

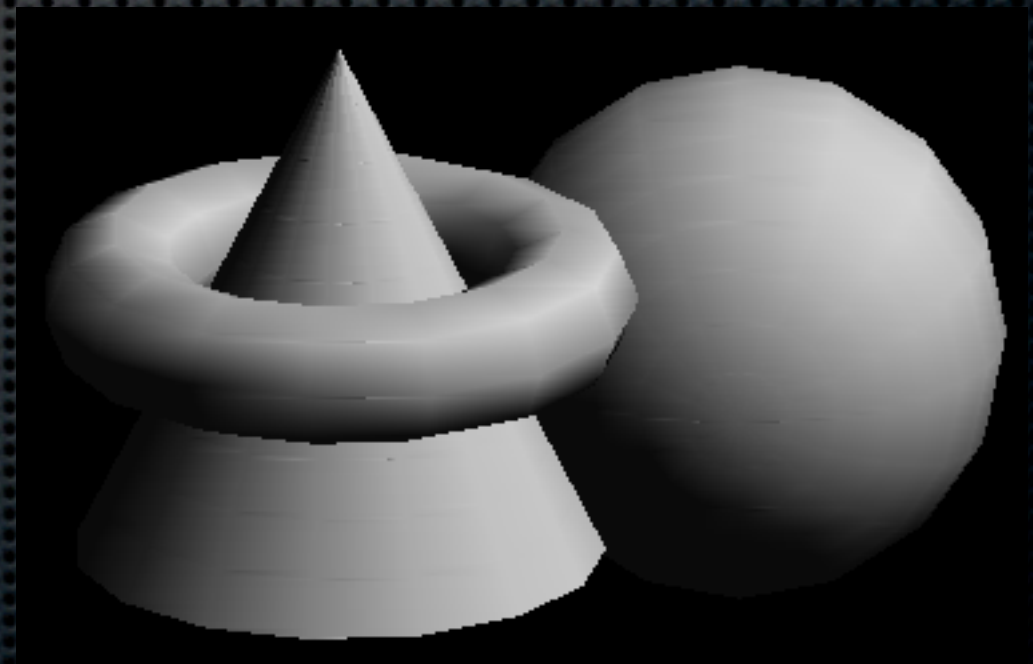
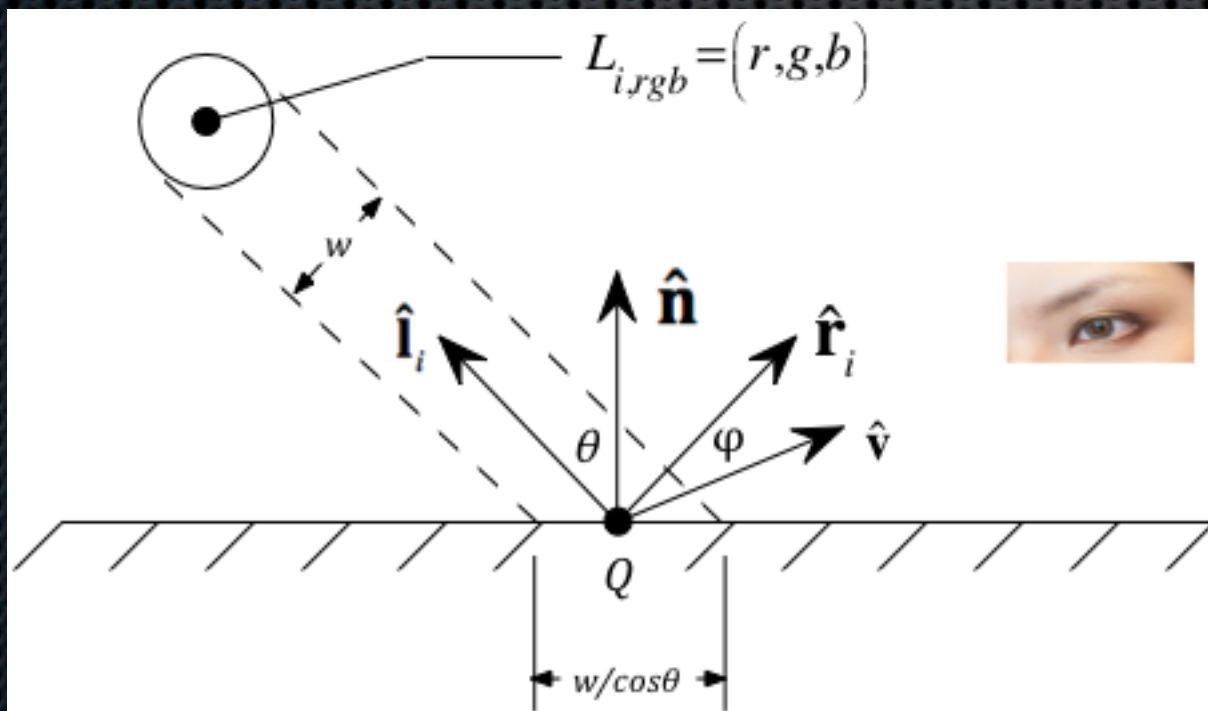
CMSC427 fall 2017

Global illumination – intro

Ray tracing and radiosity

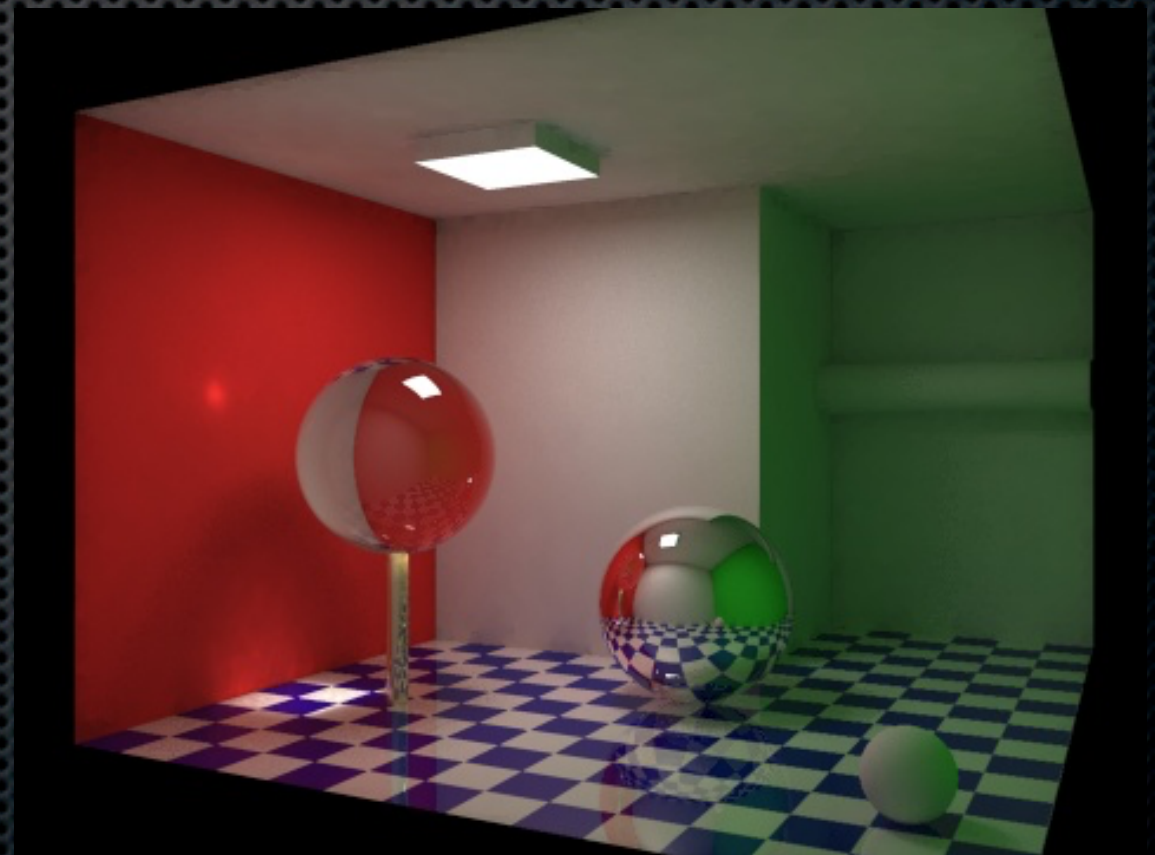
So far – local illumination

- One triangle, one light at a time
- Object rendering *into* image – what pixel sees me?
- Opaque surfaces
- No shadows, no crosstalk between facets



Now— global illumination +

- Scene oriented – consider all triangles and lights
- Image oriented rendering – what object can pixel see?
- Translucent and transparent surfaces, refraction
- Shadows, color bleeding



Ray Tracing and Radiosity

- General concepts
 - What advantages do they have?
 - How can you spot a ray-traced or radiosity image?
- How they work
 - Ray tracing overview
 - Radiosity overview
- Other approaches: path tracing, ray marching

