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**Total points: 100. Total time: 115 minutes. 6 problems over 6 pages. No book, notes, or calculator**

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Unless stated otherwise, the following conventions are used:

- $K\{X\}$  denotes  $X$  encrypted with secret key  $K$  (e.g., DES-CBC)
  - Passive attacker: can only eavesdrop.
  - Active attacker: can intercept messages and send messages with another's sender id.
  - Server handles at most one client at a time
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**1. [10 points]**

Company xLtd has principals  $X, A_1, A_2, \dots$ , where  $X$  issues certificates for the  $A_i$ 's, and is their trust anchor.

Company yLtd has principals  $Y, B_1, B_2, \dots$ , where  $Y$  issues certificates for the  $B_i$ 's, and is their trust anchor.

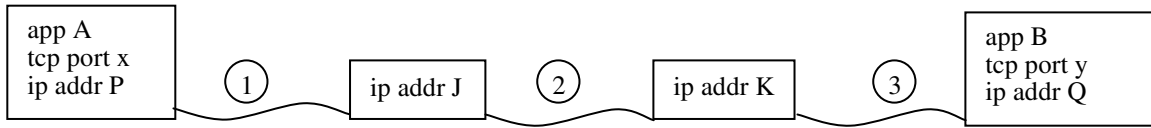
One day, xLtd acquires yLtd. You are to obtain a new PKI for the new xLtd. Parts a and b are independent.

- a. Modify the old PKIs to obtain a new PKI in which  $X$  is the sole trust anchor for all  $A_i$ 's and  $B_i$ 's; minimize the number of new certificates.
  - Give the certificate chain that  $A_1$  needs to get the public key of  $B_1$  in the new PKI.
  - Give the certificate chain that  $B_1$  needs to get the public key of  $A_1$  in the new PKI.
- b. Modify the old PKIs to obtain a new PKI in which  $X$  is the sole trust anchor for all  $A_i$ 's, and  $Y$  be the sole trust anchor for all  $B_i$ 's; minimize the number of new certificates.
  - Give the certificate chain that  $A_1$  needs to get the public key of  $B_1$  in the new PKI.
  - Give the certificate chain that  $B_1$  needs to get the public key of  $A_1$  in the new PKI.

**2. [20 points]**

Below, “structure of an IP packet” means its headers (IP, TCP, etc, up to payload) and the values of addresses, ports, SPIs.

- a. Applications A and B communicate over TCP over IP as shown, where J and K are intermediate IP routers. Give the structure of an IP packet from A to B at points 1, 2, and 3.



- b. The above configuration is now modified as follows: P and Q operate IPsec-AH with SPI of 11 (for both directions); J and K operate IPsec-AH with SPI of 22. Give the structure of an IP packet from A to B at points 1, 2, and 3.

3. [20 points]

A (client, has K)	B (server, has entry [A, K] )
<pre> send [A, B, conn]           // msg1  receive msg2 S<sub>B</sub> ← K{R<sub>B</sub>} generate random R<sub>A</sub> send [A, B, S<sub>B</sub>, R<sub>A</sub>]       // msg3  receive msg4 if S<sub>A</sub> = K{R<sub>A</sub>} then A authenticated else abort                     </pre>	<pre> receive msg1 generate random R<sub>B</sub> send [B, A, R<sub>B</sub>]           // msg2  receive msg3 if S<sub>B</sub> = K{R<sub>B</sub>} then A authenticated else abort S<sub>A</sub> ← K{R<sub>A</sub>} send [B, A, S<sub>A</sub>]           // msg4                      </pre> <p style="text-align: center;">←---- exchange data encrypted with session key = function(R<sub>A</sub>, R<sub>B</sub>, K) ----→ Close session</p>

A and B share a high-quality secret key K and periodically establish sessions as shown above.

Each part below defines a specific session key function and a question for a kind of attacker.

If you answer yes, give the attack, and if you answer no, explain briefly.

- If the session key is  $R_A + R_B$ , can a passive attacker decrypt the data exchanged in a session?
- If the session key is  $K\{R_A + R_B\}$ , can a passive attacker decrypt the data exchanged in a session?
- If the session key is  $K\{R_A \oplus R_B\}$ , can an active attacker decrypt the data exchanged in a session?
- If the session key is  $(K+1)\{R_A + R_B\}$ , can an active attacker decrypt the data exchanged in a session?

