

Computergrafik

Matthias Zwicker
Universität Bern
Herbst 2016

Today

Shading

- Introduction
- Radiometry & BRDFs
- Local shading models
- Light sources
- Shading strategies

Shading

- Compute interaction of light with surfaces
- Requires simulation of physics
 - Solve Maxwell's equations (wave model)?
http://en.wikipedia.org/wiki/Maxwell's_equations
 - Use geometrical optics (ray model)?
http://en.wikipedia.org/wiki/Geometrical_optics
[http://en.wikipedia.org/wiki/Ray_\(optics\)](http://en.wikipedia.org/wiki/Ray_(optics))

“Global illumination” in computer graphics

http://en.wikipedia.org/wiki/Global_illumination

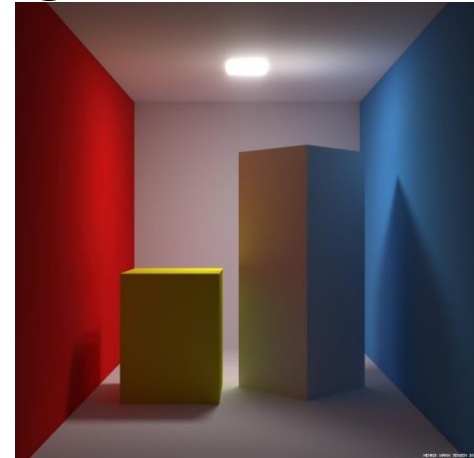
- “Gold standard” for photorealistic image synthesis
- Based on geometrical optics (ray model)
- **Multiple bounces** of light
 - Reflection, refraction, volumetric scattering, subsurface scattering
- Computationally expensive, minutes per image
- Movies, architectural design, etc.

Global illumination

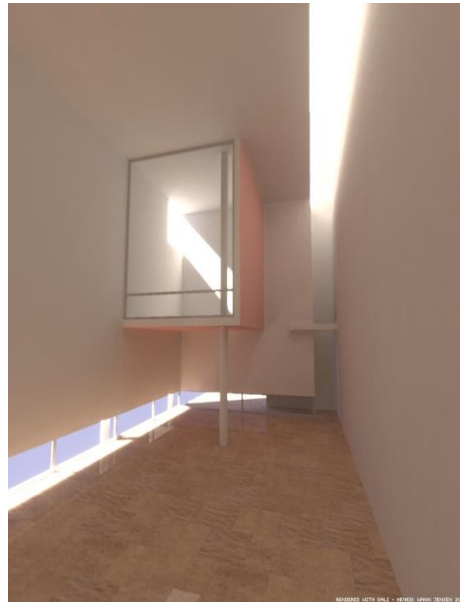
- Rendering algorithms, spring semester!



<http://www.pbrt.org/gallery.php>



Henrik Wann Jensen



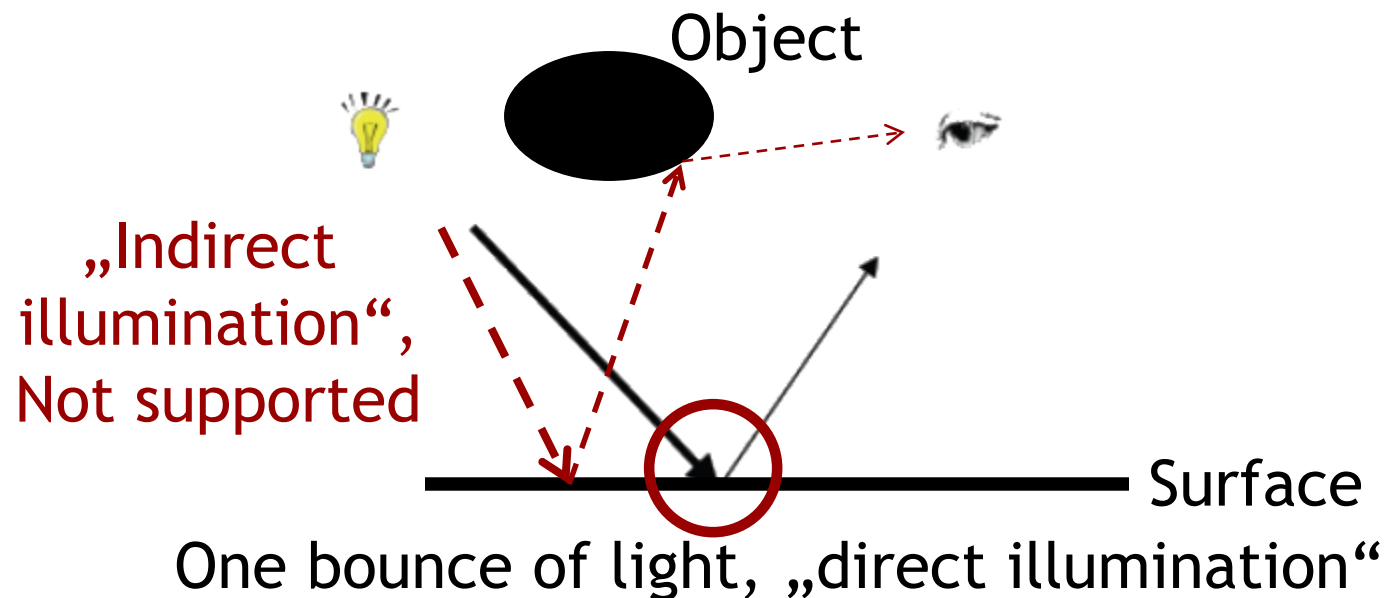
Henrik Wann Jensen



Henrik Wann Jensen

Interactive applications

- Approximations to global illumination possible, but not standard today
- Usually
 - Reproduce perceptually most important effects
 - **One bounce** of light between light source and viewer
 - **“Local/direct illumination”**



Today

Shading

- Introduction
- Radiometry & BRDFs
- Local shading models
- Light sources
- Shading strategies

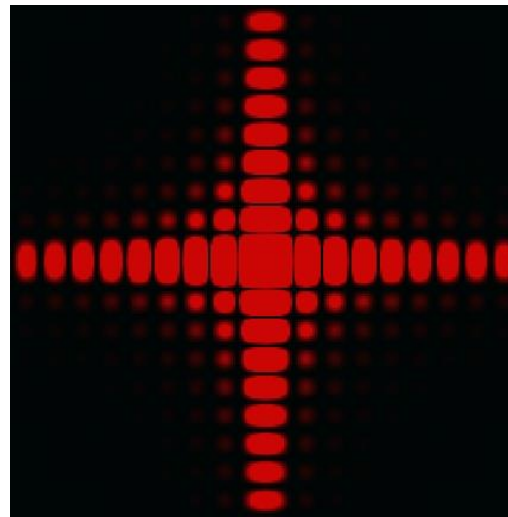
Material appearance

- What is giving a material its color and appearance?
- How is light reflected by a
 - Mirror
 - White sheet of paper
 - Blue sheet of paper
 - Glossy metal



Radiometry

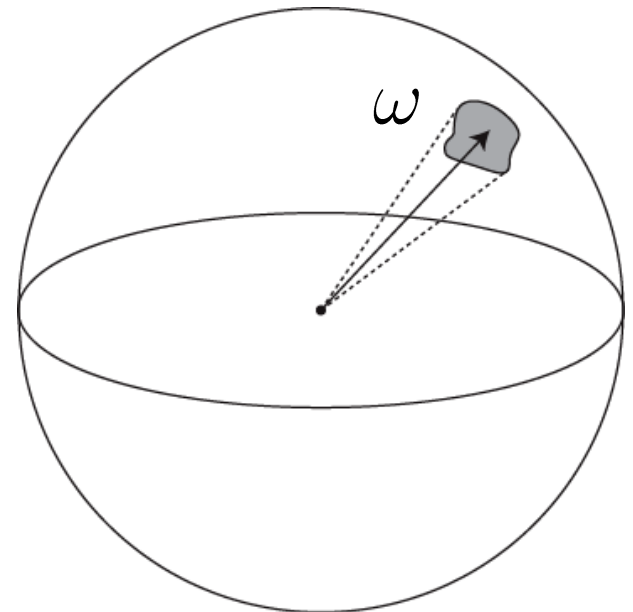
- Physical units to measure light energy
- Based on the geometrical optics model
- Light modeled as **rays**
 - Rays are idealized narrow beams of light
http://en.wikipedia.org/wiki/Ray_%28optics%29
 - Rays carry a spectrum of electromagnetic energy
- No wave effects, like interference or diffraction



Diffraction pattern
from square aperture

Solid angle

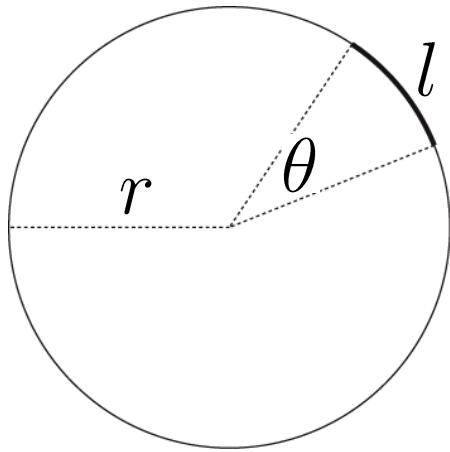
- Area of a surface patch on the unit sphere
 - In our context: area spanned by a set of directions
- Unit: steradian sr
- Directions usually denoted by ω



Unit sphere

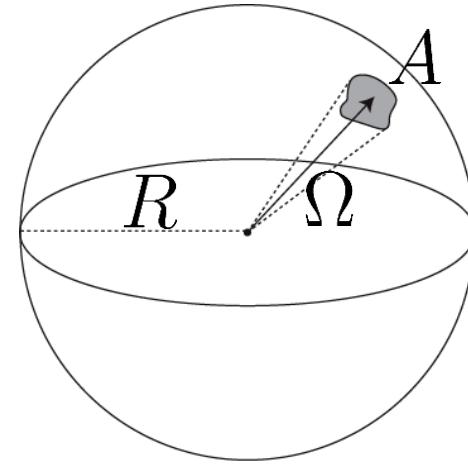
Angle and solid angle

Circle with radius r



- Angle $\theta = l/r$
- Unit circle has 2π radians

Sphere with radius R



- Solid angle $\Omega = A/R^2$
- Unit sphere has 4π steradians

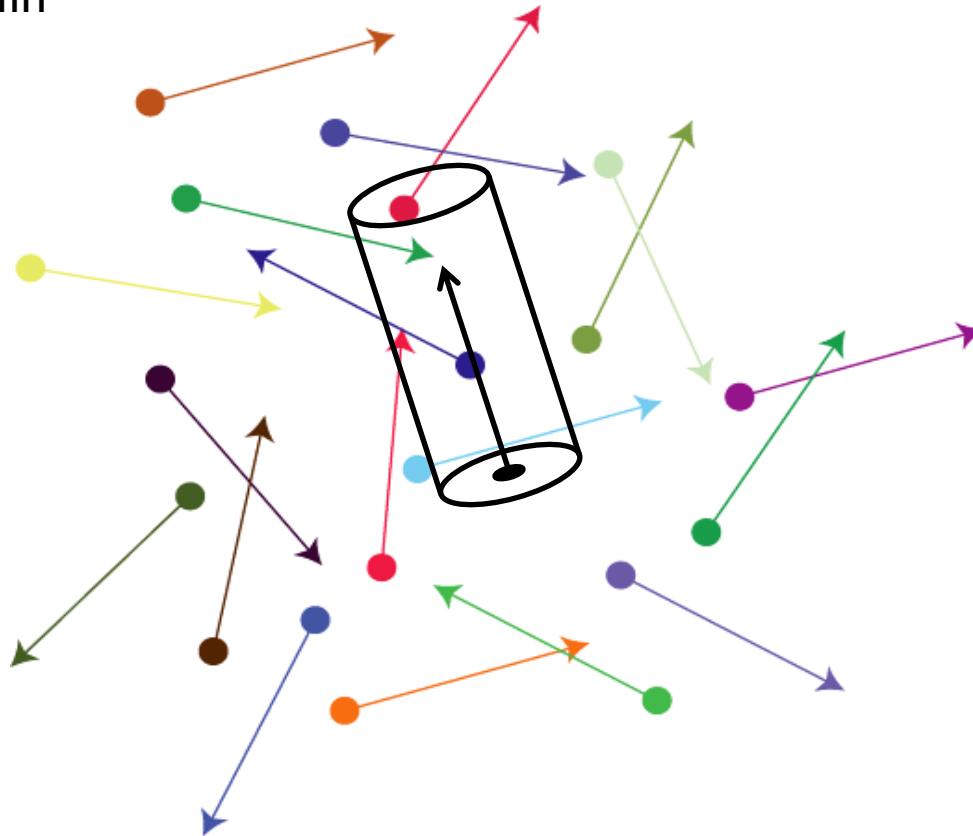
Radiance

<http://en.wikipedia.org/wiki/Radiance>

- „Energy carried along a narrow beam (ray) of light“
- Energy passing through a small area in a small bundle of directions, divided by area and by solid angle spanned by bundle of directions, in the limit as area and solid angle tend to zero
- Units: energy per area per solid angle
 $[W \cdot sr^{-1} \cdot m^{-2}]$