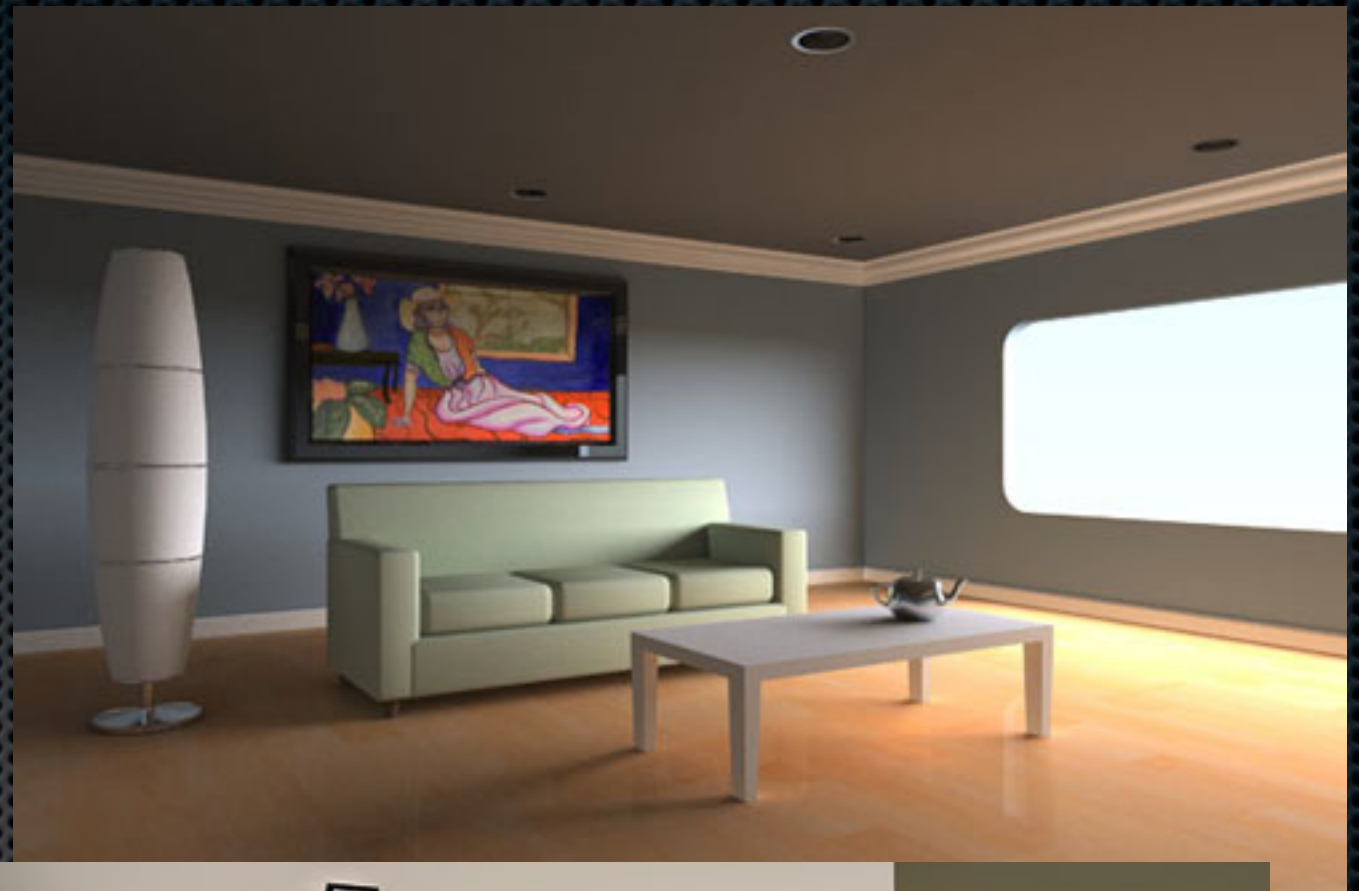
Ray tracing

- Reflections, refractions
- Sharp shadows
- Partial physical model
- Point lights
- Tracing single rays

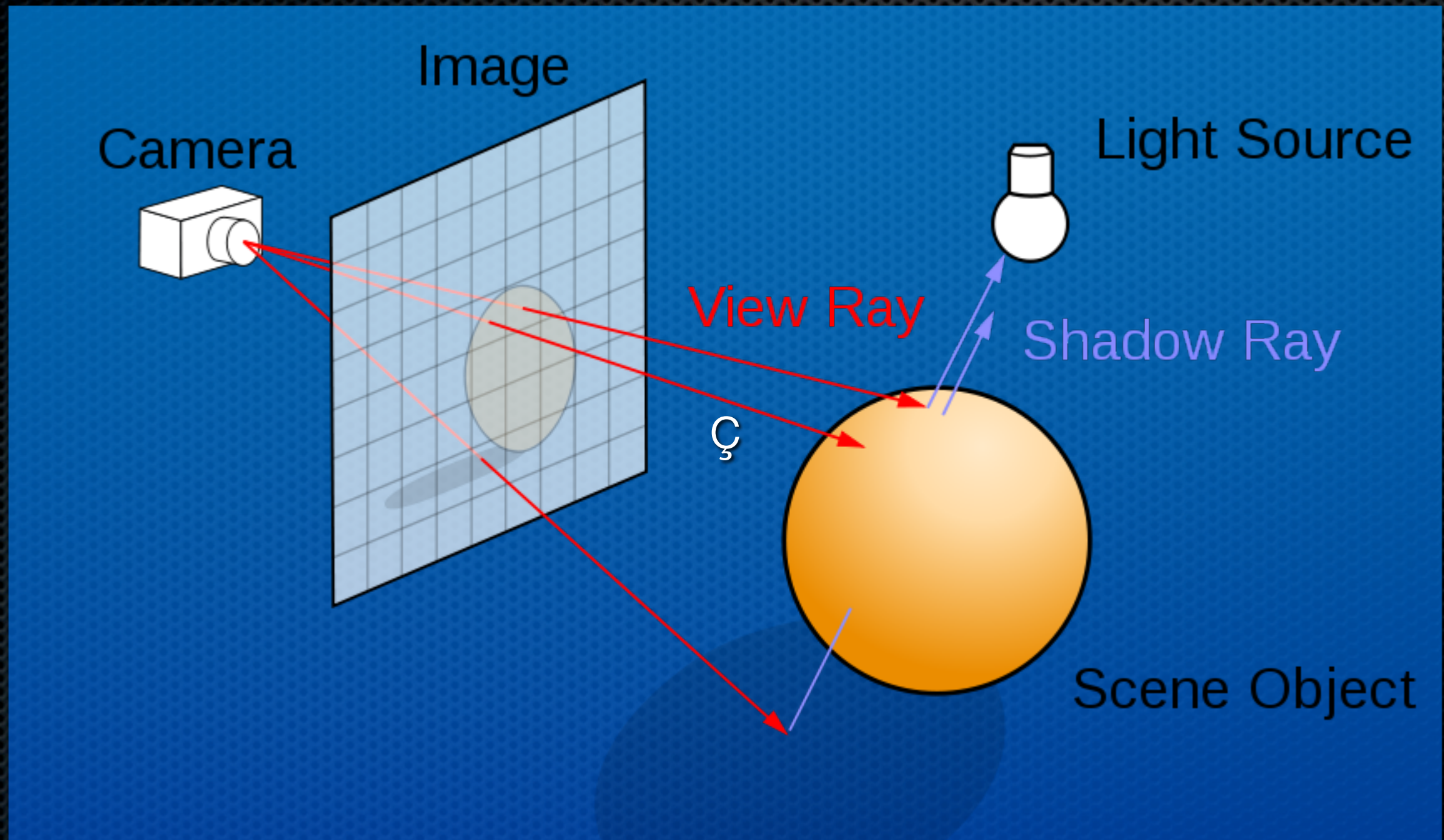


Radiosity

- Soft shadows
- Better physics
- Extended lights
- Integrating over extended areas