4. [15 points]

A (has pw)	B (has entry A:V)
<pre> obtain V from pw generate random a <math>T_A \leftarrow g^a \text{ mod-p}</math> send [A, B, V{<math>T_A</math>}] // msg1  receive msg2 <math>K_A \leftarrow (T_B)^a \text{ mod-p}</math> send[A,B, <math>K_A\{M\}</math>] // msg3 ←----- close connection -----→                     </pre>	<pre> receive msg1 extract <math>T_A</math> from V{<math>T_A</math>} using V generate random b <math>T_B \leftarrow g^b \text{ mod-p}</math> <math>K_B \leftarrow (T_A)^b \text{ mod-p}</math> send [B, A, <math>T_B</math>] // msg2                     </pre>

Principal A periodically delivers plaintext information M to principal B using the above protocol, where V is a key obtained from A's password, g and p are public Diffie-Hellman parameters, and M changes across sessions.

In each part below, if you answer no, explain briefly; if you answer yes, describe the attack.

- Can a passive attacker capable of off-line dictionary attack obtain M?
- Can an active attacker capable of off-line dictionary attack obtain M?

**5. [15 points]**

It is the year 2020, and quantum computing has just made it feasible for the general public to factor large numbers. Your company uses the following protocol, where  $g$  and  $p$  are Diffie-Hellman parameters, and  $K_1$  and  $K_2$  are explained below.

<b>A at tcp port x</b>		<b>B at tcp port y</b>	
←----- establish tcp connection between x and y ----->			
1	generate random a send [x, y, $K_1\{A, B, g, p, g^a \text{ mod } p\}$ ] // msg1		
2		receive msg1 generate random b send [y, x, $K_2\{B, A, g^b \text{ mod } p\}$ ] // msg2 compute $g^{ab} \text{ mod } p$	
3	receive msg2 compute $g^{ab} \text{ mod } p$ send [x, y, hash{ $g^{ab} \text{ mod } p$ }] // msg3		
4		receive msg 3 send [y, x, hash{1, $g^{ab} \text{ mod } p$ }] // msg4	
←----- A and B use $g^{ab} \text{ mod } p$ to encrypt data ----->			

- a. Suppose  $K_1$  is B's RSA public encryption key, and  $K_2$  is A's RSA public encryption key.
  - a1. Does the protocol hide B's identity against a passive attacker? If yes, explain. If no, show an attack.
  - a2. Does the protocol provide perfect forward secrecy against a passive attacker? If yes, explain. If no, show an attack.
- b. Repeat part a but now suppose that  $K_1$  is a shared secret key (and hence the same as  $K_2$ ).
- c. In what situation would the protocol in part b not be practical.

**6. [20 points]**

In the following Needham-Schroeder-like protocol,  $K_{AB}$ ,  $N_1$ ,  $N_2$ ,  $N_3$ , and  $N_4$  are randomly generated.

A (has master key $K_A$ )	KDC (has $[A, K_A], [B, K_B], \dots$ )	B (has master key $K_B$ )
<pre> send [A,KDC, N<sub>1</sub>, 'A to B'] // msg1  receive msg2 if (N<sub>1</sub> in msg1) ≠ (N<sub>1</sub> in msg2) then abort send [A,B, tkt<sub>AB</sub>, K<sub>AB</sub>{N<sub>2</sub>, N<sub>3</sub>}] // msg3  receive msg4 if M<sub>3</sub> = N<sub>3</sub> - 1 then B authenticated else abort M<sub>4</sub> ← N<sub>4</sub> - 1 send [A,B, K<sub>AB</sub>{M<sub>4</sub>}] // msg5  ----- A and B use K<sub>AB</sub> to encrypt data -----&gt;                     </pre>	<pre> receive msg1 tkt<sub>AB</sub> ← K<sub>B</sub>{K<sub>AB</sub>, A, N<sub>2</sub>} send [KDC,A, K<sub>A</sub>{N<sub>1</sub>, N<sub>2</sub>, B, K<sub>AB</sub>, tkt<sub>AB</sub>}] // msg2  receive msg3 if (N<sub>2</sub> in tkt<sub>AB</sub>) ≠ (N<sub>2</sub> in K<sub>AB</sub>{N<sub>2</sub>,N<sub>3</sub>}) then abort M<sub>3</sub> ← N<sub>3</sub> - 1 send [B,A, K<sub>AB</sub>{M<sub>3</sub>, N<sub>4</sub>}] // msg4  receive msg5 if M<sub>4</sub> = N<sub>4</sub> - 1 then A authenticated else abort                     </pre>	

- An attacker can eavesdrop and send messages with sender id A (but not B). The attacker learns A's master key  $K_A$  after which A changes it. Show how the attacker can have itself authenticated as A to B.
- Modify the protocol to stop the attack in part a. You can add new messages and/or augment existing messages.
- Modify the code executed by B to stop the attack in part a. Do not add new messages or change the existing messages.