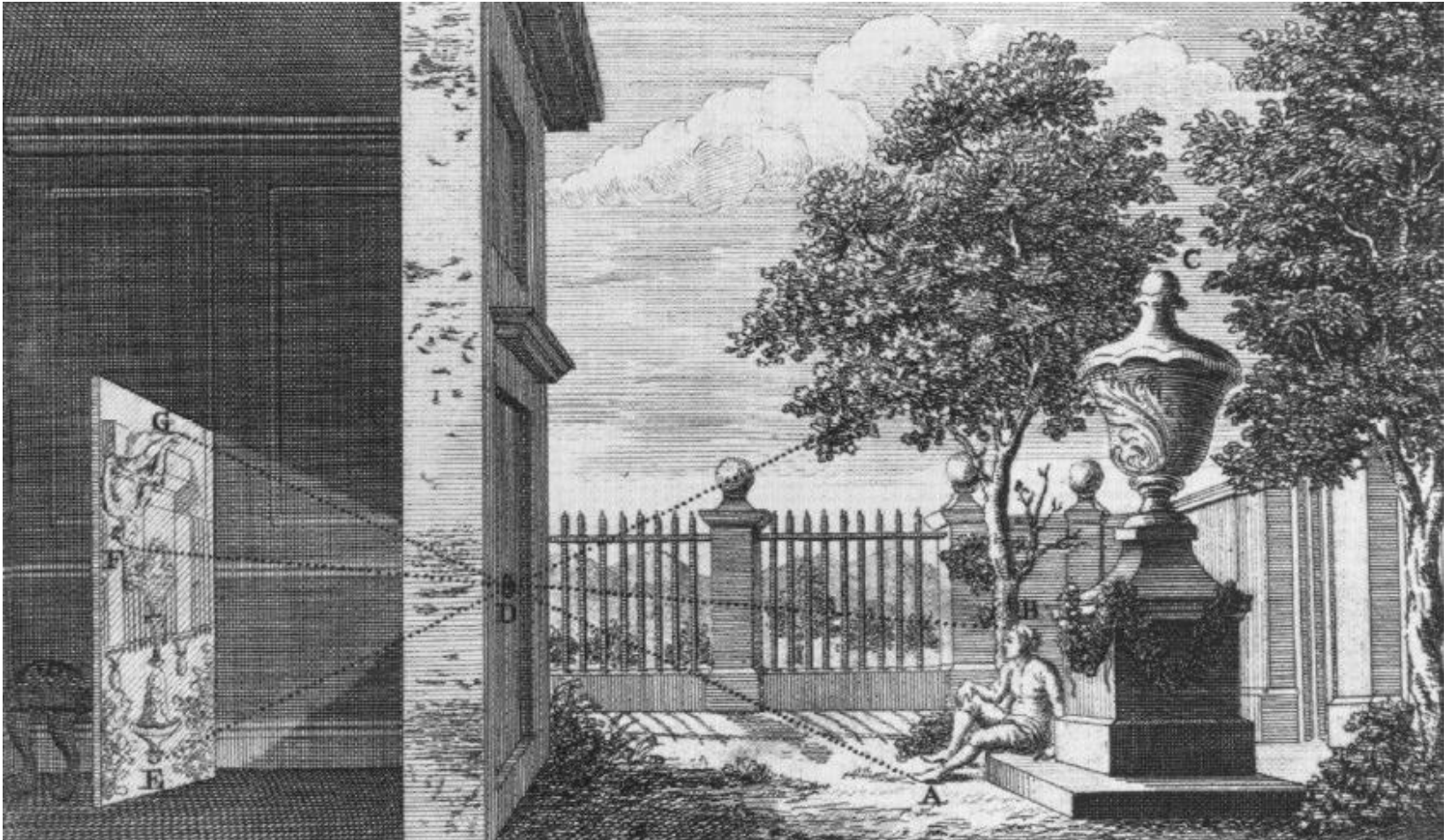
Radiance

- Think of light consisting of photon particles, each traveling along a ray
- Radiance is photon „ray density“
 - Number of photons per area per solid angle
 - „Number of photons passing through small cylinder, as cylinder becomes infinitely thin“



Pinhole camera

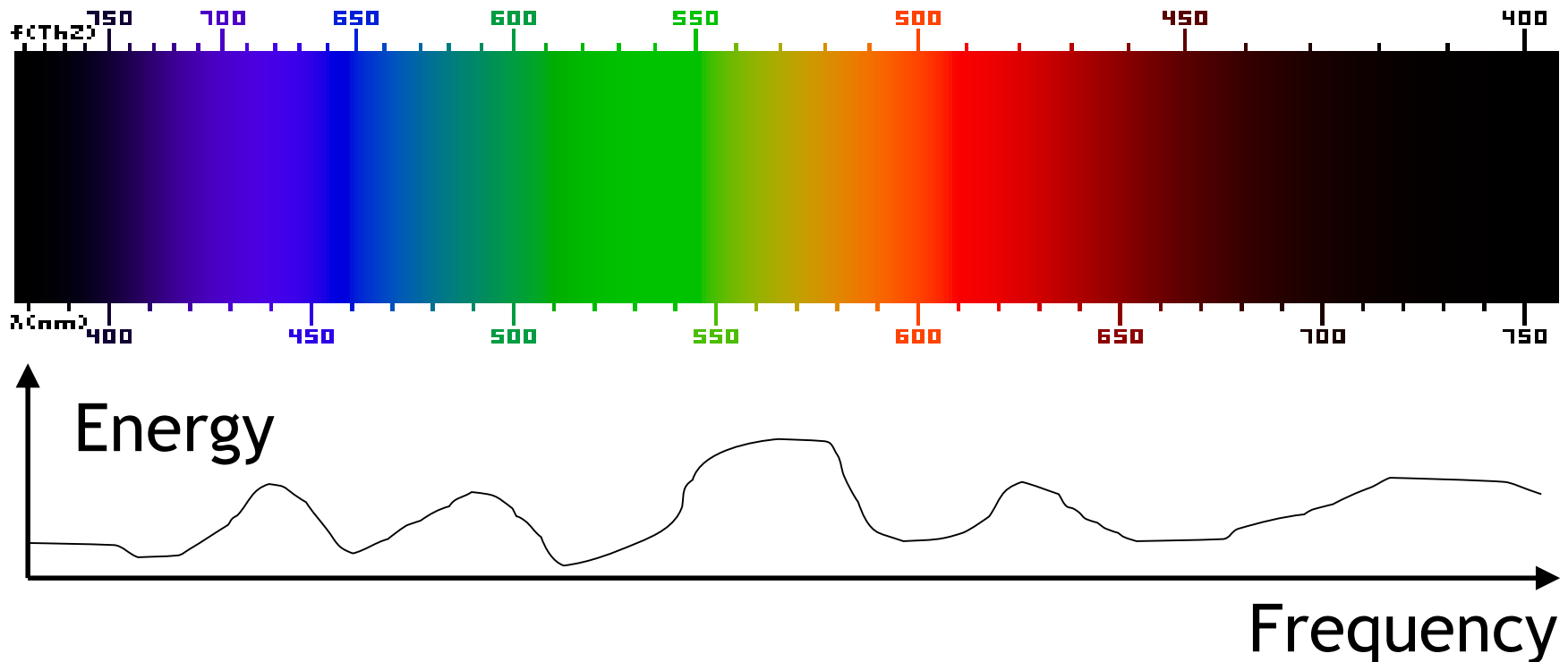
- Records radiance on projection screen



http://en.wikipedia.org/wiki/Pinhole_camera

Radiance

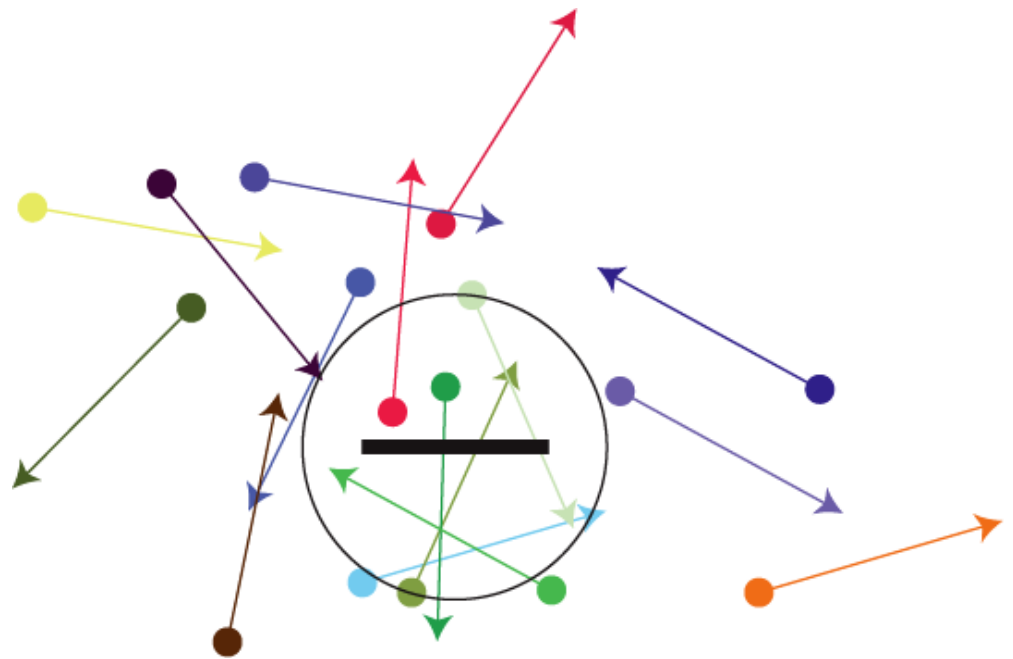
- **Spectral** radiance: energy at **each wavelength/frequency** (count only photons of given wavelength)
- Usually, work with radiance for three discrete wavelengths
 - Corresponding to R,G,B primaries



Irradiance

- Energy per area: „energy going through a small area, divided by size of area“
- „Radiance summed up over all directions“
- Units

$$[W \cdot m^{-2}]$$



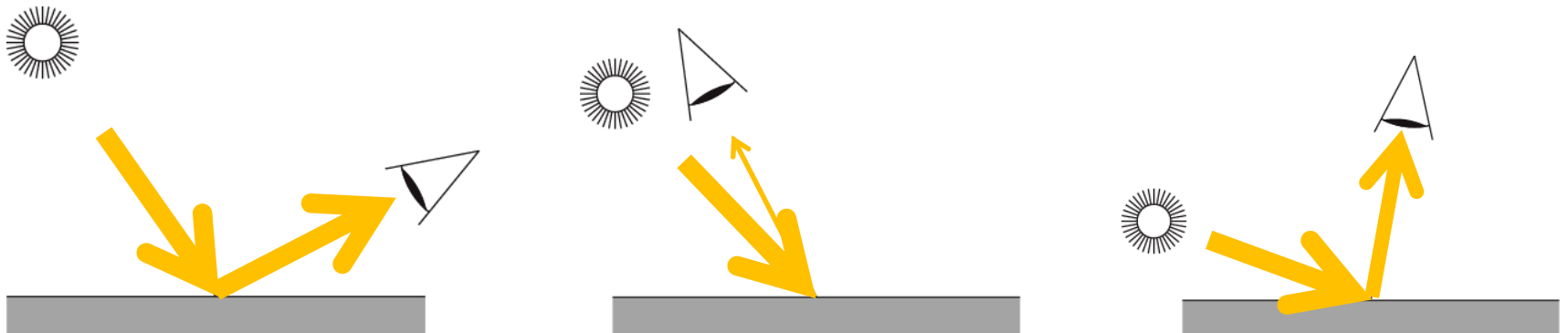
Irradiance: Count number of photons per area, in the limit as area becomes infinitely small

Local shading

- Goal: model reflection of light at surfaces
- Bidirectional reflectance distribution function (BRDF)

http://en.wikipedia.org/wiki/Bidirectional_reflectance_distribution_function

- “Given light direction, viewing direction, obtain fraction of light reflected towards the viewer”
- For any pair of light/viewing directions!
- For different wavelengths (or R, G, B) separately