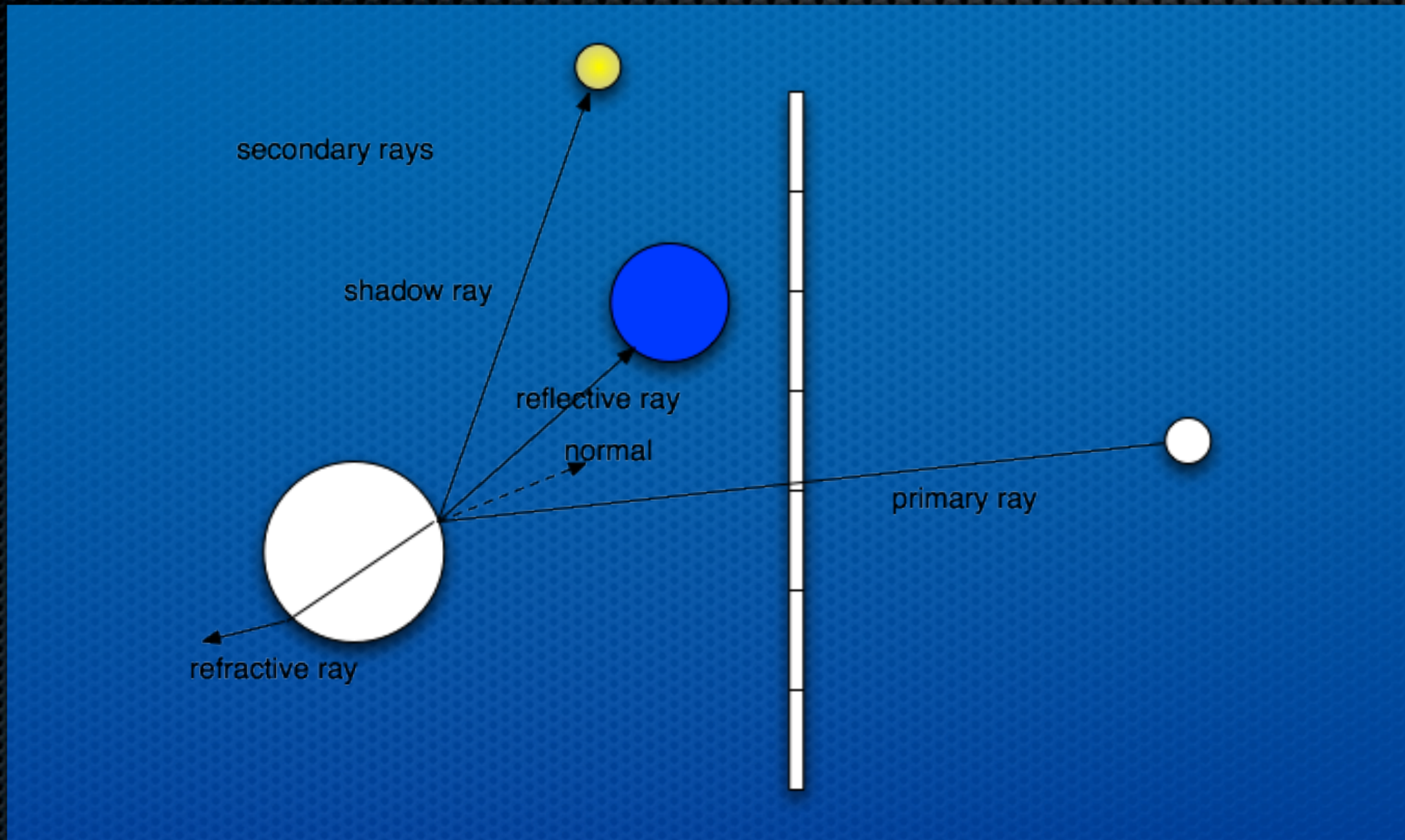
Ray tracing principles



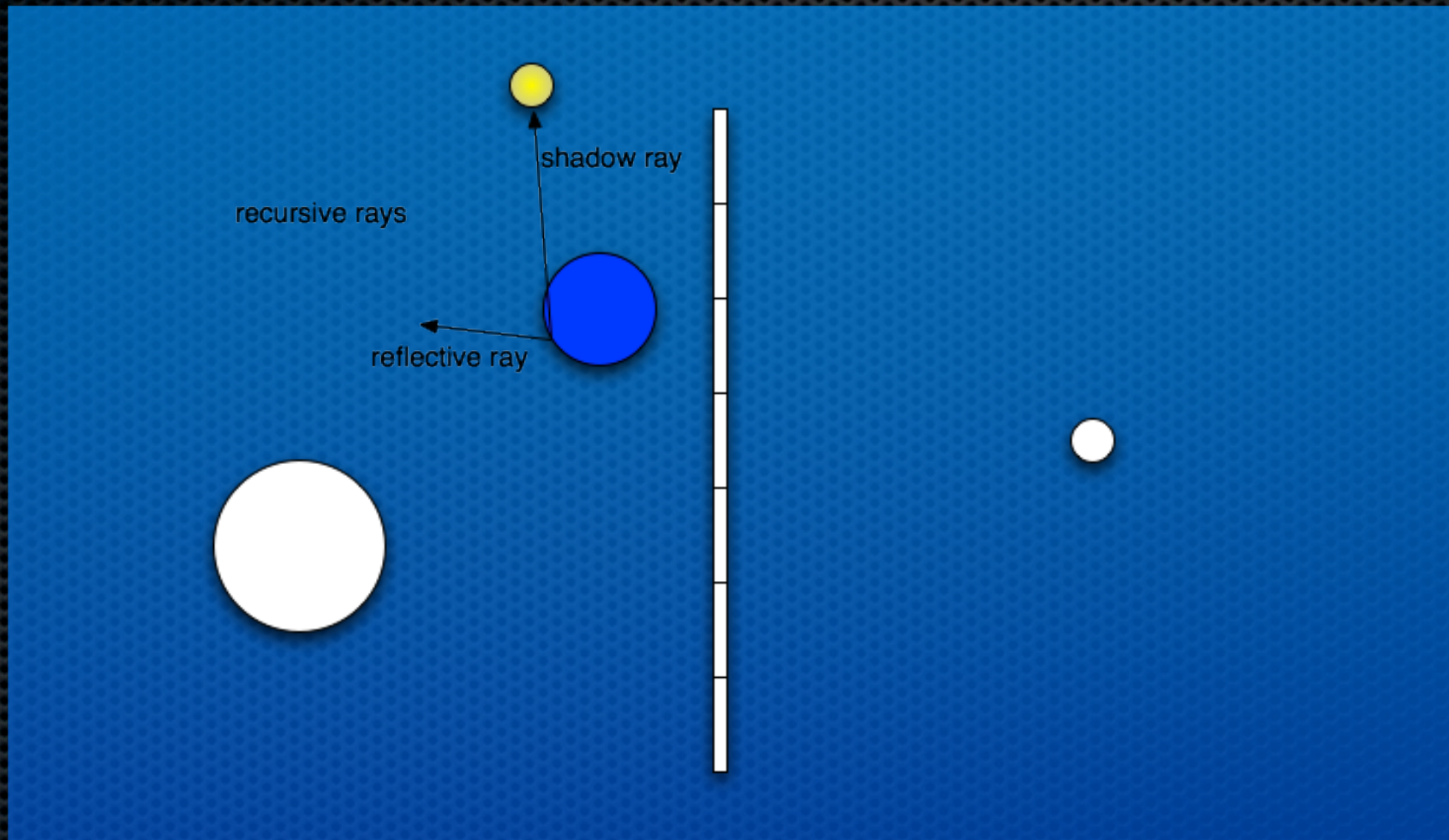
The Rays

- Concepts:
 - View (primary) ray
 - Secondary rays
 - Shadow ray (to all lights)
 - Reflection ray
 - Refraction ray

