Homework 4.1.

Suppose each player pretends this is a zero-sum game, and uses the minimax algorithm to compute a value for each node.

(a) What value will each player compute for each node?

(b) Does the above value equal the player’s maximin value, minimax value, or both?

(c) If the answer to (b) is “both”, then can you give an example of a perfect-information non-zero-sum game in which the maximin and minimax values differ?
Homework 4.2. Above is a game tree for a perfect-information zero-sum game. Run the alpha-beta algorithm on this game tree. At each node, write the intermediate and final values for alpha, beta, and \( v \).
Max’s utility:

Let $G$ be a perfect-information zero-sum game. At each node $x$ of the game tree, let $\text{negamax}(x)$ be the payoff for the player to move to $x$ if both players use their minimax strategies.

(a) Give a recursive formula for $\text{negamax}(x)$

(b) On the game tree above, put all of the $\text{negamax}$ values

(c) Modify the alpha-beta algorithm to return $\text{negamax}$ values instead of minimax values.

Homework 4.3. Let $G$ be a perfect-information zero-sum game. At each node $x$ of the game tree, let $\text{negamax}(x)$ be the payoff for the player to move to $x$ if both players use their minimax strategies.

(a) Give a recursive formula for $\text{negamax}(x)$

(b) On the game tree above, put all of the $\text{negamax}$ values

(c) Modify the alpha-beta algorithm to return $\text{negamax}$ values instead of minimax values.
**Homework 4.4.** At each node $x$, of the tree shown below, let $m(x)$ be $x$’s minimax value. Suppose Max uses an evaluation function $e(x)$ that returns $m(x)$ with probability 0.9, and $-m(x)$ with probability 0.1. At the root node, what is Max’s probability of correct decision if Max searches

(a) to depth 1?
(b) to depth 2?
(c) to depth 3?

Max’s utility: $\begin{array}{cccccccc} 1 & -1 & -1 & -1 & 1 & -1 & -1 & 1 \end{array}$