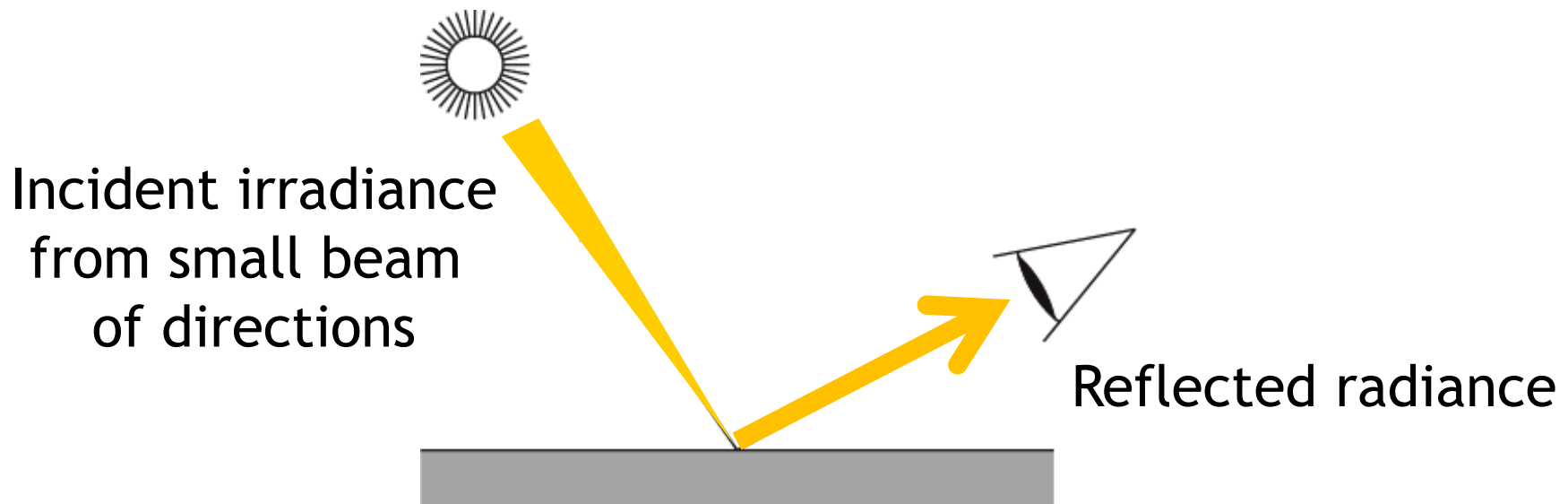
“For each pair of light/view direction, BRDF gives fraction of reflected light”

BRDFs

- BRDF describes **appearance** of material
 - Color
 - Diffuse
 - Glossy
 - Mirror
 - Etc.
- BRDF can be different at each point on surface
 - Spatially varying BRDF (SVBRDF)
 - Textures

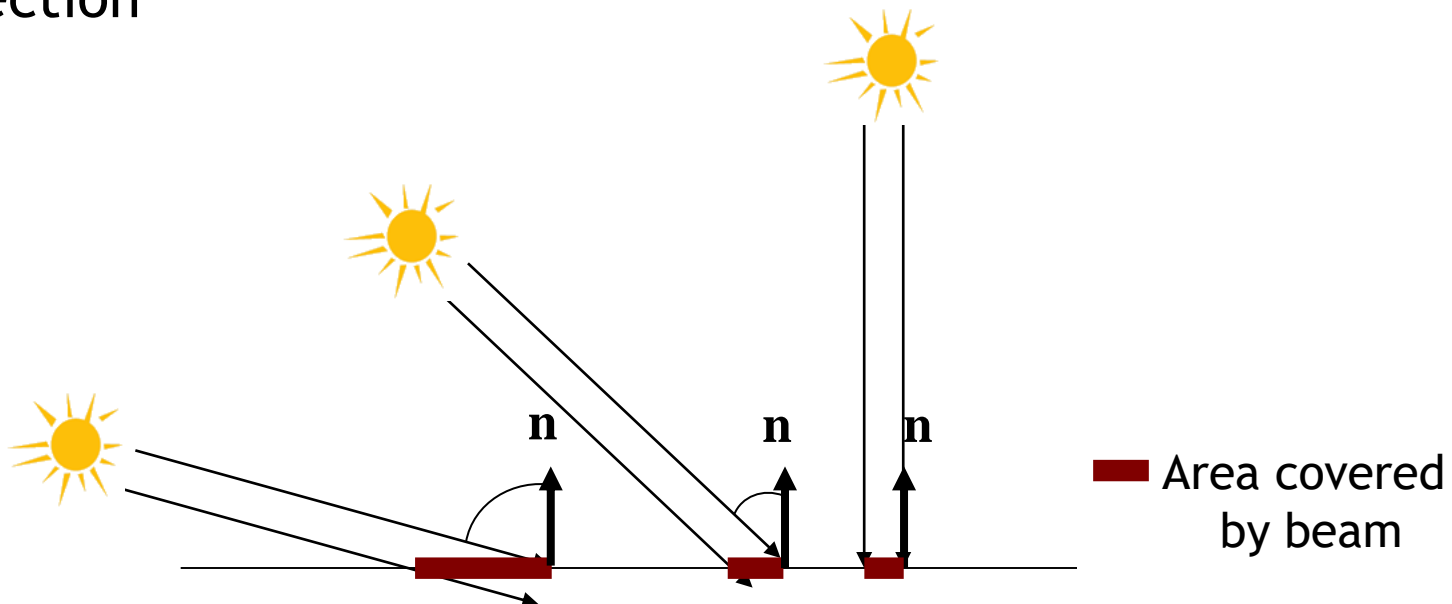
Technical definition

- Given incident and outgoing directions
- BRDF is fraction of "radiance reflected in outgoing direction" over "incident irradiance arriving from narrow beam of directions"
- Units $[W \cdot sr^{-1} \cdot m^{-2}] / [W \cdot m^{-2}] = sr^{-1}$



Irradiance from a narrow beam

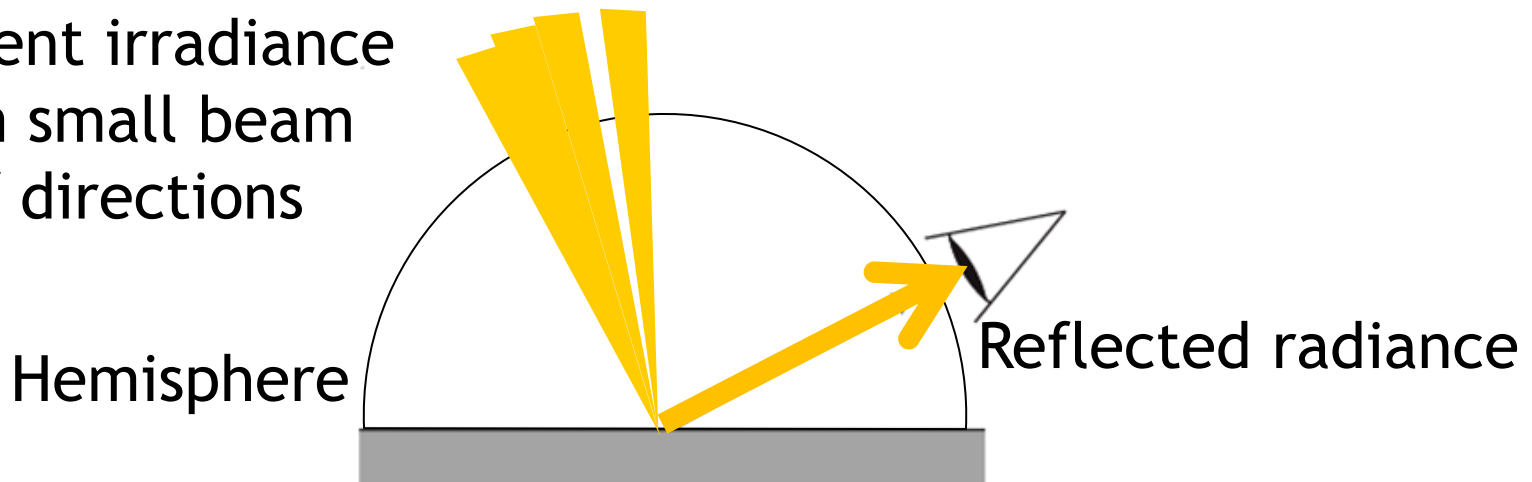
- Narrow beam of parallel rays shining on a surface
 - Area covered by beam varies with the angle between the beam and the normal \mathbf{n}
 - The larger the area, the less incident light per area
- **Irradiance** (incident light per unit area) is **proportional to the cosine** of the angle between the surface normal \mathbf{n} and the light rays
- Equivalently, irradiance contributed by beam is radiance of beam times cosine of angle between normal \mathbf{n} and beam direction



Shading with BRDFs

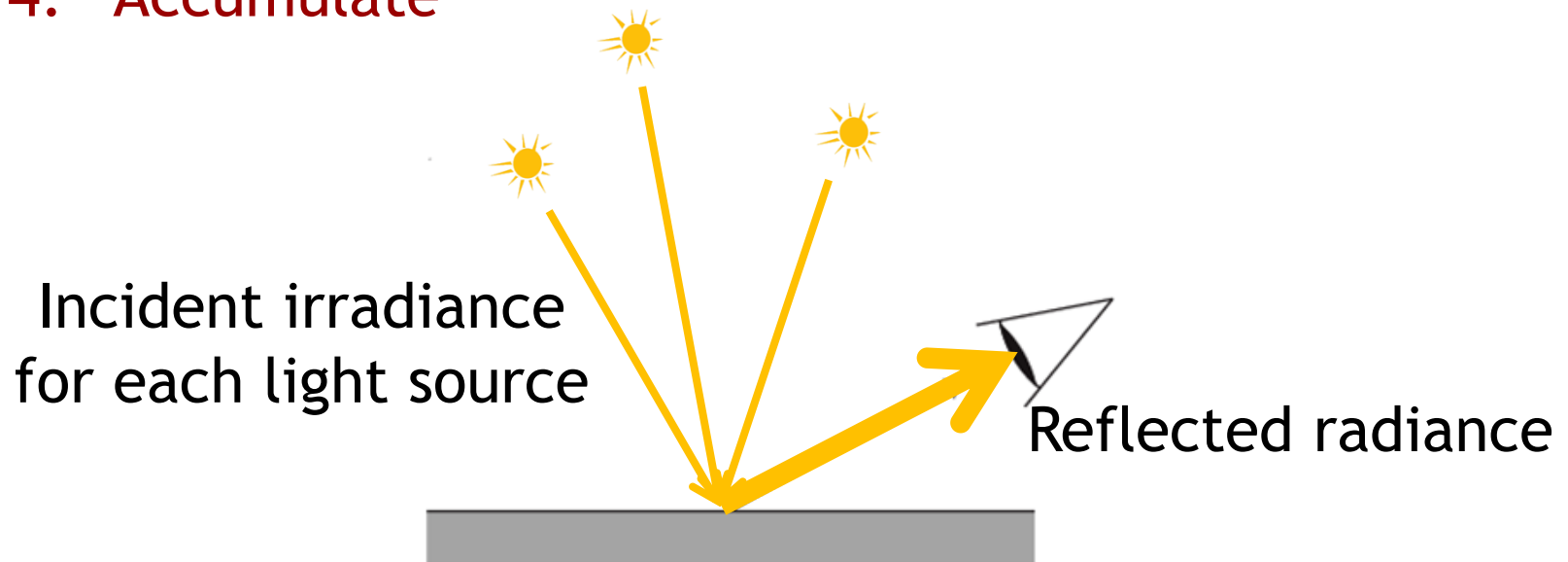
- Given radiance arriving from each direction, outgoing direction
- For all incoming directions over the hemisphere
 1. Compute **irradiance** from incoming beam
 2. **Evaluate BRDF** with incoming beam direction, outgoing direction
 3. **Multiply** irradiance and BRDF value
 4. **Accumulate**
- Mathematically, a hemispherical integral ("shading integral")
https://en.wikipedia.org/wiki/Rendering_equation