The rays again

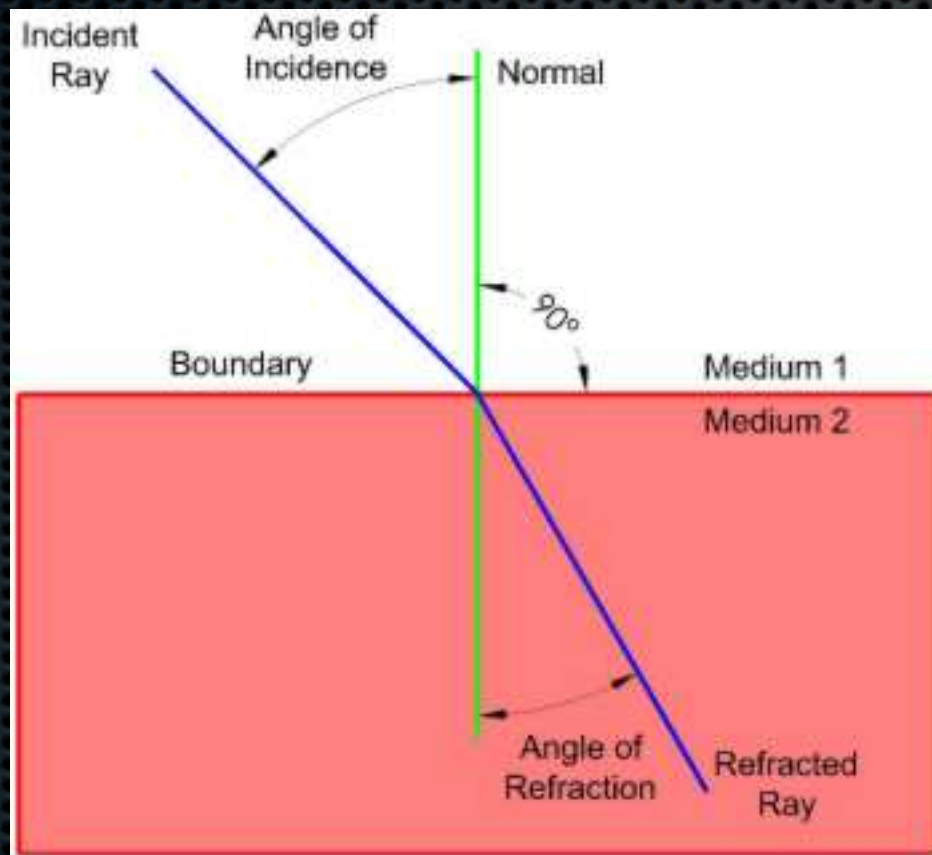


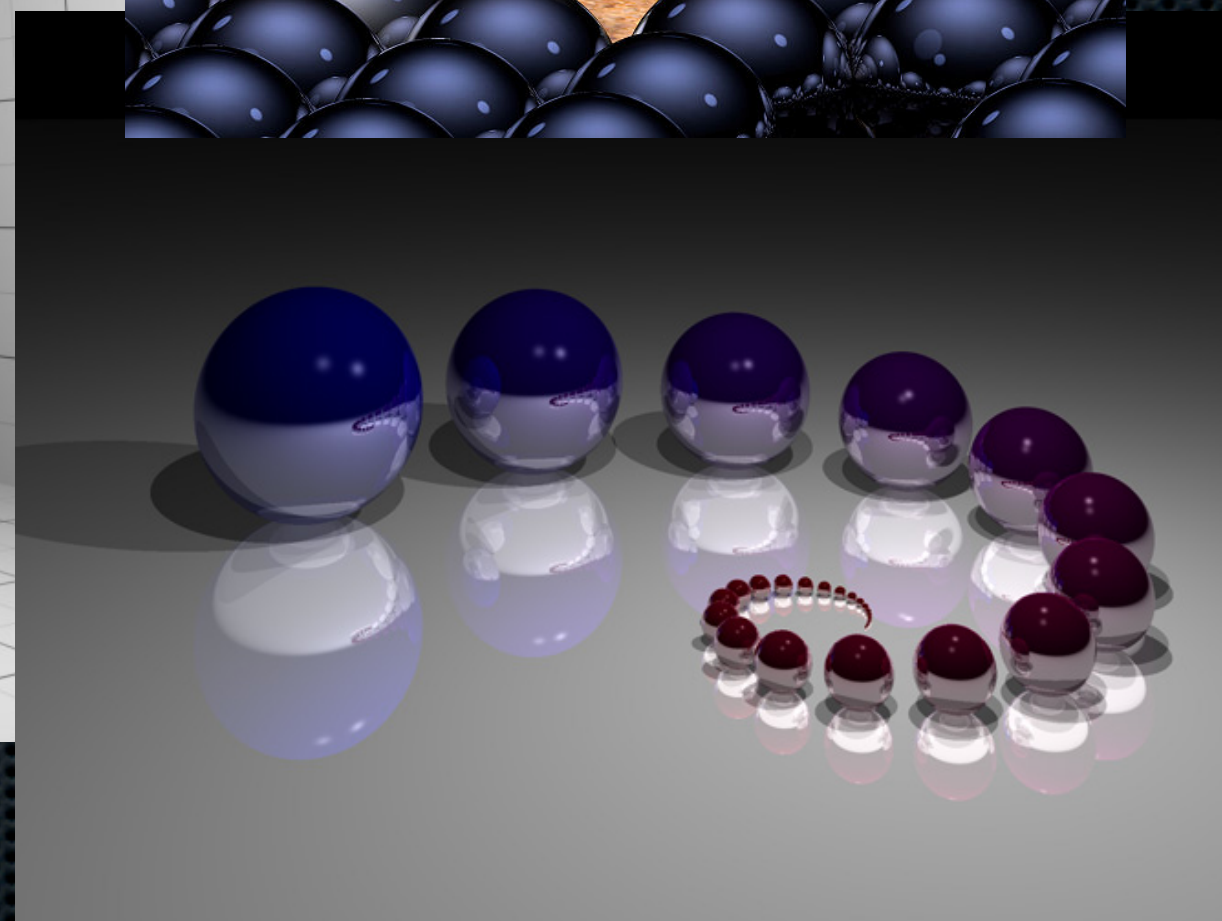
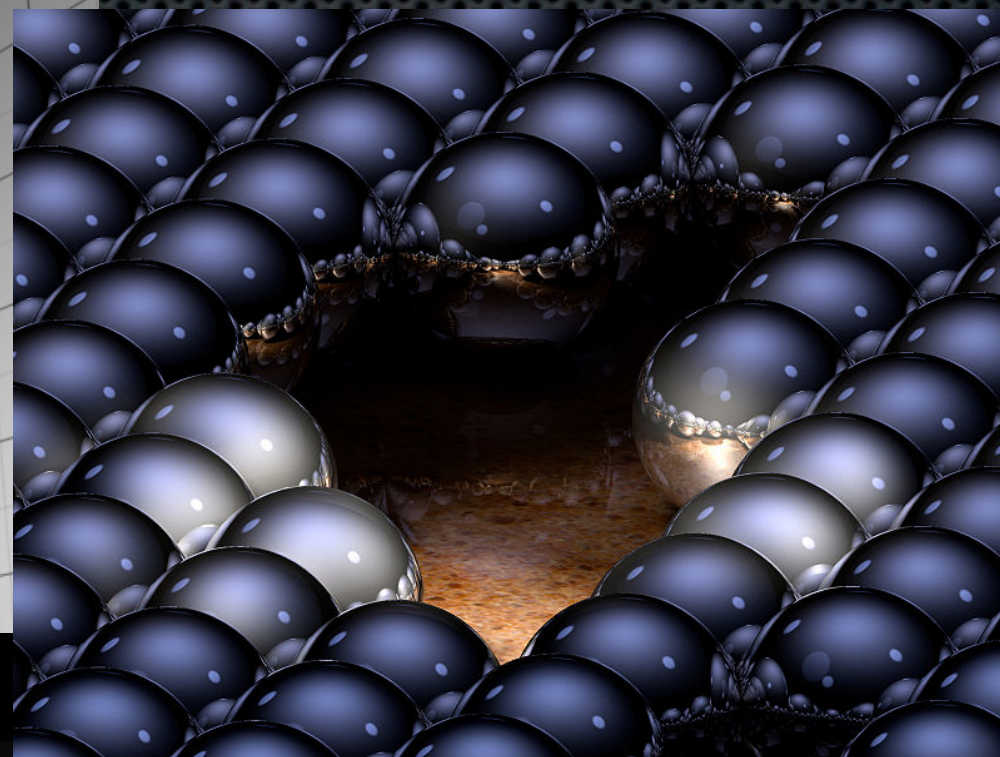
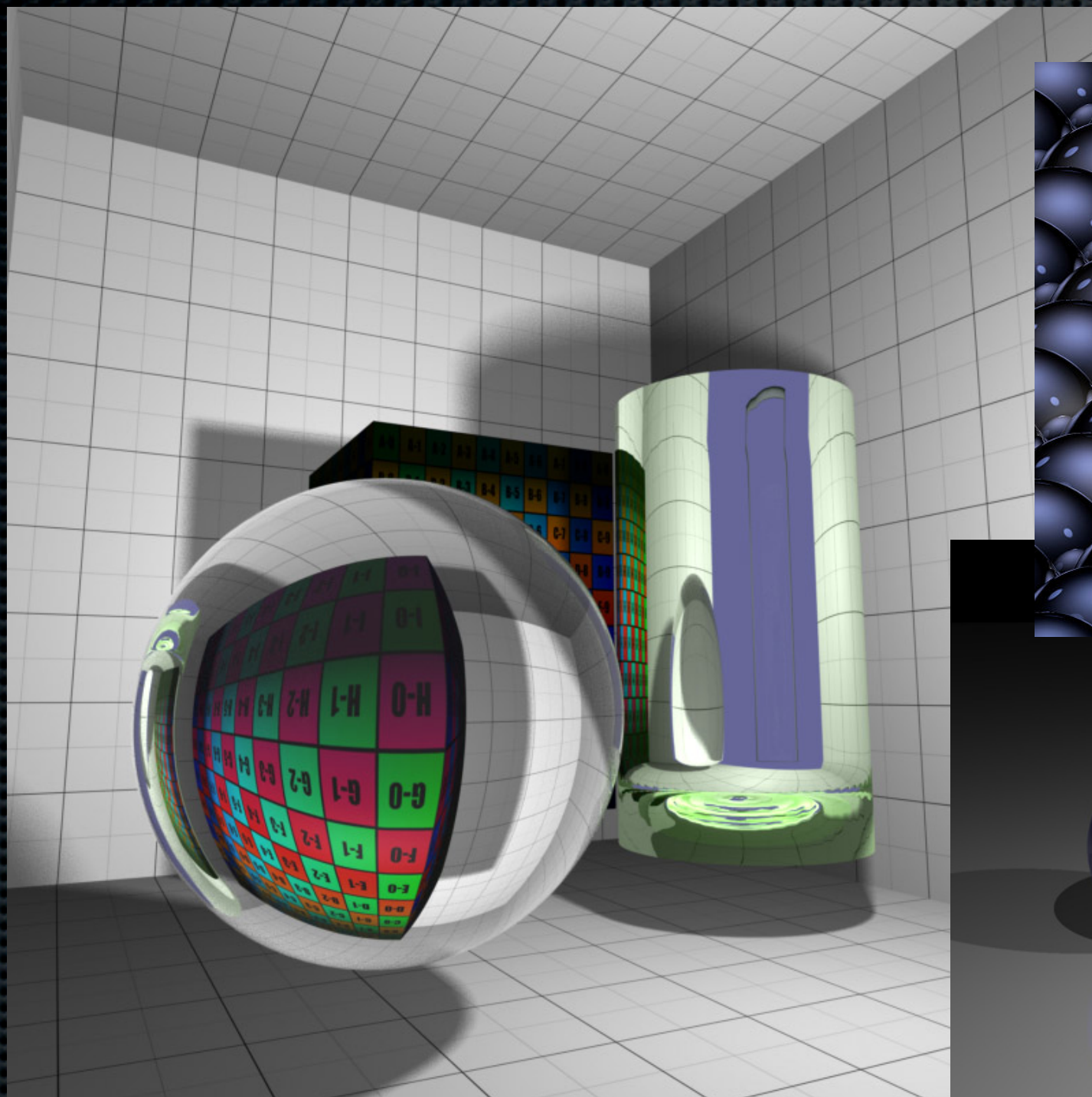
Recursive rays (rinse, repeat)



