

# Spatio-temporal Range Searching Over Compressed Kinetic Sensor Data



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# Motivation



- ▶ Kinetic data: data generated by moving objects
- ▶ Sensors collect data
- ▶ Large amounts of data
- ▶ Collect and perform lossless compression
- ▶ Goal: retrieve without decompressing
- ▶ Next: analyze

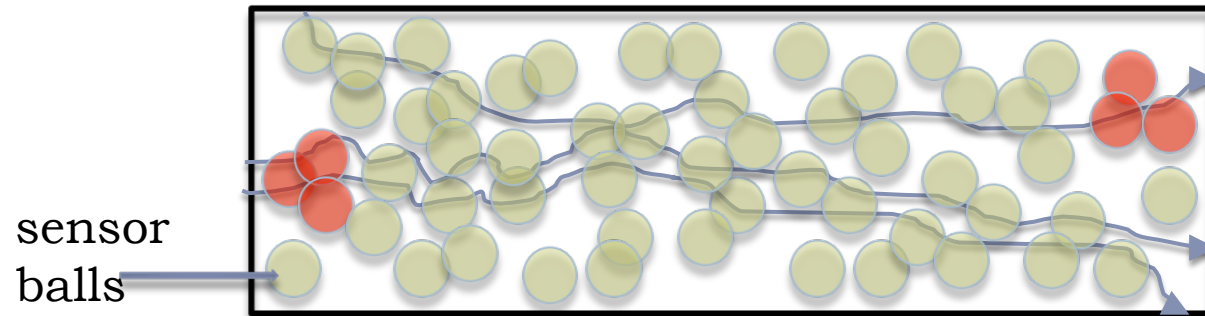
# Motivation

- ▶ Computer Science
  - ▶ Graphics: Image and video segmentation, animation
  - ▶ Databases: Maintenance over time
  - ▶ Sensor Networks: Data analysis
- ▶ Physics
  - ▶ Simulations
- ▶ Biology
  - ▶ Mathematical ecology: Migratory paths
  - ▶ HIV strain analysis
- ▶ Engineering
  - ▶ Traffic patterns and identification

# Our Framework

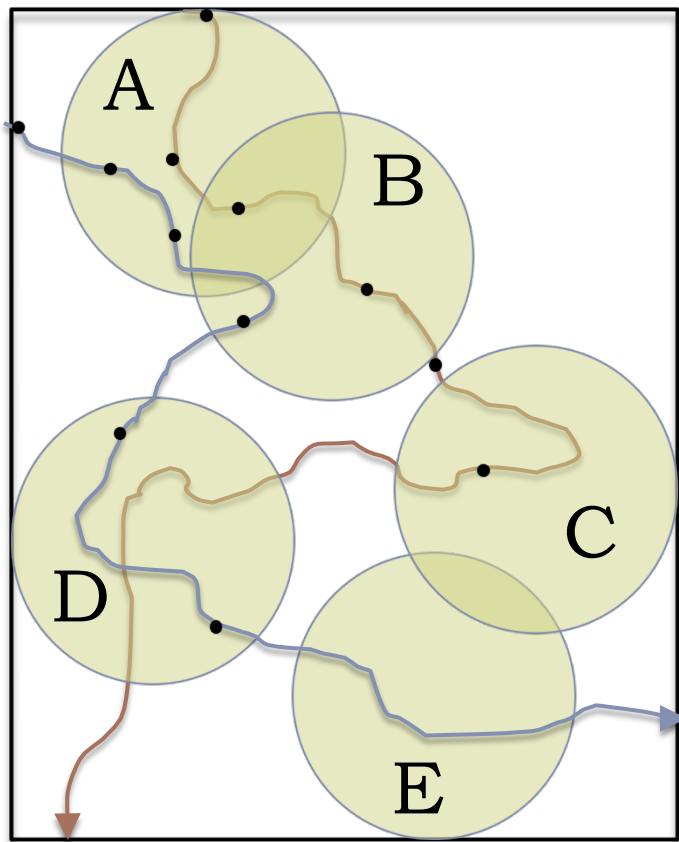
[FriedlerMount09]

- ▶ Detection region around each sensor (stationary sensors)
- ▶ Point motion unrestricted
- ▶ No advance knowledge about motion
- ▶ Each sensor reports the count of points within its region at each synchronized time step
- ▶  $k$ -local: Sensor outputs statistically only dependent on  $k$  nearest neighbors



# Data Collection

Data based on underlying geometric motion



Sensor data streams

A	B	C	D	E
1	0	0	0	0
2	0	0	0	0
2	1	0	0	0
0	2	0	0	0
0	0	0	1	0
0	0	1	1	0

time  
↓

# Range Searching: Our Problem

Compress and preprocess the data so as to perform...

