) 3-address code
(d) stack code

11. Given the following C declarations:

```c
typedef struct {
    int a, b;
} CELL, *PCELL;
CELL foo[100];
PCELL bar(int x, CELL y) { ... }
```

(a) write the type expression for "foo"
(b) write the type expression for "bar"