Refraction

- Depends on ratio of speed of light between two materials





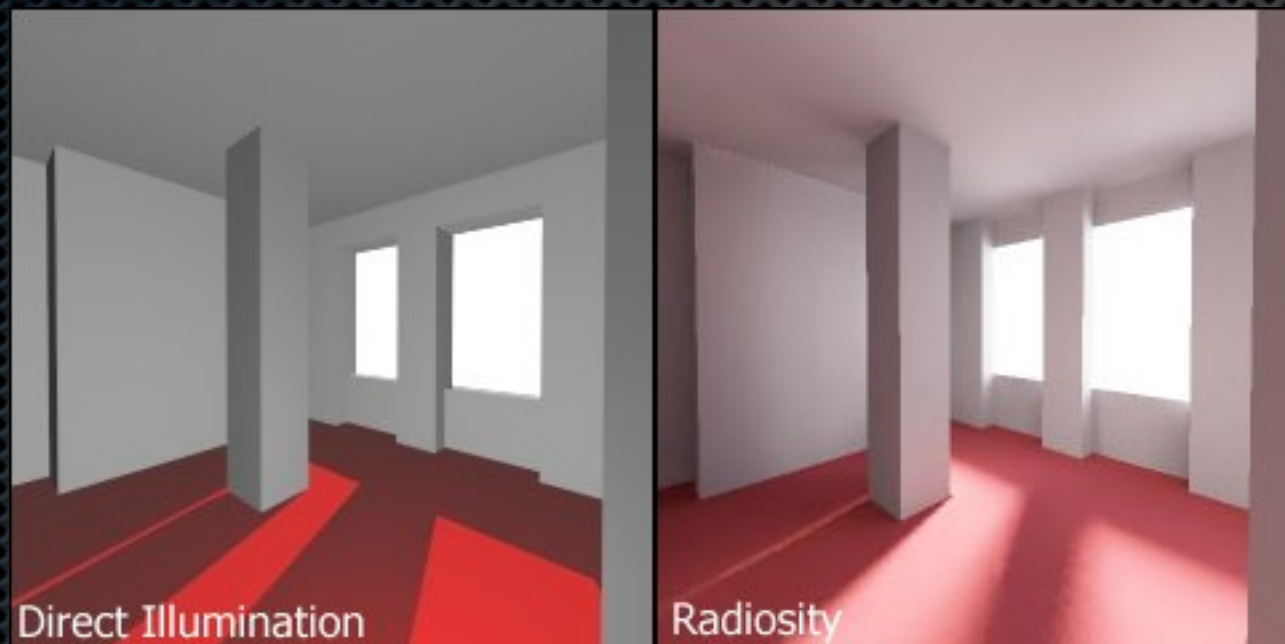


Tweaking ray tracing

- One is not enough
 - One primary ray can “barely” miss an object
 - Stochastic or random ray tracing
 - multiple, random primary rays out of a pixel
- Speeding it up
 - Speed up intersection calculations by data structure

Radiosity principles

- Global vs. local computations

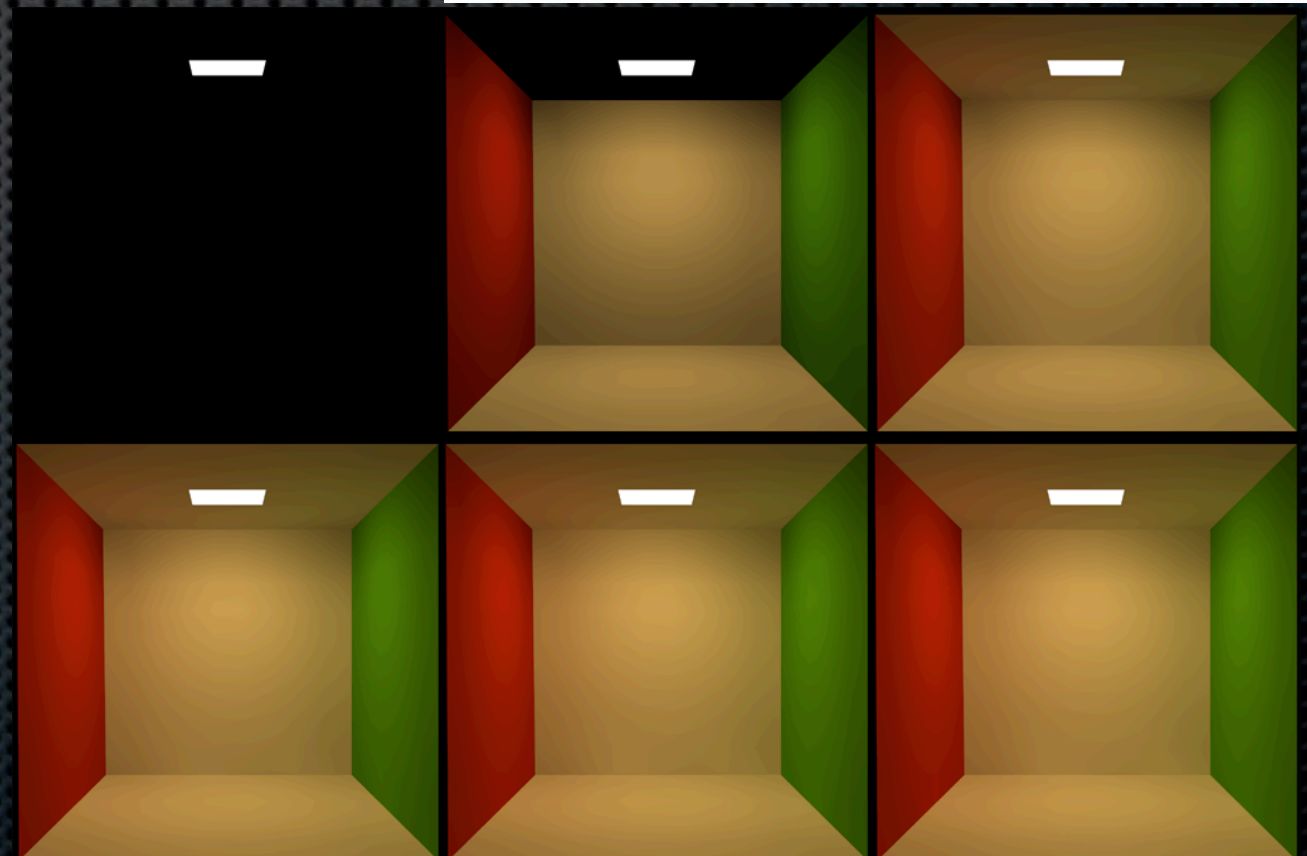
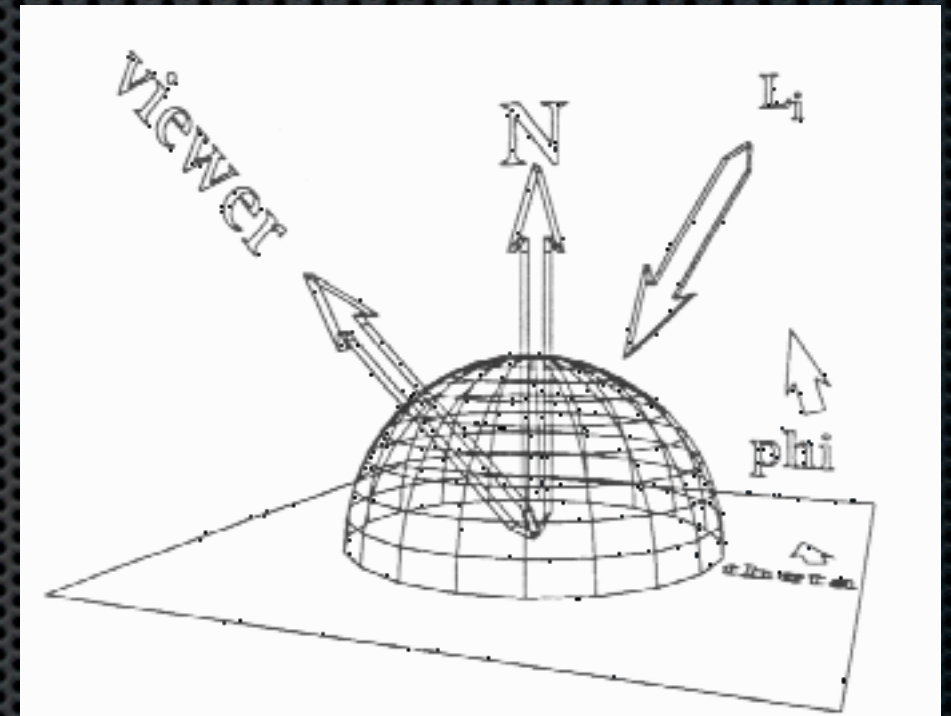