Incident irradiance
from small beam
of directions



Shading with BRDFs

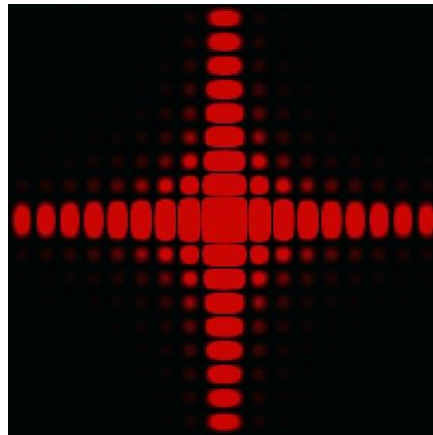
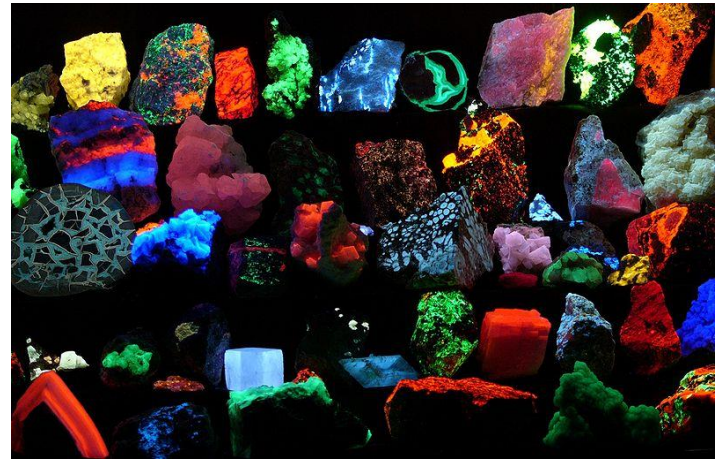
- If only discrete number of **small light sources** taken into account, need minor modification of algorithm
- For each light source
 1. Compute **irradiance** arriving from light source
 2. **Evaluate BRDF** with direction to light source, outgoing direction
 3. **Multiply** irradiance and BRDF value
 4. **Accumulate**



Limitations of BRDF model

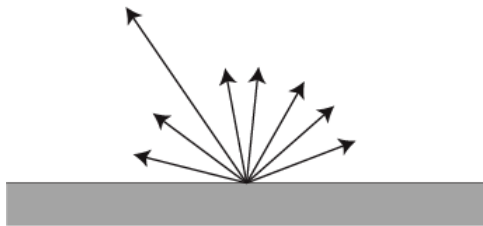
Cannot model

- Fluorescence
- Subsurface and volume scattering
- Polarization
- Interference/diffraction

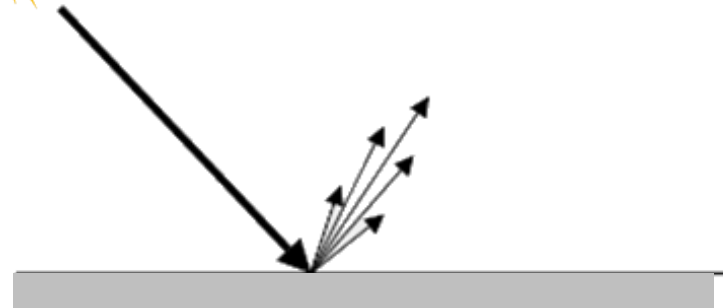


Visualizing BRDFs

- Given viewing or light direction, plot BRDF value over sphere of directions
- Illustration in „flatland“ (1D slices of 2D BRDFs)



Diffuse reflection

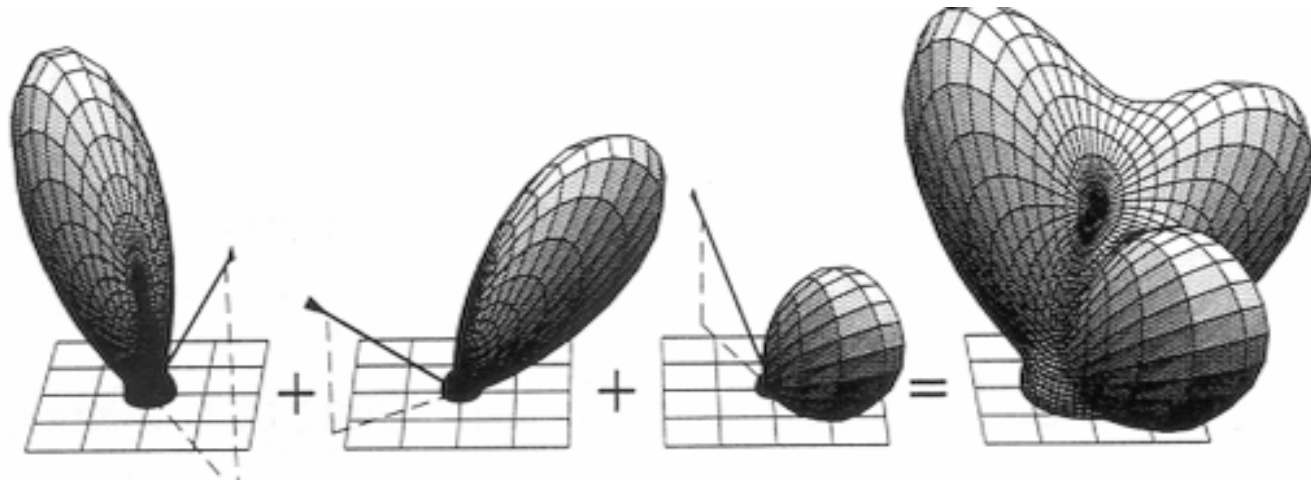


Glossy reflection



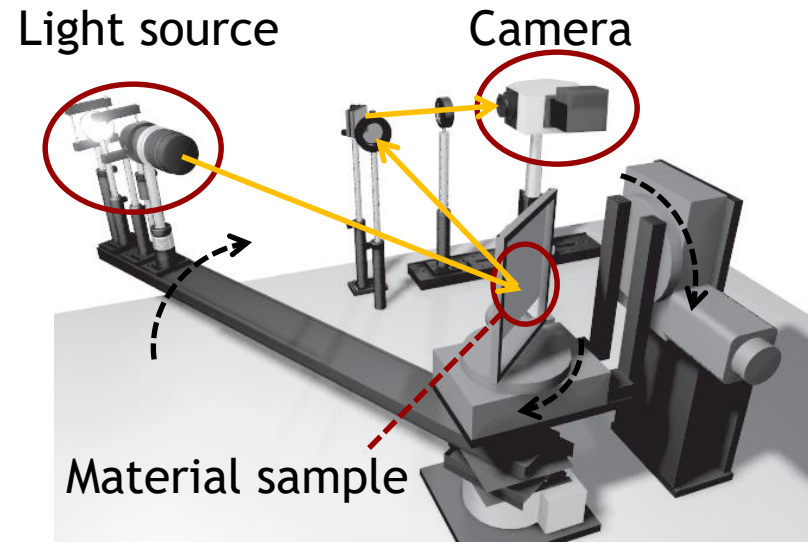
Visualizing BRDFs

- Can add up several BRDFs to obtain more complicated ones



BRDF representation

- How to define and store BRDFs that represent physical materials?
- **Physical measurements**
 - Gonioreflectometer: robot with light source and camera
 - Measures reflection for each light/camera direction
 - Store measurements in table
- Too much data for interactive application
 - 4 degrees of freedom!



Cornell University
Gonioreflectometer

BRDF representation

- Analytical models
 - Try to describe physical properties of materials using mathematical expressions
- Many models proposed in graphics
 - http://en.wikipedia.org/wiki/Bidirectional_reflectance_distribution_function
 - <http://en.wikipedia.org/wiki/Cook-Torrance>
 - http://en.wikipedia.org/wiki/Oren-Nayar_diffuse_model
- Will restrict ourselves to simple models here

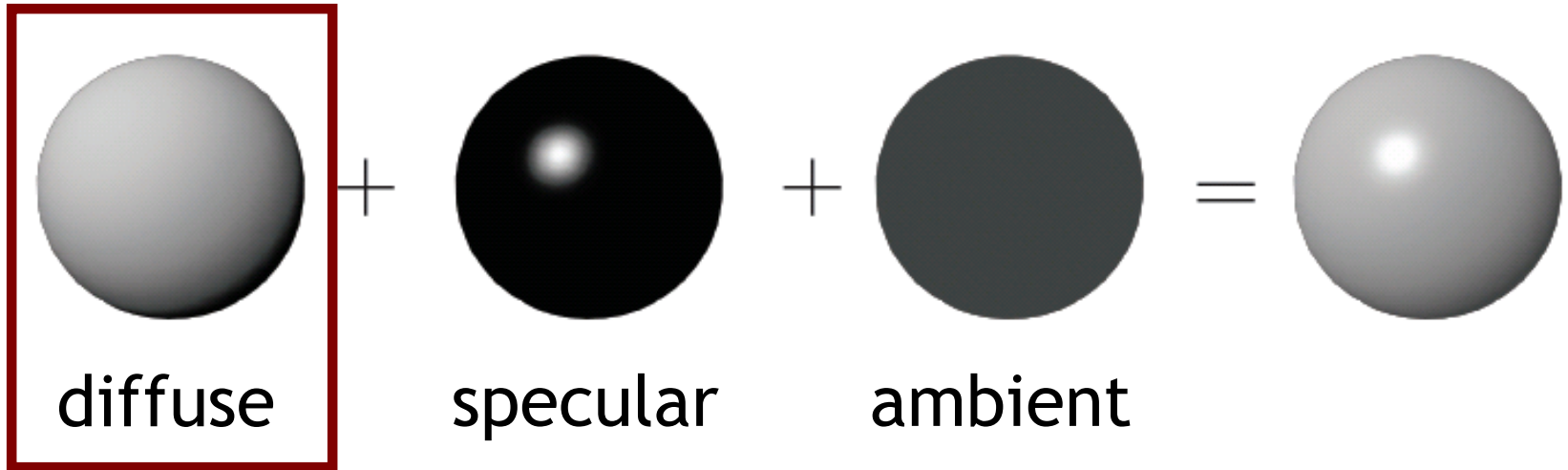
Today

Shading

- Introduction
- Radiometry & BRDFs
- Local shading models
- Light sources
- Shading strategies

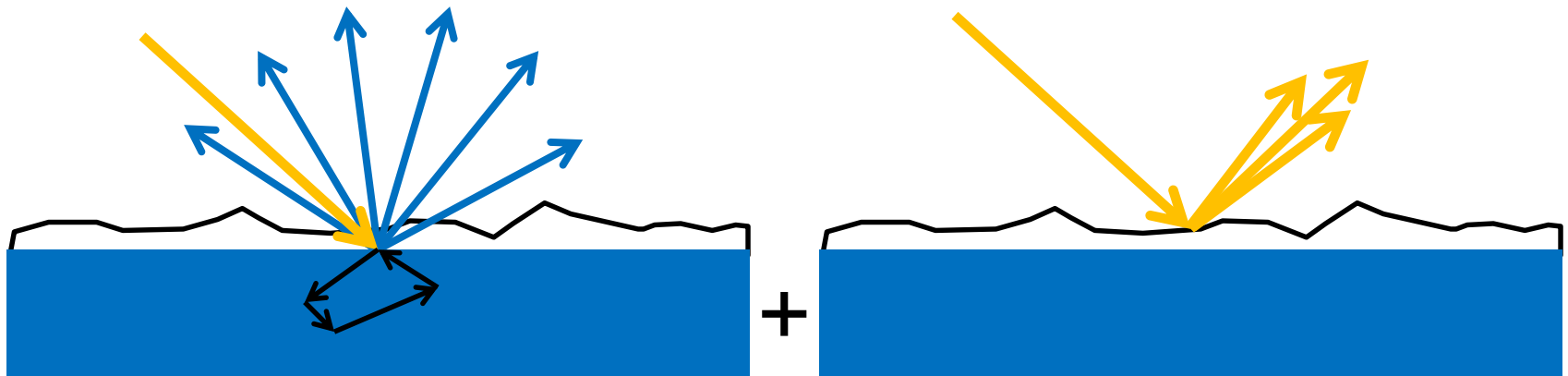
Simplified model

- BRDF is sum of **diffuse**, **specular**, and **ambient** components
 - Covers a large class of real surfaces
 - Each is simple analytical function
- Incident light from discrete set of light sources (discrete set of directions)
- Model is not completely physically justified!

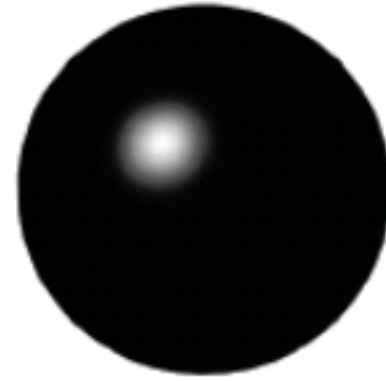


Simplified physical model

- Approximate model for two-layer materials
- Subsurface scattering leading to diffuse reflection on bottom layer
- Mirror reflection on (rough) top layer



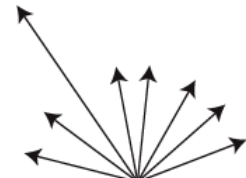
diffuse



specular

Diffuse reflection

- Ideal diffuse material reflects light equally in all directions
 - Also called **Lambertian** surfaces
http://en.wikipedia.org/wiki/Lambert's_cosine_law
- **View-independent**
 - Surface looks the same independent of viewing direction
- Matte, not shiny materials
 - Paper
 - Unfinished wood
 - Unpolished stone



Diffuse reflection



Diffuse sphere

Diffuse reflection

- “Radiance reflected by a diffuse (“Lambertian”) surface is constant over all directions”
- Hm, why do we see brightness variations over diffuse surfaces ?