- ▶ Temporal range query: Given a time interval, return an aggregation of the counts over that time interval.

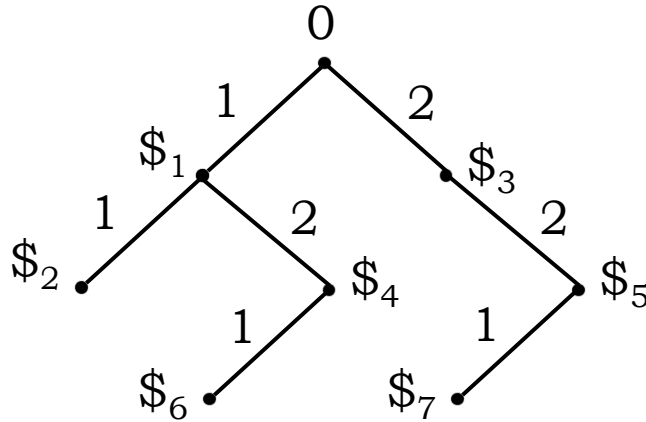
aggregation type: sum      t: 1 2 3 4 5 6 7 8 9 10 11  
X: 0,0,4,4,5,4,3,3,1, 1, 0 → 17

- ▶ Spatio-temporal range query: Given a time interval and spherical spatial region, return an aggregation of the counts over that time interval and within that region.

• 11122021...  
• 00110123...  
• 00223101...  
→ 10  
aggregation type: sum

# Lempel-Ziv Dictionary Compression [LZ78]

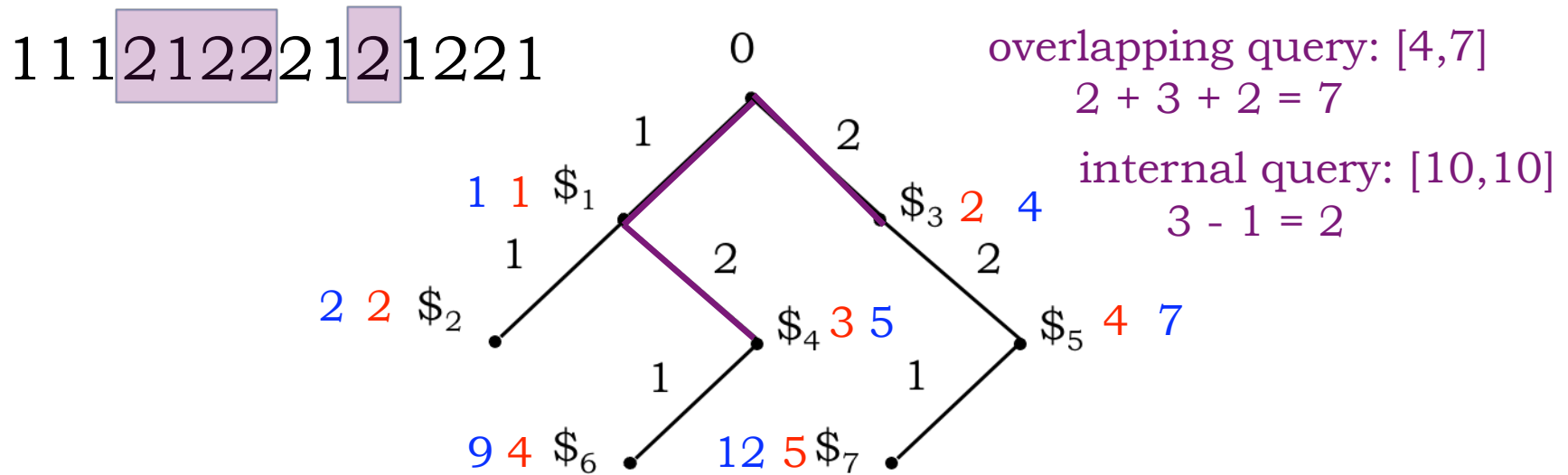
1 1 1 2 1 2 2 2 1 2 1 2 2 1  
↑ ↑ ↑ ↑ ↑     ↑     ↑



Create a trie while scanning through a string.  
The compressed string contains pointers to this dictionary.