The Cornell box

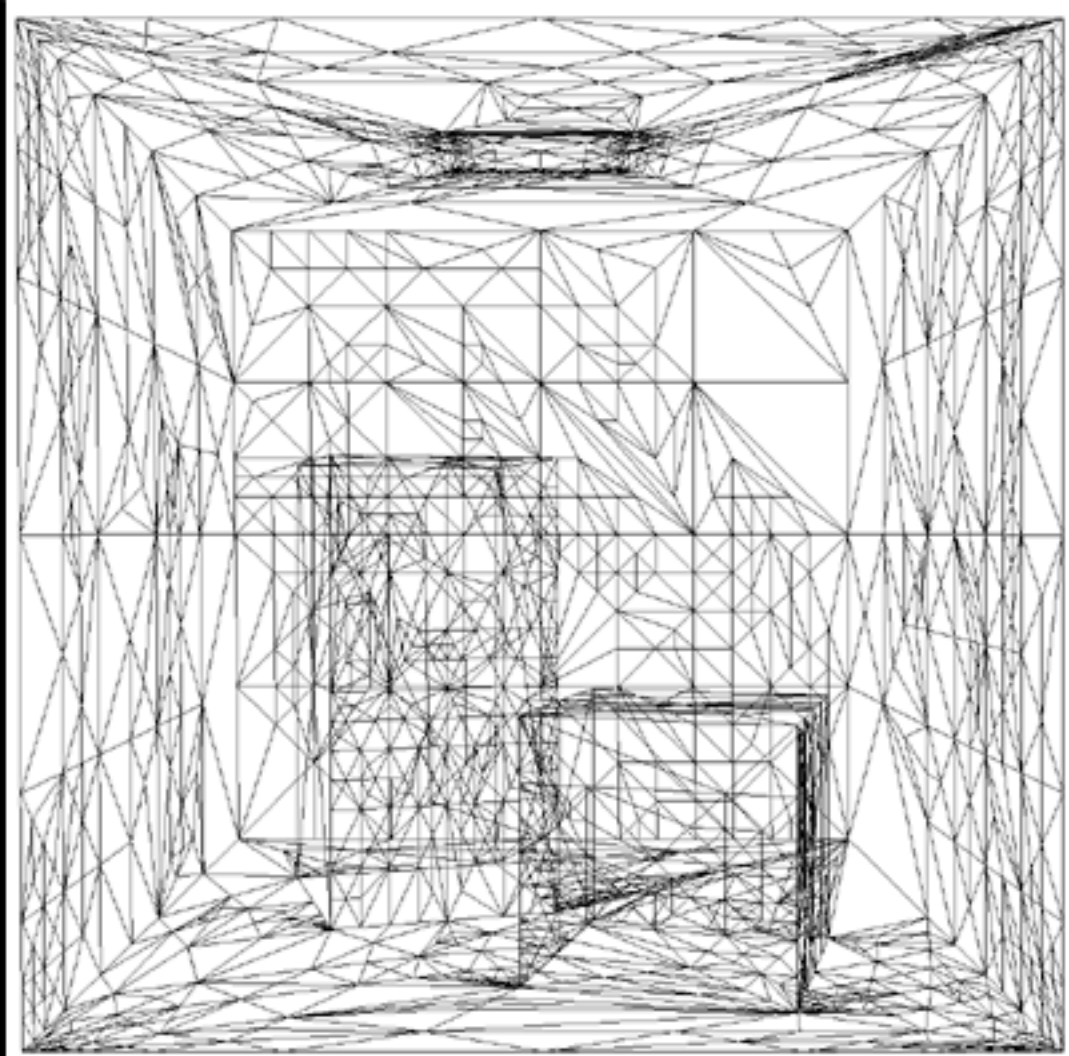


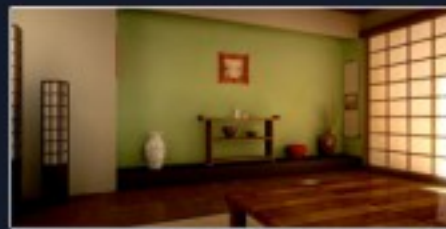
Radiosity vs. ray tracing

- Ray tracing - sample rays for each light, reflection and refraction
- Radiosity - integration over all rays on patch
- Iterate until light solutions are stable



Patch computations





Ray tracing details

- The basic recursive algorithm
- Casting the primary ray
- Intersecting with an object: sphere (circle), triangle
- Computing refraction ray

Ray tracing algorithm

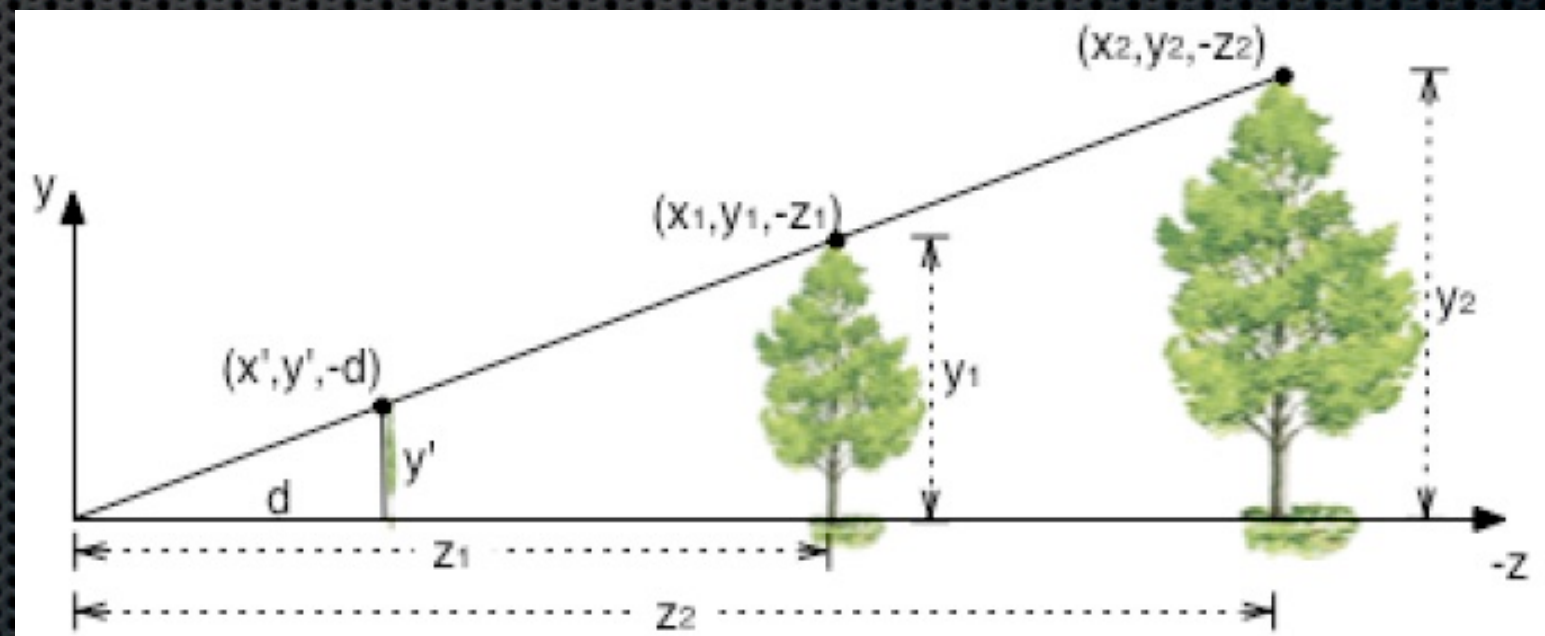
```
for (int j = 0; j < imageHeight; ++j) {  
    for (int i = 0; i < imageWidth; ++i) {  
        Ray primaryRay = new Ray(i,j);  
        color[i][j] = rayTrace(primaryRay,0);  
    }  
}
```

```
rayTrace(ray, generation)  
    if (generation > maxGen) return backgrdColor;  
    hitPt = intersect(ray, objectList);  
    if (hitPt == null) return backgroundColor;  
    c = accumulateLights(hitPt);  
    if (reflective(hitPt)) {  
        reflectRay = reflect(ray, hitPt)  
        c += trace(reflectRay) }  
    if (refractive(hitPt)) {  
        refractRay = refract(ray, hitPt)  
        c += trace(refractRay) }  
    return c
```