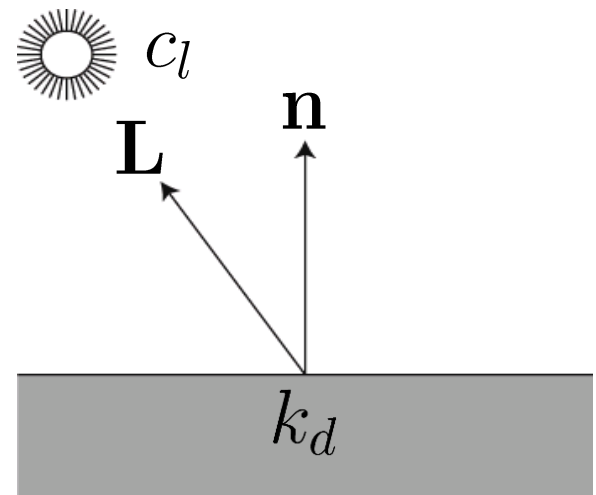


Diffuse reflection

- Given
 - Light color (radiance) c_l
 - Unit surface normal \mathbf{n}
 - One light source, unit light direction \mathbf{L}
 - Material diffuse reflectance (material color) k_d
- Diffuse reflection c_d

$$c_d = c_l (\underbrace{\mathbf{n} \cdot \mathbf{L}}_{\text{Cosine between normal and light}}) k_d$$

Cosine between
normal and light,
converts radiance to incident irradiance



Diffuse reflection

Notes on $c_d = c_l(\mathbf{n} \cdot \mathbf{L})k_d$

- Parameters k_d , c_l are r,g,b vectors
- c_l : **radiance** of light source
- $c_l(\mathbf{n} \cdot \mathbf{L})$: **irradiance** on surface
- k_d is diffuse BRDF, a **constant**!
- Compute r,g,b values of reflected color c_d separately

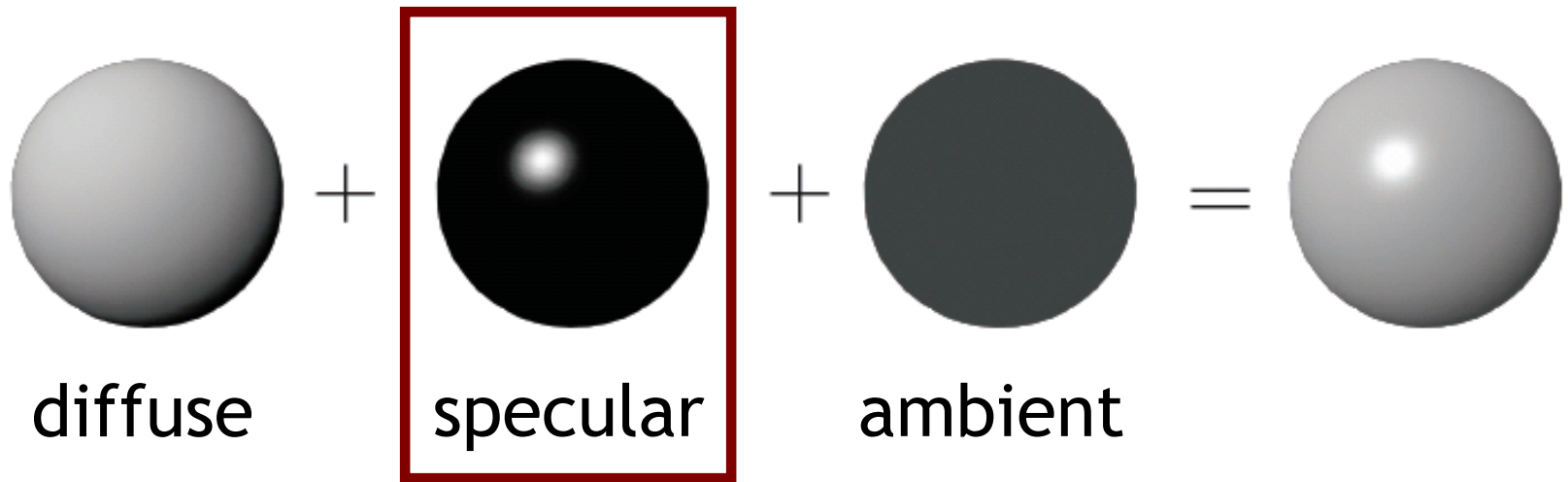
Diffuse reflection

- Provides visual cues
 - Surface curvature
 - Depth variation



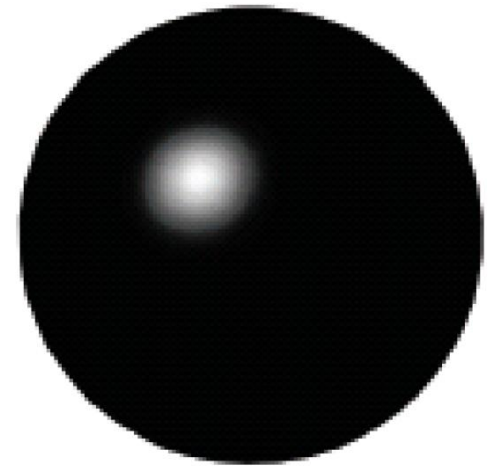
Lambertian (diffuse) sphere under different lighting directions

Simplified model



Specular reflection

- Shiny or glossy surfaces
 - Polished metal
 - Glossy car finish
 - Plastics
- Specular highlight
 - Blurred reflection of the light source
 - Position of highlight depends on viewing direction



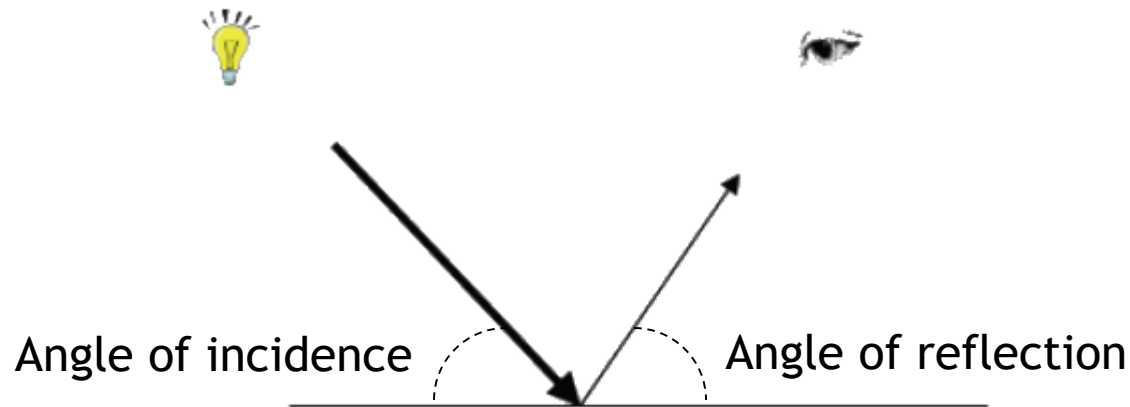
Sphere with
specular highlight

Shiny or glossy materials



Specular reflection

- Ideal specular reflection is mirror reflection
 - Perfectly smooth surface
 - Incoming light ray is bounced in single direction
 - Angle of incidence equals angle of reflection

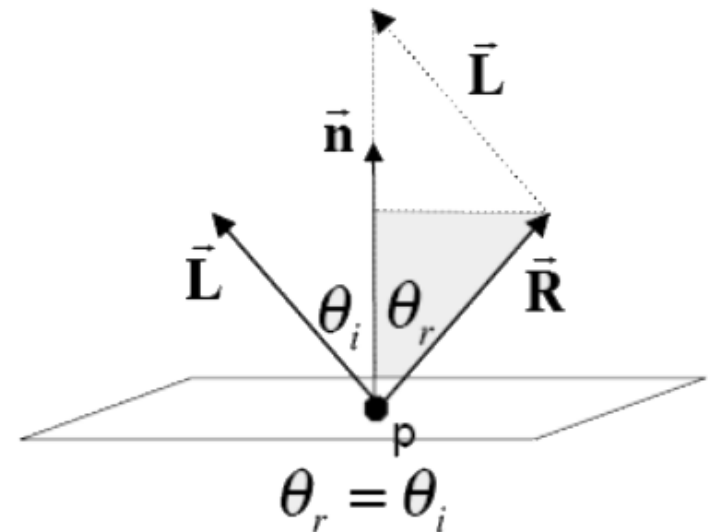


Law of reflection

- “Angle of incidence equals angle of reflection” applied to 3D vectors \mathbf{L} and \mathbf{R}
- Equation expresses constraints:
 1. Normal, incident, and reflected direction all in same plane ($\mathbf{L} + \mathbf{R}$ is a point along the normal)
 2. Angle of incidence $\theta_i =$ angle of reflection θ_r

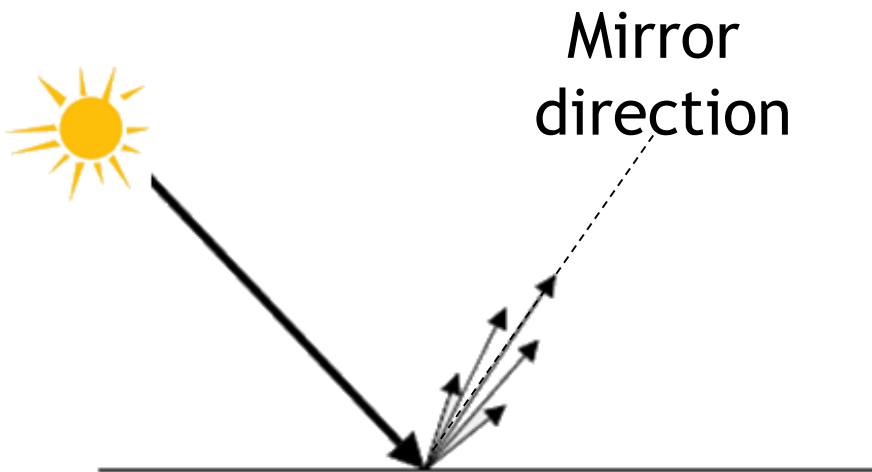
$$\bar{\mathbf{R}} + \bar{\mathbf{L}} = 2 \cos \theta \, \bar{\mathbf{n}} = 2(\bar{\mathbf{L}} \cdot \bar{\mathbf{n}}) \bar{\mathbf{n}}$$

$$\bar{\mathbf{R}} = 2(\bar{\mathbf{L}} \cdot \bar{\mathbf{n}}) \bar{\mathbf{n}} - \bar{\mathbf{L}}$$



Glossy materials

- Many materials not quite perfect mirrors
- Glossy materials have blurry reflection of light source



Glossy teapot with highlights from many light sources

Physical model

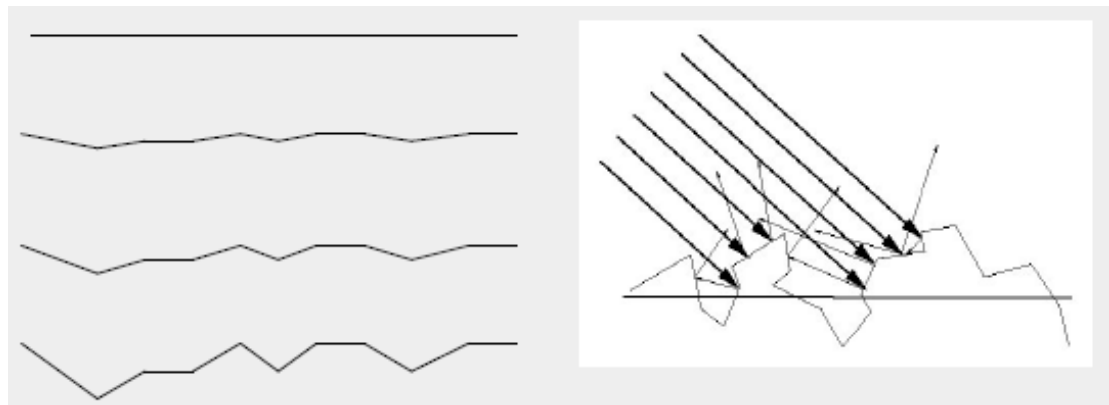
- Assume surface composed of small mirrors with random orientation (microfacets)
- Smooth surfaces
 - Microfacet normals close to surface normal
 - Sharp highlights
- Rough surfaces
 - Microfacet normals vary strongly
 - Leads to blurry highlight

