

BILL, RECORD LECTURE!!!!

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Van Der Warden's (VDW) Thm

Exposition by William Gasarch

June 2, 2026

VDW's Thm

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$a, a + d, \dots, a + (k - 1)d$ are all the same color

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We will determine W later.

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1. Within one block.
2. If we take enough blocks, how they relate.

Within a Block

Def: $a, a + d, a + 2d$ is an **almost mono 3AP** if $\text{COL}(a) = \text{COL}(a + d) \neq \text{COL}(a + 2d)$. The **color of an almost mono 3AP** is $\text{COL}(a) = \text{COL}(a + d)$.

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Look at the first three elements of a block of 5:

1. **RRR** or **BBB**. 1-2-3 is mono 3AP.
2. **RBR** or **BRB**. 1-3-5 is mono 3AP or almost mono 3AP.
3. **RBB** or **BRR**. 2-3-4 is mono 3AP or almost mono 3AP.
4. **BBR** or **RRB**. 1-2-3 is almost mono 3AP.
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So always get a mono 3AP or an almost mono 3AP. Can assume its almost mono 3AP and its **R**.

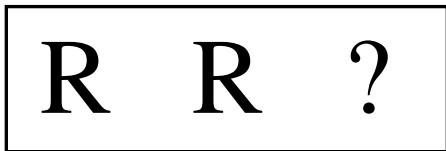
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We can get by with LESS blocks- we will consider this point after the proof.

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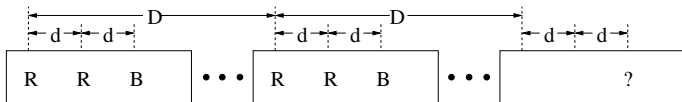
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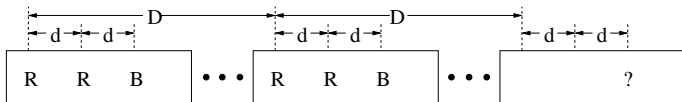


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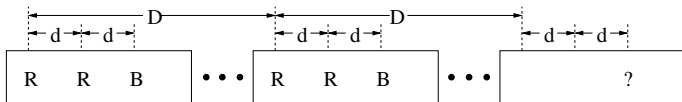
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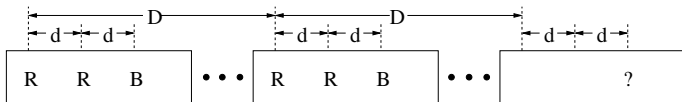
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Done!

Is $W(3, 2) = 365$?

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The few known VDW numbers are **much smaller** than the bounds given by the proof of VDW's Thm.

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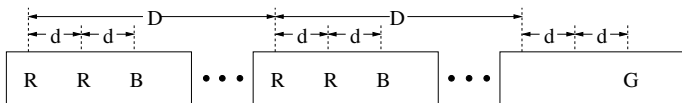
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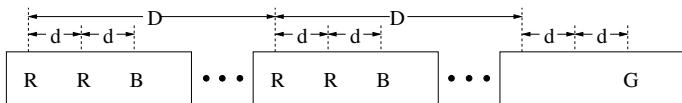
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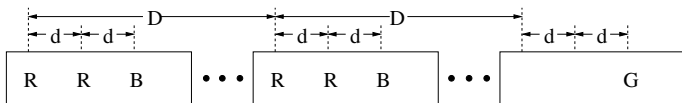
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We have 2 almost mono 3APs of diff colors that same last element.

Need to use Big Blocks

Let W be LOTS of blocks of size $7 \times 2 \times (3^7 + 1)$.

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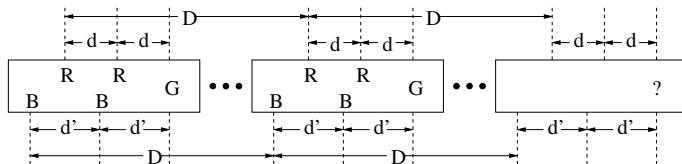
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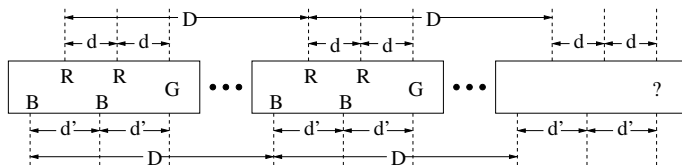


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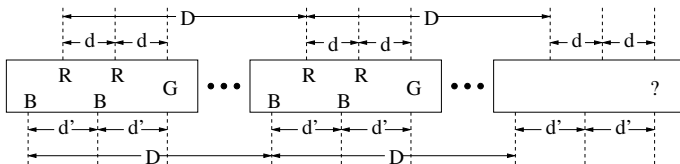
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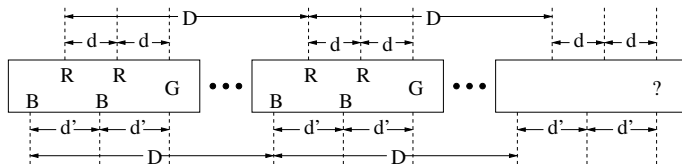
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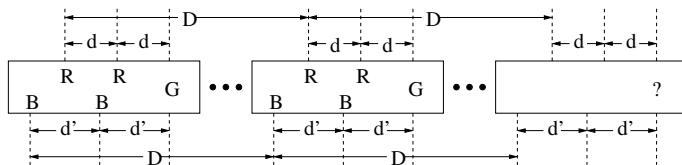
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From what you have seen:

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- ▶ You COULD do a proof that $W(3, 4)$ exists. You would need to iterate what I did twice.
- ▶ There are ways to formalize the proof; however, they are not enlightening.