# Temporal Range Searching

- ▶ Create trie with accompanying pointers
- ▶ Annotate trie with aggregate values and word start times
- ▶ Given a temporal range  $[t_0, t_1]$  find the anchor points  $\$^0$  and  $\$^1$  such that  $\$^0 \leq t_0$  and  $\$^1 \geq t_1$
- ▶ Use stored prefixes, words, and subtraction of prefixes to find aggregates





# Spatio-temporal Range Searching

## Set of Clumps

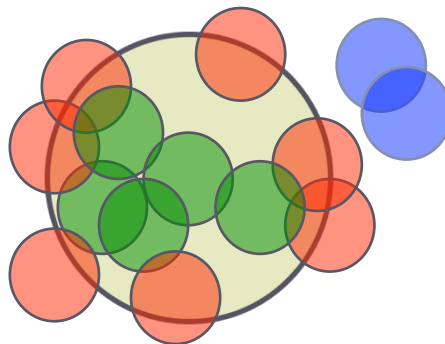
A finite set of balls with the following packing property:

Given any ball  $b$  with radius  $r$ , the number of clumps of radius  $r'$  that intersect  $b$  is at most  $O(1+(r/r')^\gamma)$  where  $\gamma$  is a constant possibly dependent on dimension.

## Clumps and Ranges

Given a range  $Q$ , a clump may either

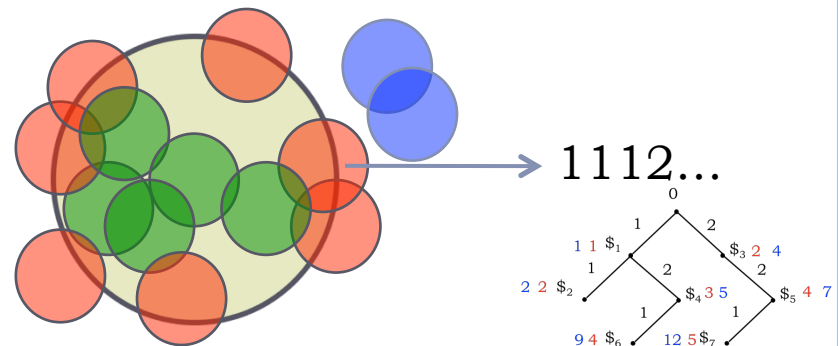
- ▶ be contained in  $Q$  (green)
- ▶ be stabbed by  $Q$  (red)
- ▶ lie outside of  $Q$  (blue)



# Spatio-temporal Range Searching

- ▶ The sensors are clustered and compressed. Each cluster has an associated ball. These balls form a set of clumps.
- ▶ Range Searching Among Clumps: Given any query range  $Q$  and using a partition-tree, we can report
  - ▶ a subset of clump subsets that form a disjoint cover of the clumps within  $Q$
  - ▶ the subset of clumps that  $Q$  stabs

- ▶ Main Theorem: By adding an auxiliary data structure to answer temporal range queries to each node in the range searching among clumps solution we can answer spatio-temporal range queries.



# Results

Bounds for Range Searching		
	Temporal	Spatio-temporal
Preprocessing time	$O(\text{Enc}(X))$	$O(\text{Enc}(\mathbf{X}))$
Query time	$O(\log T)$	$O(((1/\varepsilon^{d-1}) + \log S) \log T)$
Space	$O(\text{Enc}(X))$	$O(\text{Enc}(\mathbf{X}) \log S)$

- ▶  $X$ : The set of sensor system observations
- ▶  $\text{Enc}(X)$ : The encoded size (in bits) of the sensor system
- ▶  $T$ : The total time over which data was collected
- ▶  $S$ : The total number of sensors
- ▶  $d$ : The dimension of the sensor space

First range searching bounds over compressed data

## Other Results and Future Work

- ▶ Temporal range searching in the semigroup setting ✓
- ▶ Extend analysis of compression algorithm to consider empirical entropy (no underlying random process) ✓
- ▶ Extend analysis to allow  $\delta$ -independence instead of strict pure statistical dependence ✓
- ▶ Statistical analysis without decompressing the data
- ▶ Lossy compression
- ▶ Experimental evaluation
- ▶ Application in non-sensor contexts

Thank you!  
Questions?