Polished

Smooth

Rough

Very rough



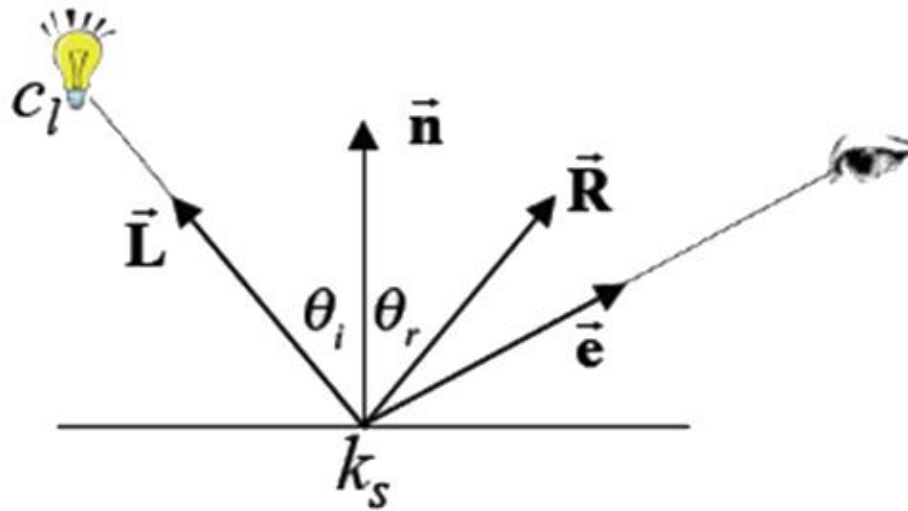
Physical model

- Expect most light to be reflected in mirror direction
- Because of microfacets, some light is reflected slightly off ideal reflection direction
- Reflection
 - Brightest when view vector is aligned with reflection
 - Decreases as angle between view vector and reflection direction increases

Phong model

http://en.wikipedia.org/wiki/Phong_shading

- Simple “implementation” of the physical model
- Radiance of light source c_l
- Specular reflectance coefficient k_s
- Phong exponent p
 - Higher p , smaller (sharper) highlight



Reflected radiance

$$c = c_l k_s (\mathbf{R} \cdot \mathbf{e})^p$$

Note

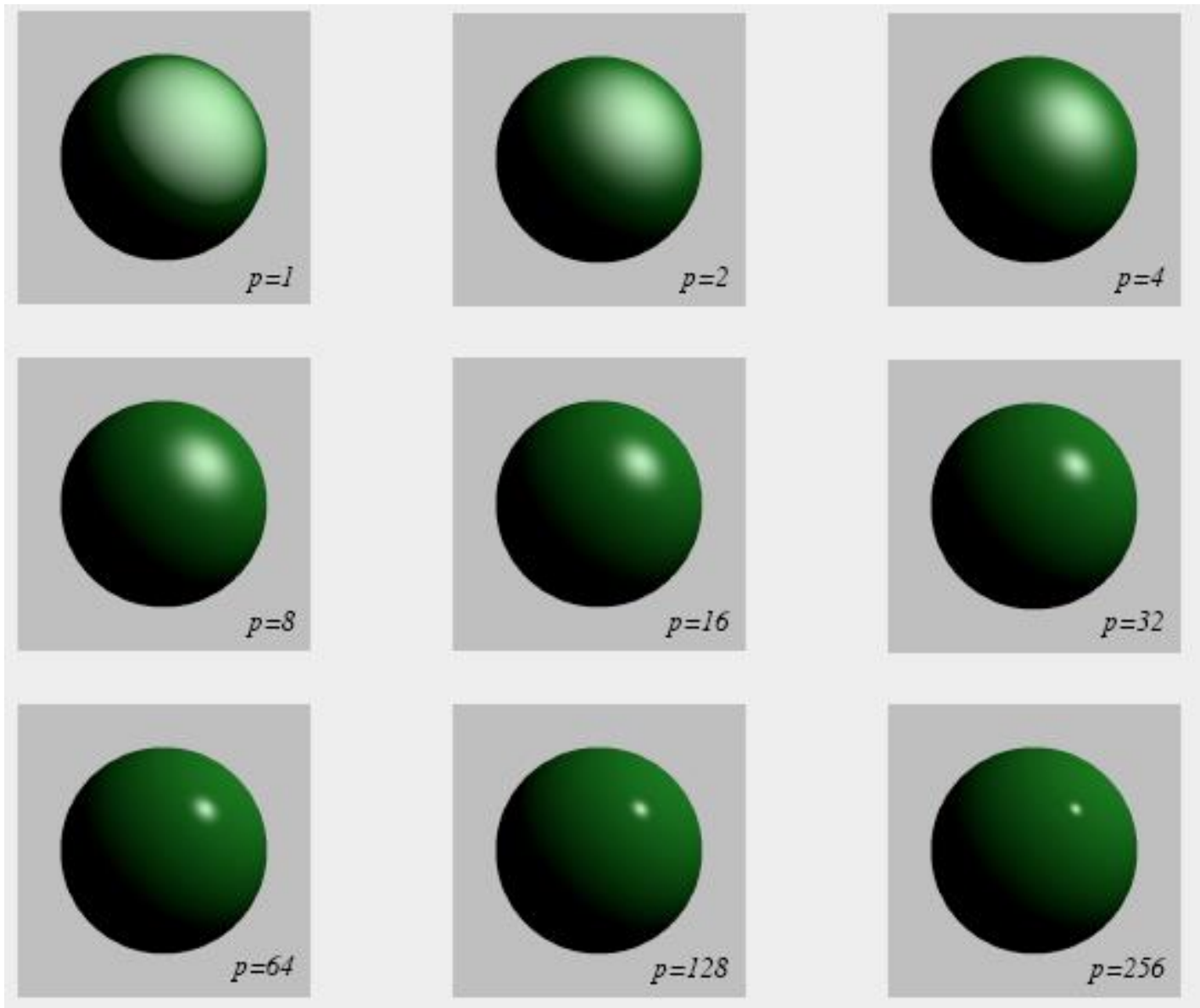
- Technically, Phong „BRDF“ is

$$c = c_l \underbrace{(\cancel{\mathbf{n}} \cdot \cancel{\mathbf{L}})}_{\text{Irradiance}} \underbrace{\frac{k_s (\mathbf{R} \cdot \mathbf{e})^p}{\cancel{\mathbf{n}} \cdot \cancel{\mathbf{L}}}}_{\text{„BRDF“}}$$

- Phong model is not usually considered a BRDF, because it violates energy conservation

http://en.wikipedia.org/wiki/Bidirectional_reflectance_distribution_function#Physically_based_BRDFs

Phong model

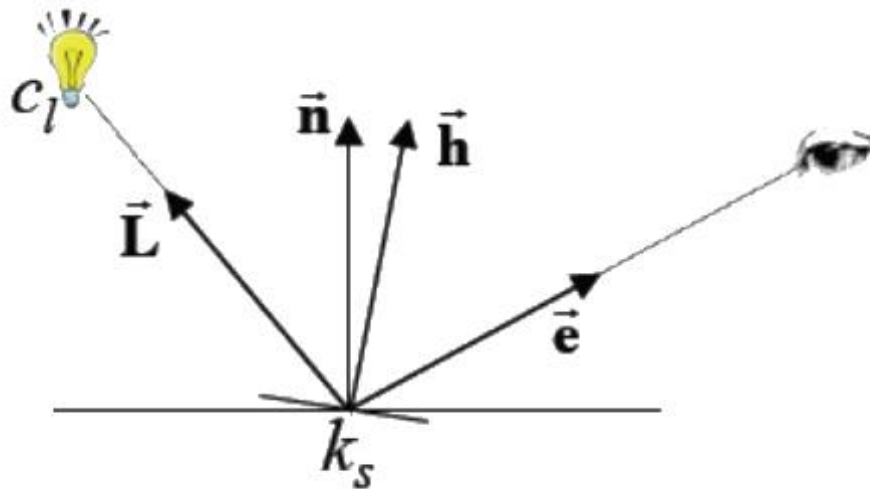


Blinn model (Jim Blinn, 1977)

- Alternative to Phong model
- Define unit halfway vector

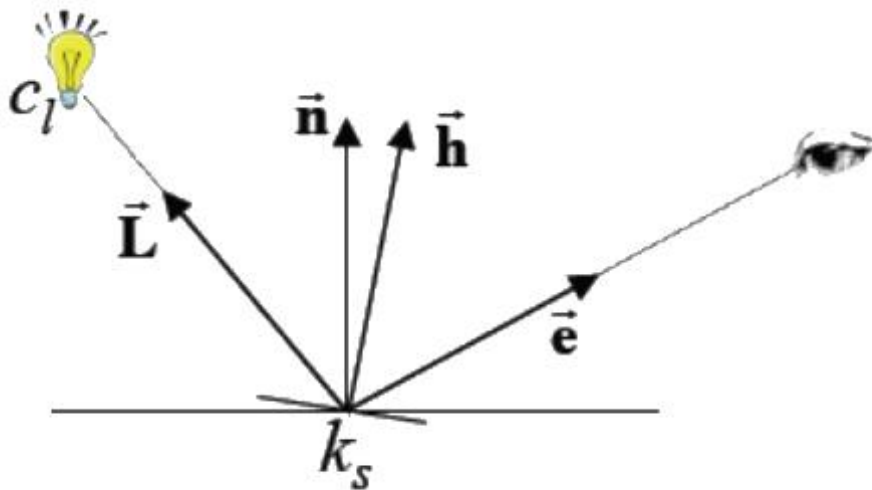
$$\mathbf{h} = \frac{\mathbf{L} + \mathbf{e}}{\|\mathbf{L} + \mathbf{e}\|}$$

- Halfway vector represents normal of microfacet that would lead to mirror reflection to the eye



Blinn model

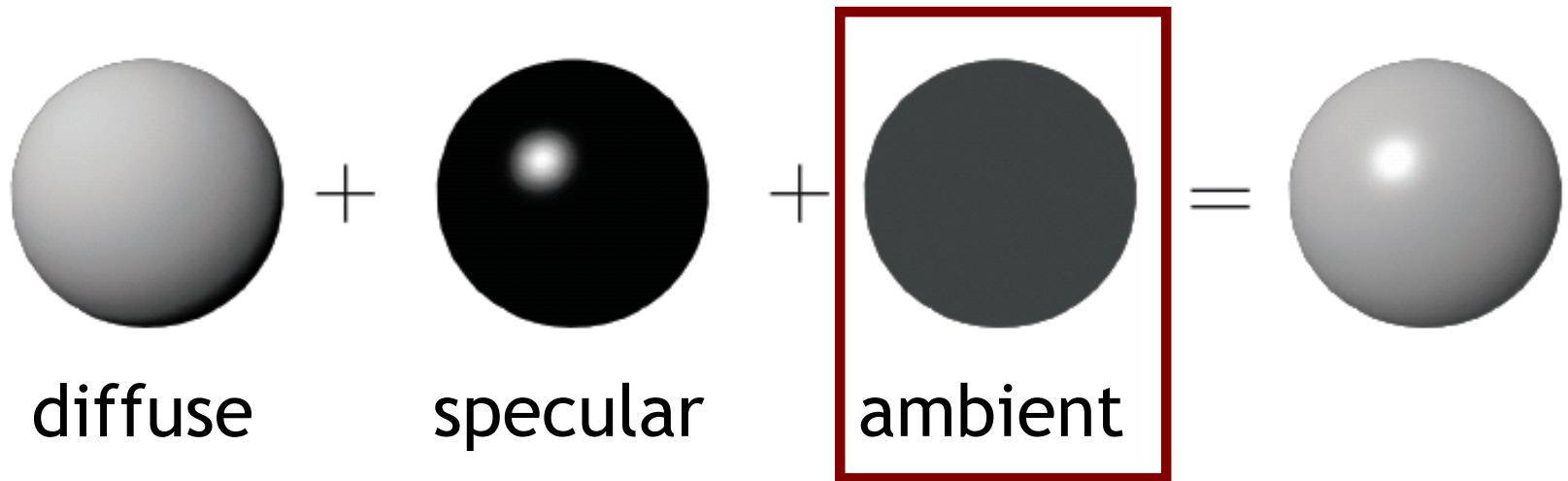
- The larger the angle between microfacet orientation and normal, the less likely
- Use cosine of angle between them
- Shininess parameter s
- Very similar to Phong