Casting first ray

$$p(t) = eye + t(imagePt - eye) \quad \text{with } t \text{ in } [0, \text{inf}]$$

imagePt is $(x', y', -d)$, eye is at origin



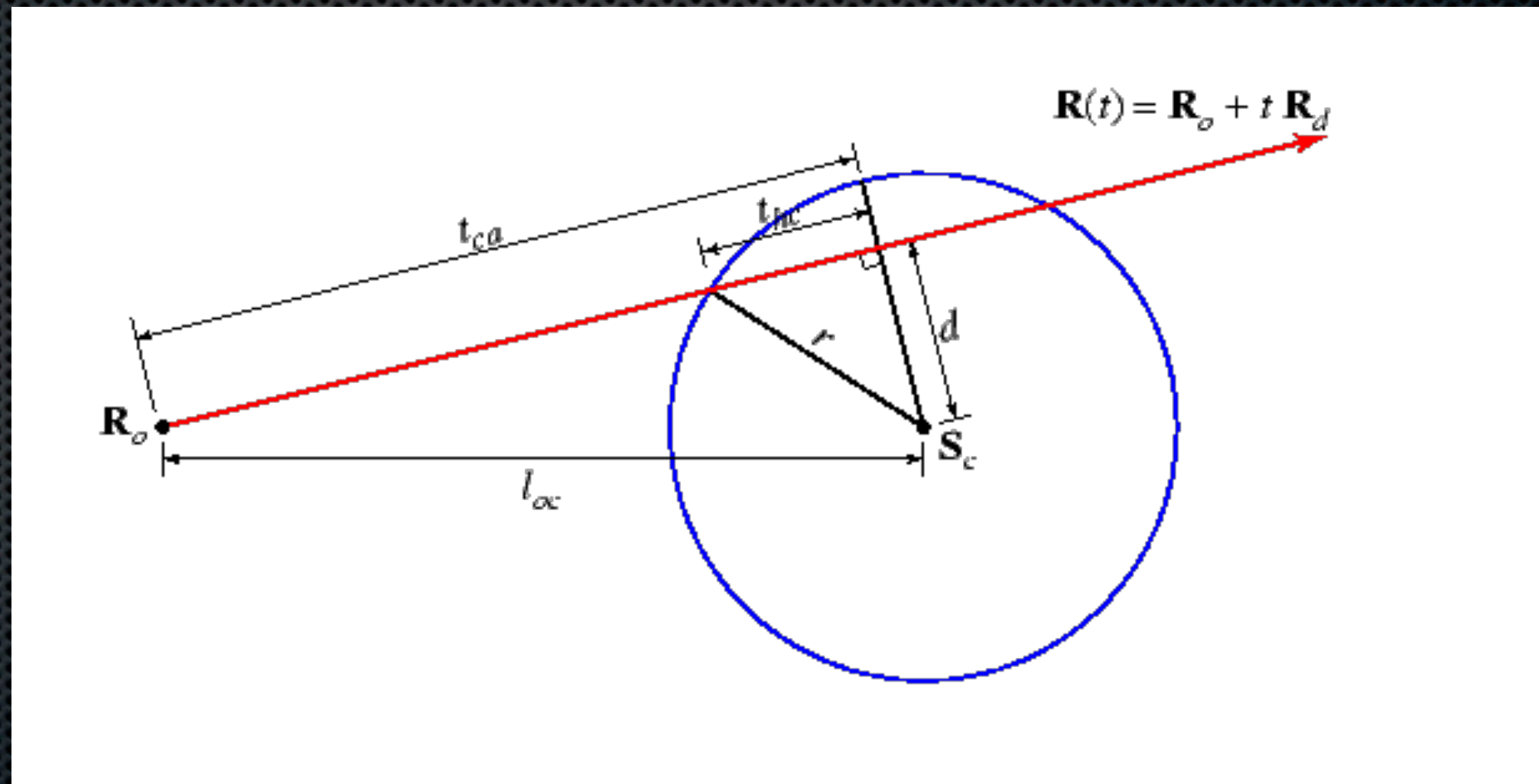
Intersecting with first object

For each object:

Compute hit time t when ray hits object

Find object with smallest t – that is hit point

**Spheres
are
easiest!**



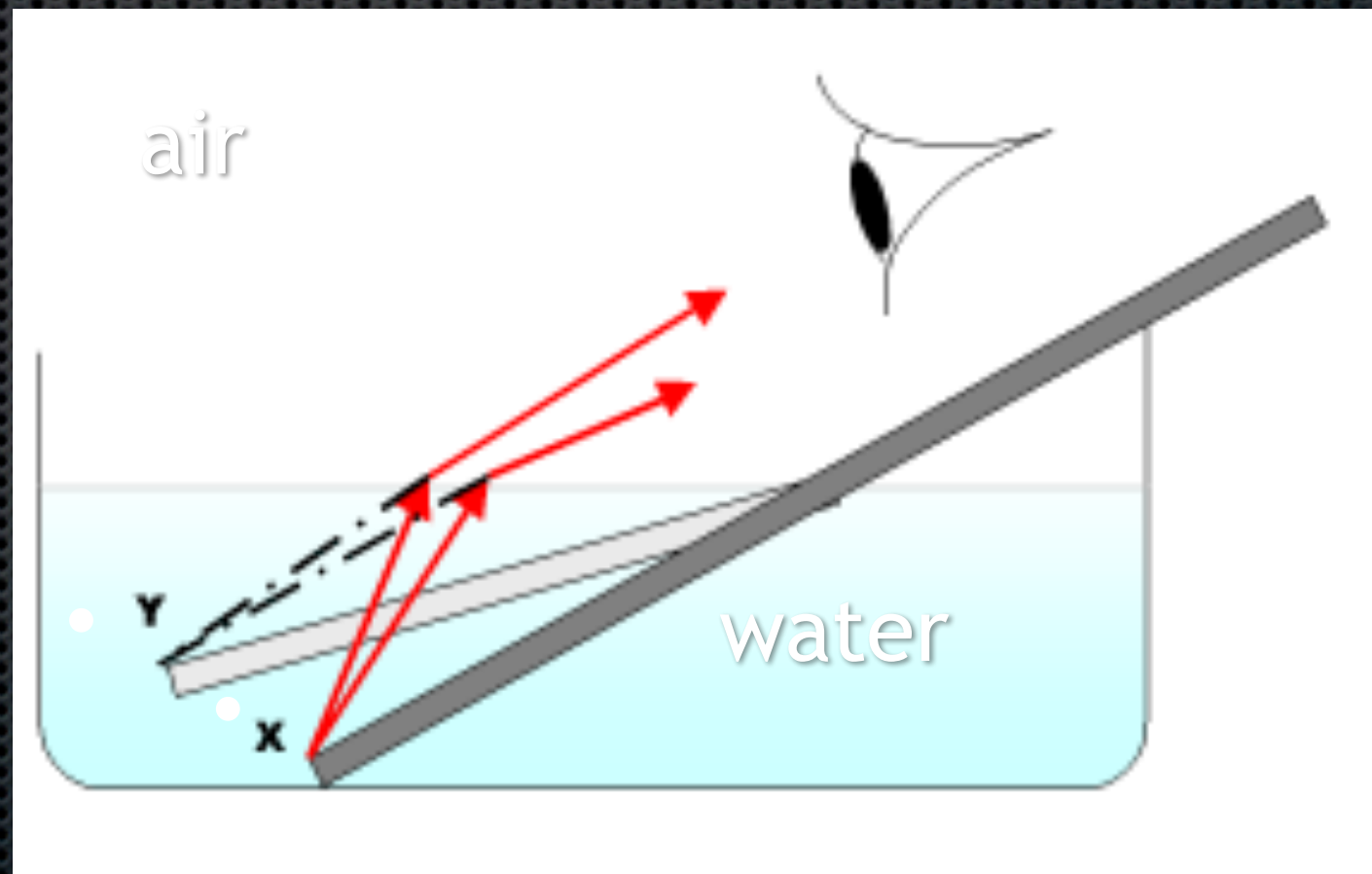
Reflection & refraction



Refraction

<http://en.wikipedia.org/wiki/Refraction>

- Light rays that travel from one medium to another are bent
- To the viewer, object at location x appears to be at location y



