

1. Show that a square 3D orthonormal rotation matrix M has the inverse M^T , so $M^* M^T = I$. Use the properties of the matrix that, if rewritten as three column vectors $\mathbf{c1}$, $\mathbf{c2}$, $\mathbf{c3}$, we have $\mathbf{c1} \cdot \mathbf{c1} = 1$, $\mathbf{c2} \cdot \mathbf{c2} = 1$, $\mathbf{c3} \cdot \mathbf{c3} = 1$, and we have $\mathbf{c}_i \cdot \mathbf{c}_j = 0$ if $i \neq j$. These properties plus the basics of matrix multiplication are enough to complete the demonstration.

$$M = \begin{bmatrix} c1x & c2x & c3x \\ c1y & c2y & c3y \\ c1z & c2z & c3z \end{bmatrix} = [\mathbf{c1} \quad \mathbf{c2} \quad \mathbf{c3}]$$

2. Given the following scene:

Vertex at	(5,0,0)	with $k_d = 0.80$, $k_s = 0.70$, $k_a = 0.40$
Normal	(0,1,0)	
Light at	(1,5,0)	with $c_l = 100$, $p = s = 2$
Camera at	(10,4,1)	
Ambient light		with $c_a = 50$

- Compute the diffuse component c_d . Assume for (a), and the rest of question 2, the light is a point light but not attenuated by distance – compute the L vector as in the slides, before the section on lights.
- Compute the specular component by the Phong model (call this c_p , on slides called c). As part of this show your work on computing the R reflection vector.
- Compute the specular component by the Blinn model (call this c_b).
- Compare the results of the Phong and Blinn model. Are they close?
- Compute the ambient component, call this c_a .

3. With the scene above, recompute the diffuse component assuming

- The light is a point source. Now assume the light is attenuated by distance.
- The light is a spotlight with direction $\langle 3, -5, 0 \rangle$ and theta max 30 degrees.
- There is a directional light with direction $\langle 3, -5, 0 \rangle$.