Reflected radiance

$$c = c_l k_s (\mathbf{h} \cdot \mathbf{n})^s$$

Simplified model



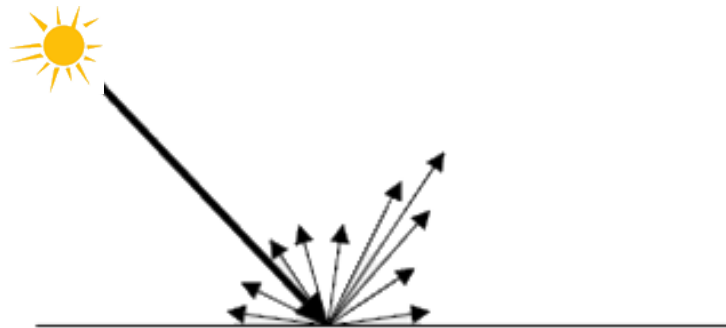
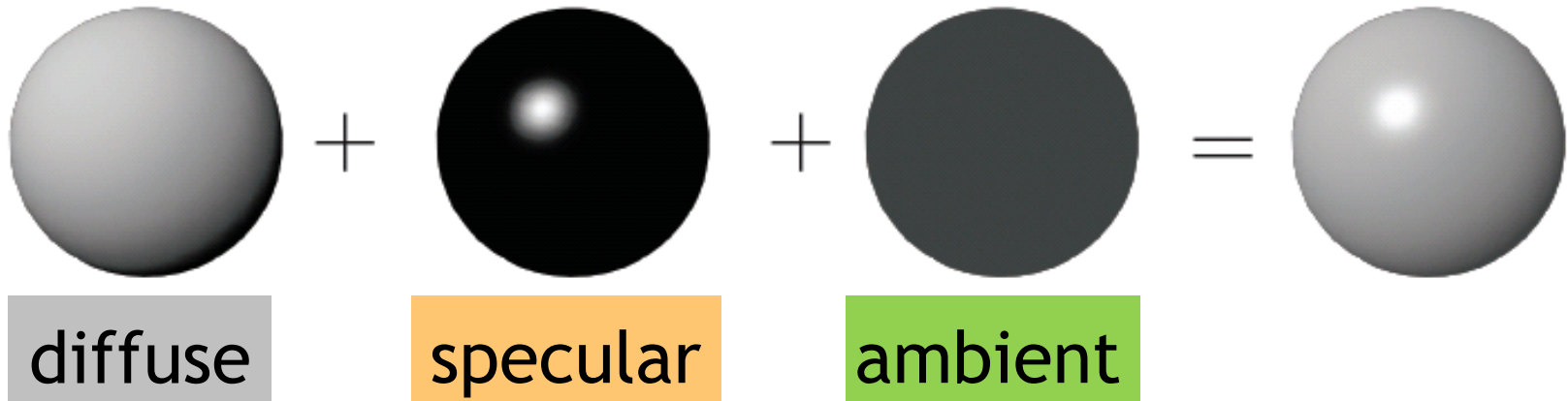
Ambient light

- In real world, light is bounced all around scene
- Could use global illumination techniques to simulate
- Simple approximation
 - Add constant ambient light at each point $k_a c_a$
 - Ambient light c_a
 - Ambient reflection coefficient k_a
- Areas with no direct illumination are not completely dark

Complete model

- Blinn model with several light sources i

$$c = \sum_i c_{l_i} (k_d (\mathbf{L}_i \cdot \mathbf{n}) + k_s (\mathbf{h}_i \cdot \mathbf{n})^s) + k_a c_a$$



Notes

$$c = \sum_i c_{l_i} (k_d (\mathbf{L}_i \cdot \mathbf{n}) + k_s (\mathbf{h}_i \cdot \mathbf{n})^s) + k_a c_a$$

- All colors, reflection coefficients have separate values for R,G,B
- Usually, ambient = diffuse coefficient
- For metals, specular = diffuse coefficient
 - Highlight is color of material
- For plastics, specular coefficient = (x,x,x)
 - Highlight is color of light

Today

Shading

- Introduction
- Radiometry & BRDFs
- Local shading models
- Light sources
- Shading strategies

Light sources

- Light sources can have complex properties
 - Geometric area over which light is produced
 - Anisotropy in direction
 - Variation in color
 - Reflective surfaces act as light sources



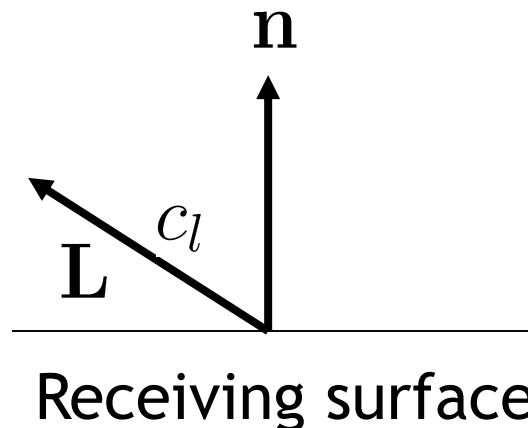
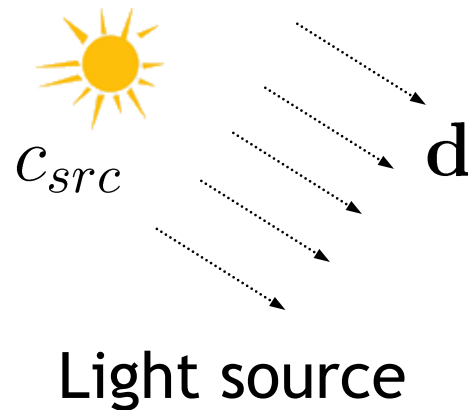
- Interactive rendering is based on simple, standard light sources

Light sources

- At each point on surfaces need to know
 - Direction of incoming light (the \mathbf{L} vector)
 - Radiance of incoming light (the c_l values)
- Standard, simplified light sources
 - **Directional**: from a specific direction
 - **Point light source**: from a specific point
 - **Spotlight**: from a specific point with intensity that depends on the direction
- No model for light sources with an **area**!

Directional light

- Light from a distant source
 - Light rays are parallel
 - Direction and radiance **same everywhere** in 3D scene
 - As if the source were infinitely far away
 - Good approximation to sunlight
- Specified by a unit length direction vector, and a color



$$L = -d$$

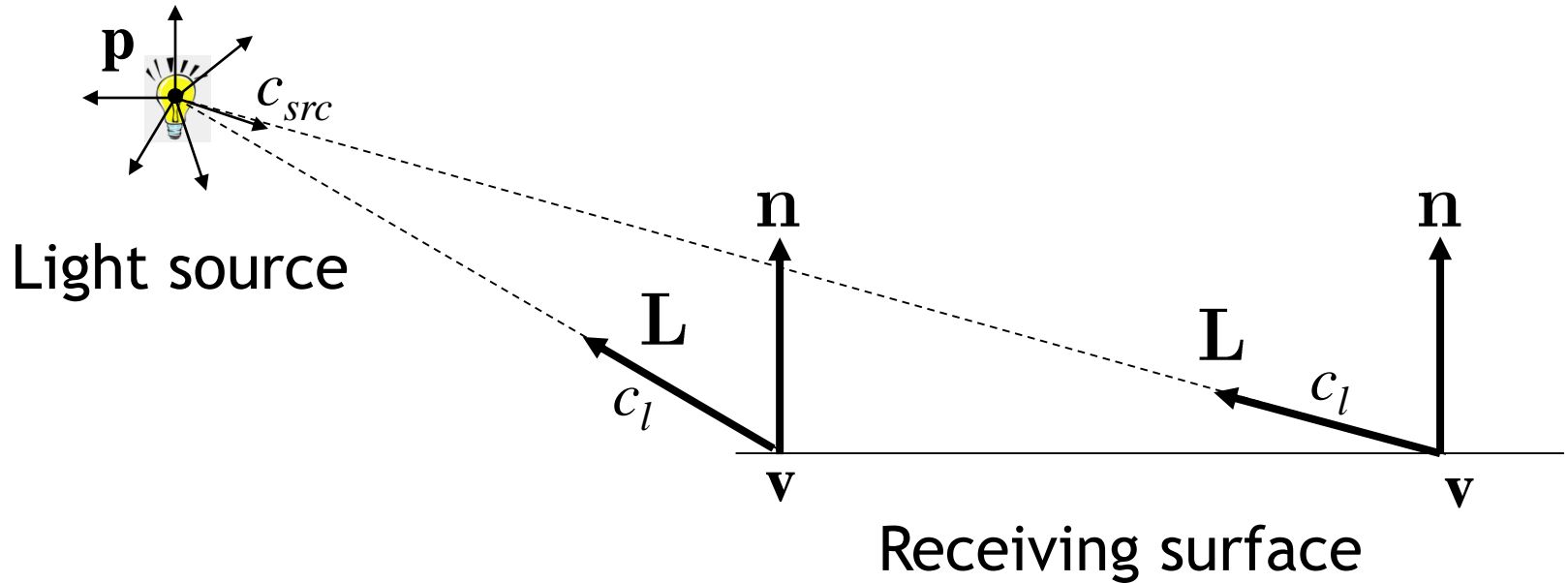
$$c_l = c_{src}$$

Point lights

- Simple model for light bulbs
- **Infinitesimal point** that radiates light in all directions equally
 - Light vector varies across the surface
 - Radiance drops off proportionally to the inverse square of the distance from the light
 - Intuition for inverse square falloff?
- Not physically plausible!



Point lights



Incident light direction

$$\mathbf{L} = \frac{\mathbf{p} - \mathbf{v}}{\|\mathbf{p} - \mathbf{v}\|}$$

Radiance

$$c_l = \frac{c_{src}}{\|\mathbf{p} - \mathbf{v}\|^2}$$

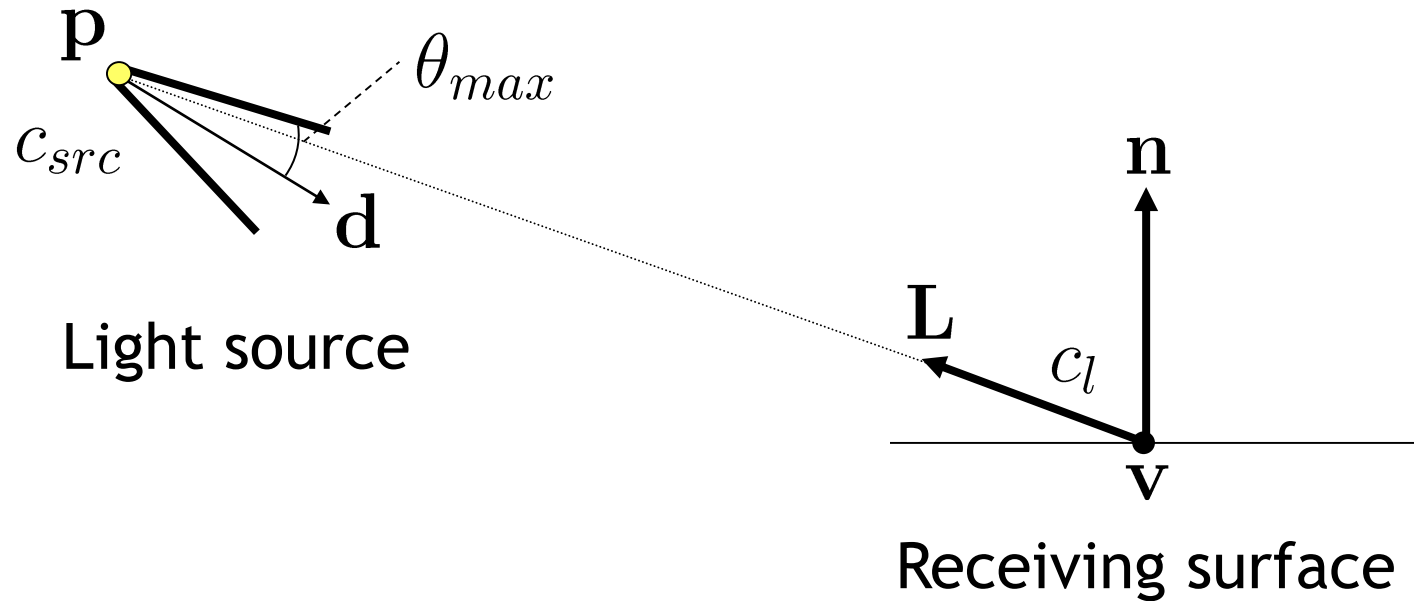
Spotlights

- Like point source, but radiance depends on direction

Parameters

- Position, the location of the source
- Spot direction, the center axis of the light
- Falloff parameters
 - how broad the beam is (cone angle θ_{max})
 - how light tapers off at edges of the beam (cosine exponent f)