Index of refraction

http://en.wikipedia.org/wiki/Refractive_index

- Speed of light depends on medium
 - Speed of light in vacuum c
 - Speed of light in medium v
- Index of refraction $n=c/v$
 - Air 1.00029
 - Water 1.33
 - Acrylic glass 1.49
- “Change in phase velocity leads to bending of light rays”



Snell's law

http://en.wikipedia.org/wiki/Snell's_law

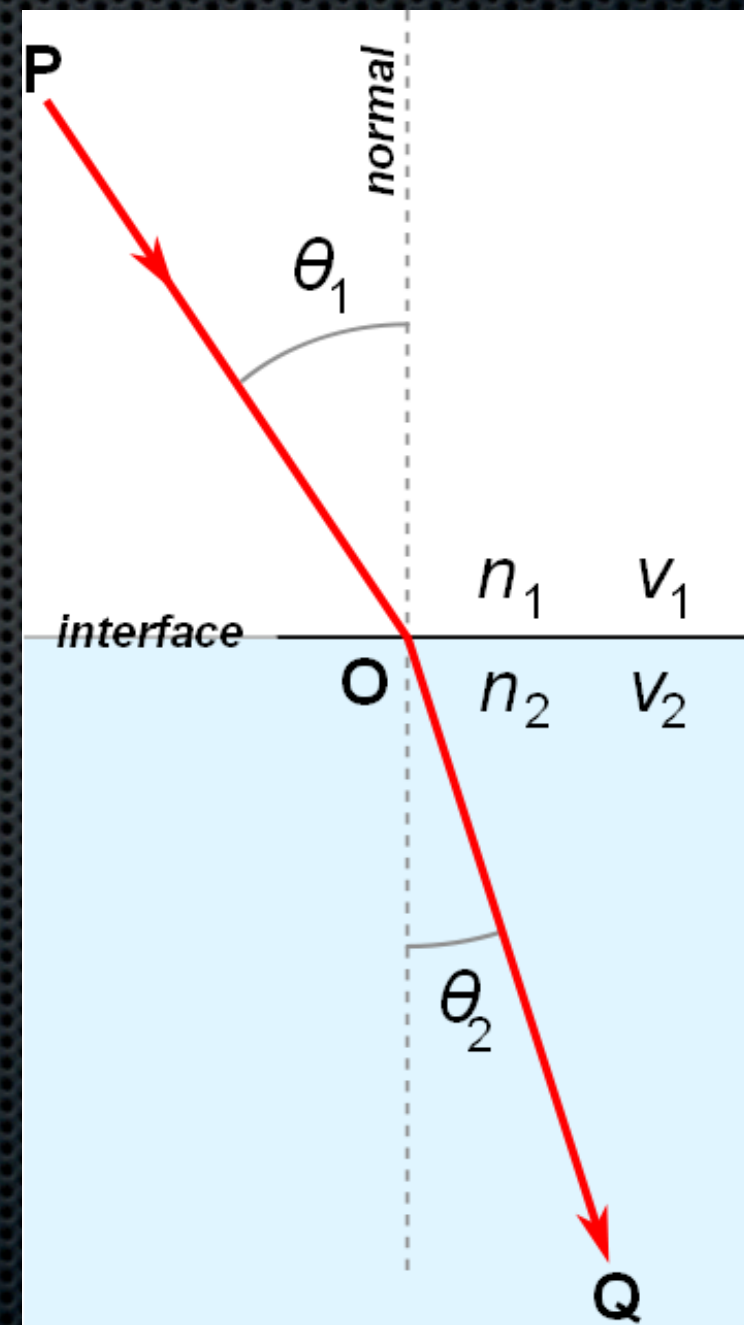
- Ratio of sines of angle of incidence θ_1 and refraction θ_2 is equal to opposite ratio of indices of refraction n_1, n_2

$$\frac{\sin \theta_1}{\sin \theta_2} = \frac{n_2}{n_1}$$

- Vector form in 3D

$$\mathbf{r} = \frac{n_1}{n_2} \mathbf{v} + \left(\frac{n_1}{n_2} \cos \theta_1 + \cos \theta_2 \right) \mathbf{n}$$

- Viewing, refracted direction \mathbf{v}, \mathbf{r} (P,Q)
- Normal vector \mathbf{n}



Total internal reflection

http://en.wikipedia.org/wiki/Total_internal_reflection

- Angle of refracted ray

$$\theta_2 = \arcsin \left(\theta_1 \frac{n_1}{n_2} \right)$$

- Critical angle

$$\theta_c = \frac{n_2}{n_1}$$



- If $\theta_1 = \theta_c$ we get $\theta_2 = \pi/2$ refracted ray is parallel to interface
- If $\theta_1 > \theta_c$ we have total internal reflection (light ray does not cross interface between media)

Fresnel equations

- Fresnel equations are relatively complex to evaluate
- In graphics, often use Schlick's approximation
https://en.wikipedia.org/wiki/Schlick%27s_approximation
- Ratio F between reflected and refracted light
- Indices of refraction n_1, n_2

$$F = f + (1 - f)(1 - \mathbf{v} \cdot \mathbf{n})^5$$

$$f = \frac{\left(1.0 - \frac{n_1}{n_2}\right)^2}{\left(1.0 + \frac{n_1}{n_2}\right)^2}$$

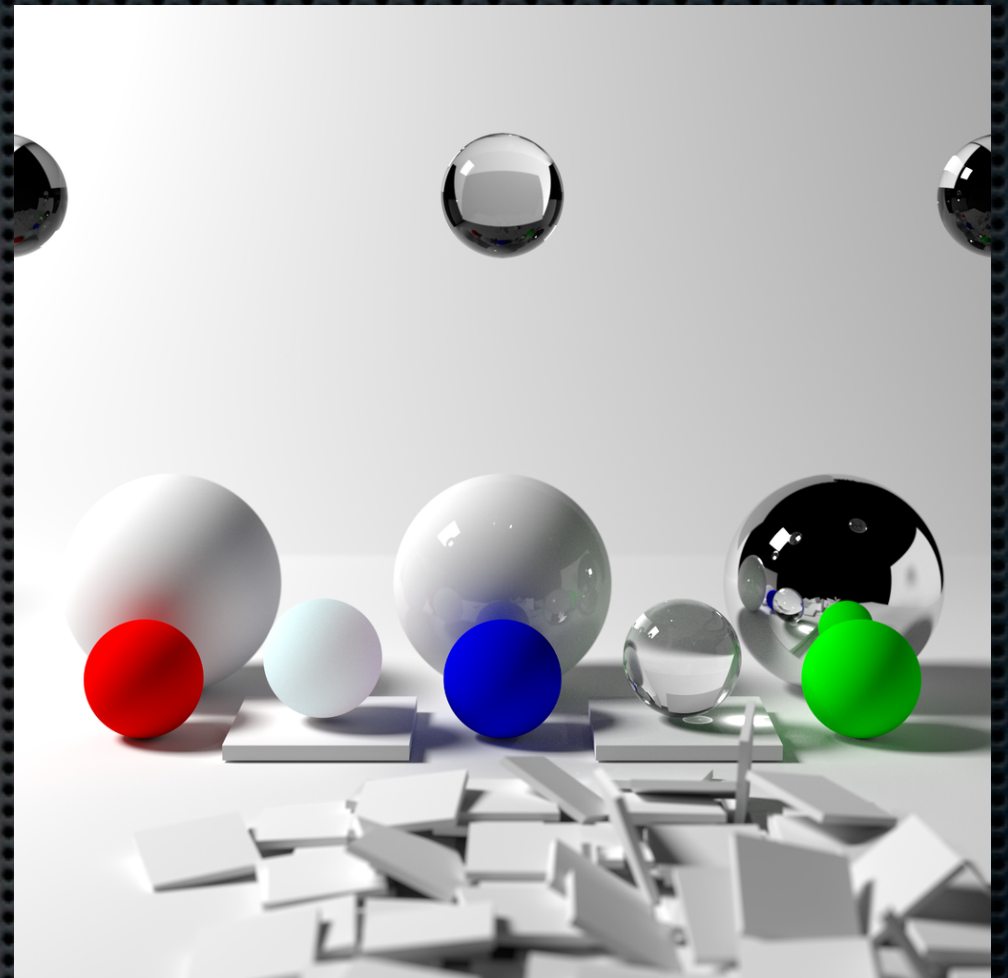
Newer algorithms

- Path tracing

- A multisampled, randomized version of ray tracing to approx. radiosity

- Ray marching

- A “binary search” approach to finding the hit point for complex shapes when no closed form exists



This image is ...?