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Note that we **do not** do

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Induction, But On What?

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There are proofs by induction with better bounds, but still quite large.

Yasmine Remembers This Proof from The Course on Ramsey Theory

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YASMINE When you did this proof you said that since you use big blocks:

I like Big Blocks and I cannot Lie!

BILL I did!

YASMINE You should write a song with that refrain.

BILL I did!

Yasmine Remembers This Proof from The Course on Ramsey Theory

YASMINE When you did this proof you said that since you use big blocks:

I like Big Blocks and I cannot Lie!

BILL I did!

YASMINE You should write a song with that refrain.

BILL I did!

YASMINE Great! Can we hear it?

Yasmine Remembers This Proof from The Course on Ramsey Theory

YASMINE When you did this proof you said that since you use big blocks:

I like Big Blocks and I cannot Lie!

BILL I did!

YASMINE You should write a song with that refrain.

BILL I did!

YASMINE Great! Can we hear it?

BILL I will sing it, for some definition of **sing**.

I Like Big Blocks! (Non Chorus)

I Like Big Blocks! (Non Chorus)

We partition N into block so wide

I Like Big Blocks! (Non Chorus)

We partition N into block so wide

Each Block's got a col-o-ring inside

I Like Big Blocks! (Non Chorus)

We partition N into block so wide

Each Block's got a col-o-ring inside

Encode each block by its own pro-file

I Like Big Blocks! (Non Chorus)

We partition N into block so wide

Each Block's got a col-o-ring inside

Encode each block by its own pro-file

Collapse the colors; compress the style

I Like Big Blocks! (Non Chorus)

We partition N into block so wide

Each Block's got a col-o-ring inside

Encode each block by its own pro-file

Collapse the colors; compress the style

Pigeon-hole says types repeat

I Like Big Blocks! (Non Chorus)

We partition N into block so wide

Each Block's got a col-o-ring inside

Encode each block by its own pro-file

Collapse the colors; compress the style

Pigeon-hole says types repeat

Now look at blocks, and take a seat.

I Like Big Blocks! (Non Chorus)

We partition N into block so wide

Each Block's got a col-o-ring inside

Encode each block by its own pro-file

Collapse the colors; compress the style

Pigeon-hole says types repeat

Now look at blocks, and take a seat.

Ind-uction hums

I Like Big Blocks! (Non Chorus)

We partition N into block so wide

Each Block's got a col-o-ring inside

Encode each block by its own pro-file

Collapse the colors; compress the style

Pigeon-hole says types repeat

Now look at blocks, and take a seat.

Ind-uction hums

The gears all click

I Like Big Blocks! (Non Chorus)

We partition N into block so wide

Each Block's got a col-o-ring inside

Encode each block by its own pro-file

Collapse the colors; compress the style

Pigeon-hole says types repeat

Now look at blocks, and take a seat.

Ind-uction hums

The gears all click

ω^2 —What a trick!

I Like Big Blocks! (Chorus)

I Like Big Blocks! (Chorus)

I like big blocks and I cannot lie!

I Like Big Blocks! (Chorus)

I like big blocks and I cannot lie!

You other math folks can't deny!

I Like Big Blocks! (Chorus)

I like big blocks and I cannot lie!

You other math folks can't deny!

With finitely many colors that you choose

I Like Big Blocks! (Chorus)

I like big blocks and I cannot lie!

You other math folks can't deny!

With finitely many colors that you choose

There's a mono AP that you can't refuse.

I Like Big Blocks! (Non Chorus)

I Like Big Blocks! (Non Chorus)

Color red-blue? Or three or more?

I Like Big Blocks! (Non Chorus)

Color red-blue? Or three or more?

Doesn't matter– same encore

I Like Big Blocks! (Non Chorus)

Color red-blue? Or three or more?

Doesn't matter– same encore

Hide your patterns, try to duck,

I Like Big Blocks! (Non Chorus)

Color red-blue? Or three or more?

Doesn't matter– same encore

Hide your patterns, try to duck,

Regularity brings the luck

I Like Big Blocks! (Non Chorus)

Color red-blue? Or three or more?

Doesn't matter– same encore

Hide your patterns, try to duck,

Regularity brings the luck

A Length-k run in one shade

I Like Big Blocks! (Non Chorus)

Color red-blue? Or three or more?

Doesn't matter— same encore

Hide your patterns, try to duck,

Regularity brings the luck

A Length- k run in one shade

Its a combinatorial serenade!

I Like Big Blocks! (Final Chorus)

I Like Big Blocks! (Final Chorus)

I like big blocks and I cannot lie!

I Like Big Blocks! (Final Chorus)

I like big blocks and I cannot lie!

Mono APs you can't deny.

I Like Big Blocks! (Final Chorus)

I like big blocks and I cannot lie!

Mono APs you can't deny.

With giant blocks and recursive tracks

I Like Big Blocks! (Final Chorus)

I like big blocks and I cannot lie!

Mono APs you can't deny.

With giant blocks and recursive tracks

Van der Waerden's got your back.

I Like Big Blocks! (Final Chorus)

I like big blocks and I cannot lie!

Mono APs you can't deny.

With giant blocks and recursive tracks

Van der Waerden's got your back.
(Applause if deserved.)

How Much Time?

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YASMINE How much time did you spend on that?

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BILL Longer than it took to do admissions for REU-CAAR.

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have disproved the Erdos unit distance conjecture before OpenAI
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BILL I may not win a Turing Award, but I have a shot at being inducted into the Rock and Roll Hall of fame, along with fellow rappers **Jay Z** and **Enimen**, and **Notorious B.I.G.**

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The End

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