Spotlights



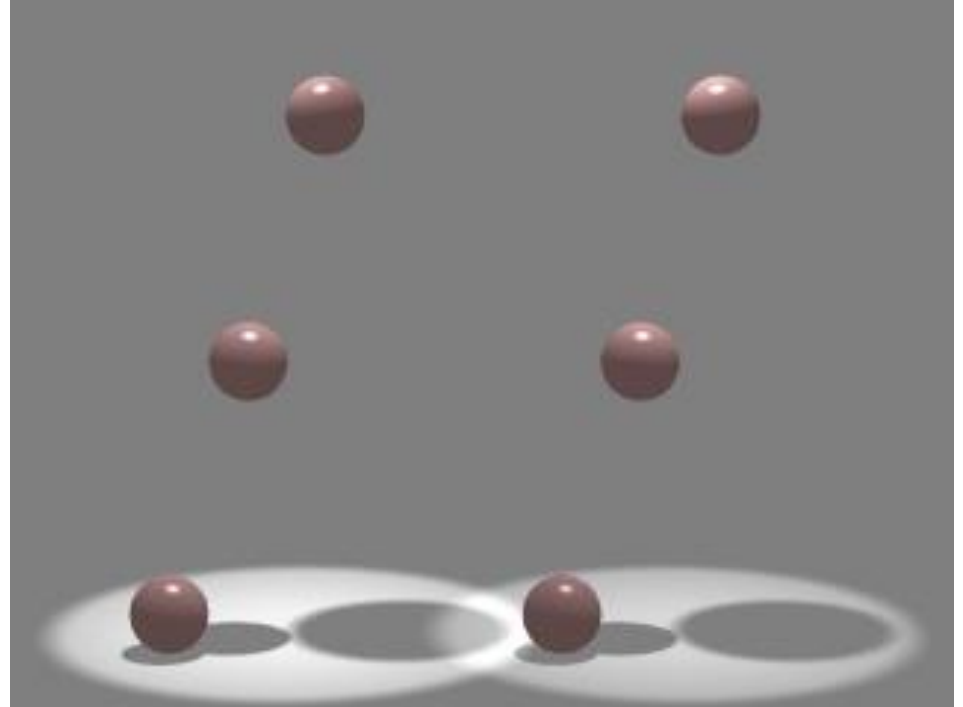
$$\mathbf{L} = \frac{\mathbf{p} - \mathbf{v}}{\|\mathbf{p} - \mathbf{v}\|}$$

$$c_l = \begin{cases} 0 & \text{if } -\mathbf{L} \cdot \mathbf{d} \leq \cos(\theta_{max}) \\ c_{src} (-\mathbf{L} \cdot \mathbf{d})^f & \text{otherwise} \end{cases}$$

Spotlights



Photograph of spotlight



Spotlights in OpenGL

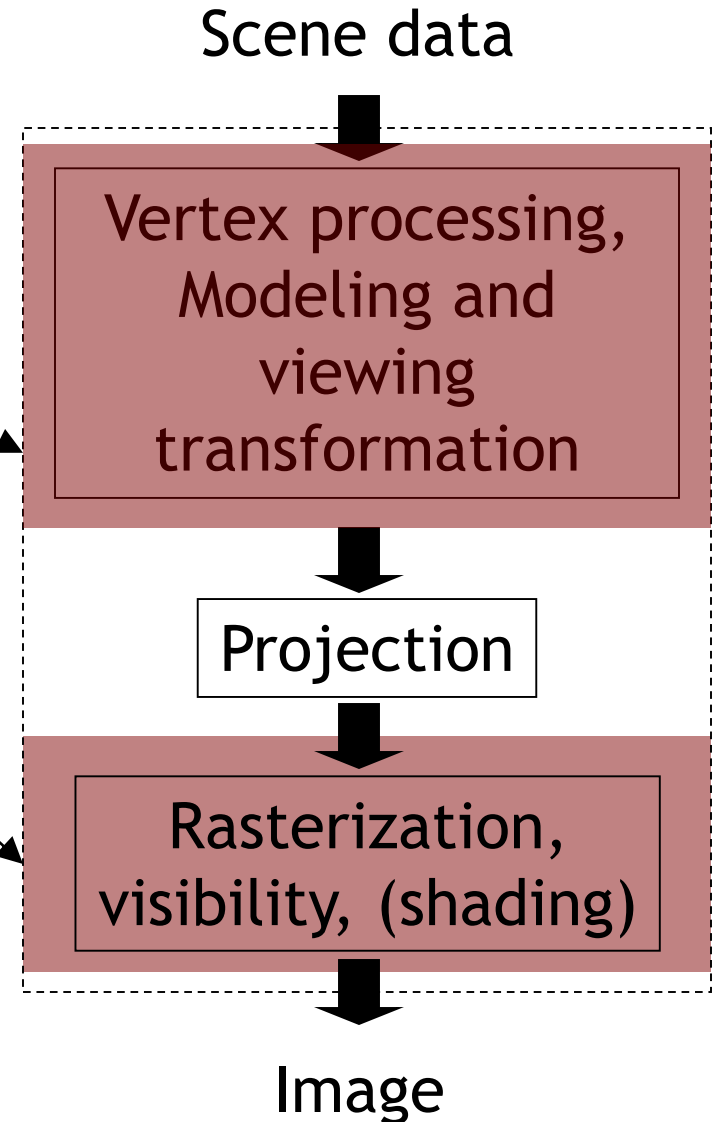
Today

Shading

- Introduction
- Radiometry & BRDFs
- Local shading models
- Light sources
- Shading strategies

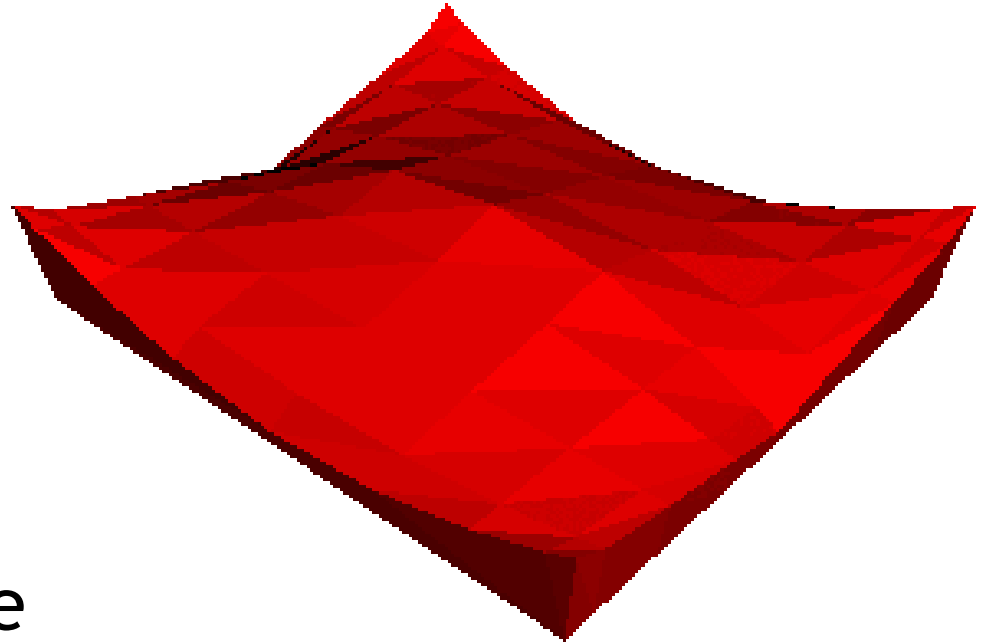
Per-triangle, -vertex, -pixel shading

- May compute shading operations
 - Once per triangle
 - Once per vertex
 - Once per pixel



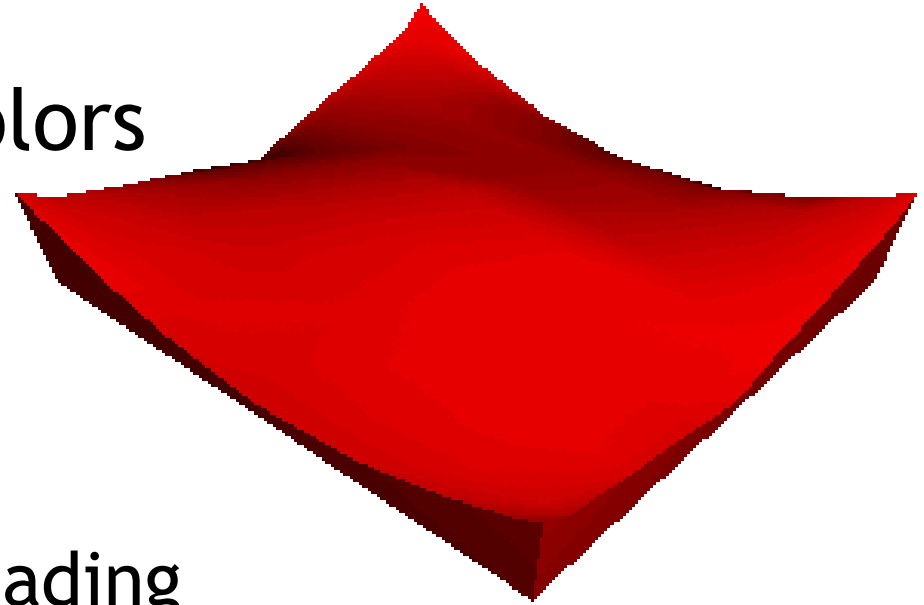
Per-triangle shading

- Known as **flat shading**
- Evaluate shading once per triangle using per-triangle normal
- Advantages
 - Fast
- Disadvantages
 - Faceted appearance



Per-vertex shading

- Known as **Gouraud shading** (Henri Gouraud 1971)
- Per-vertex normals
- Interpolate vertex colors across triangles
- Advantages
 - Fast
 - Smoother than flat shading
- Disadvantages
 - Problems with small highlights

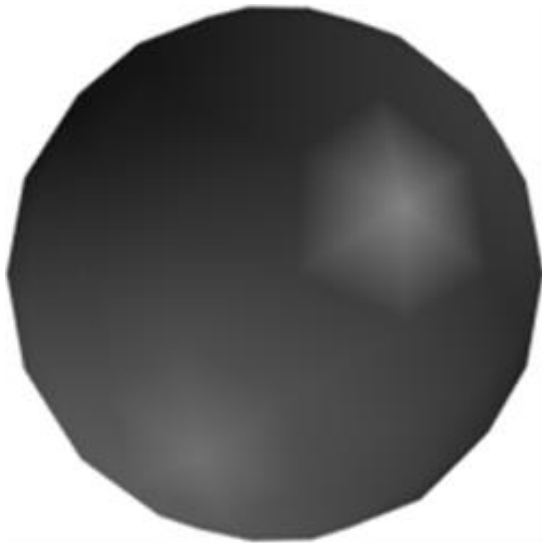


Per-pixel shading

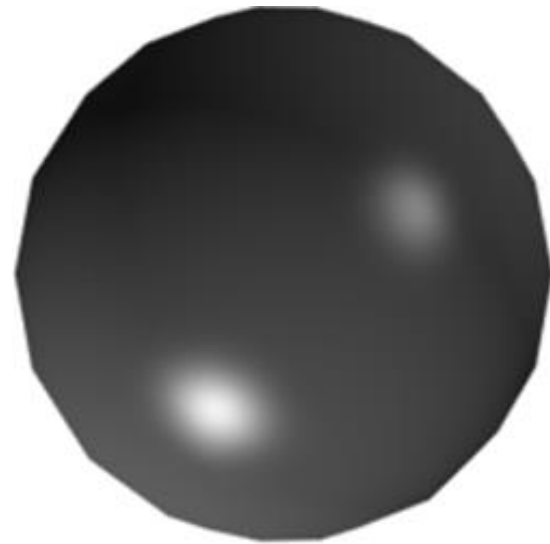
- Also known as **Phong interpolation** (not to be confused with Phong illumination model)
 - Rasterizer interpolates normals across triangles
 - Illumination model evaluated at each pixel
 - Implemented using **programmable shaders** (**next week**)
- Advantages
 - Higher quality than Gouraud shading
- Disadvantages
 - Much slower, but no problem for today's GPUs

Gouraud vs. per-pixel shading

- Gouraud has problems with highlights
- Could use more triangles...



Gouraud



Per-pixel,
same triangles

What about shadows?

- Standard shading assumes light sources are **visible everywhere**
 - Does not determine if light is blocked
 - **No shadows!**
- Shadows require additional work
- Later in the course

What about textures?

- How to combine „colors“ stored in textures and lighting computations?
- Interpret textures as shading coefficients
- Usually, texture used as ambient and diffuse reflectance coefficient k_d , k_a
- Textures provide **spatially varying** BRDFs
 - Each point on surface has different BRDF parameters, different appearance

Summary

- Local illumination (single bounce) is computed using BRDF
- BRDF captures appearance of a material
 - Amount of reflected light for each pair of light/viewing directions
- Simplified model for BRDF consists of diffuse + Phong/Blinn + ambient
 - Lambert's law for diffuse surfaces
 - Microfacet model for specular part
 - Ambient to approximate multiple bounces
- Light source models
 - Directional
 - Point, spot, inverse square fall-off
- Different shading strategies
 - Per triangle, Gouraud, per pixel

Next time

- Programmable shaders