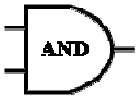
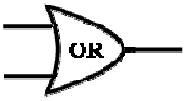
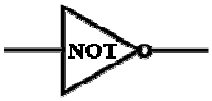
Circuits

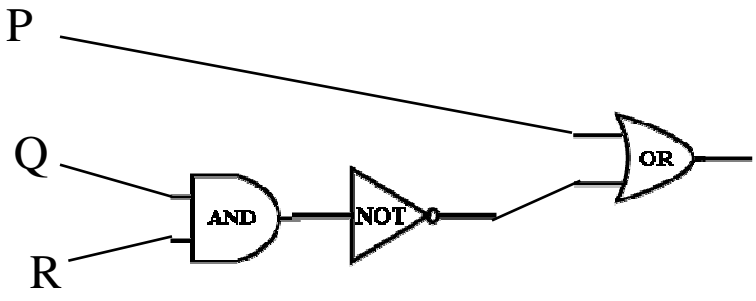
- and gate 

- or gate 

- not gate 

Combining & Determining I/O Relationship

- **P ∨ ~ (Q ^ R)**



Draw the Circuit for:

P,Q&R are inputs

Simplify before building the circuit

P	Q	R	Output
1	1	1	1
1	1	0	1
1	0	1	0
1	0	0	1
0	1	1	0
0	1	0	0
0	0	1	0
0	0	0	0

Number Conversions

- Base of the Number System
  - 10 (decimal), 2 (binary), 8 (octal), 16 (hexadecimal)
  - tells how many different numerals are used
  - determines the value of each place
- Conversions from anything to Base 10
  - use the definition of the number system
- Conversions from Base 10 to anything
  - use repeated integer division

Addition of Binary Numbers

- Carry if the number would be too large for the number system -- if it is greater than 1

1001	1001	1011	1101
+ 10	+ 11	+ 11	+111
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Addition of Oct and Hex Numbers

- Carry if the number would be too large for the number system (larger than 7 or 15)

723_8	265_8	ABC_{16}	CDE_{16}
$+12_8$	$+ 33_8$	$+ 12_{16}$	$+ED_{16}$
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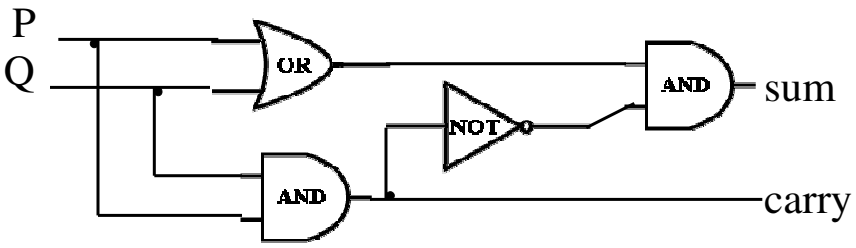
Using a Circuit for Addition

- Write as a Logic Expression
- Translate to Circuits

input		output	
P	Q	Carry	Sum
0	0	0	0
0	1	0	1
1	0	0	1
1	1	1	0

Half Adder

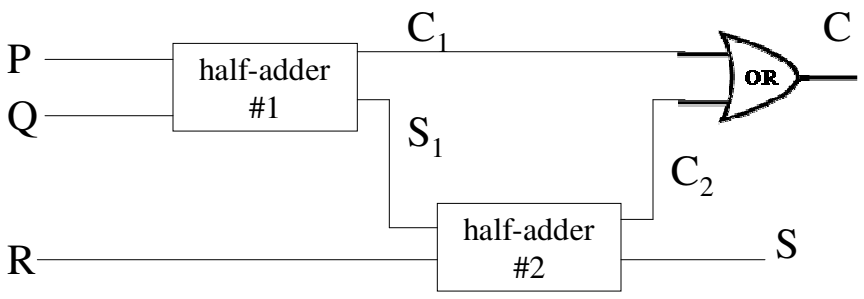


P and Q are binary values (1 bit each)

sum = (P v Q) ^ ~(P ^ Q)

carry = (P ^ Q)

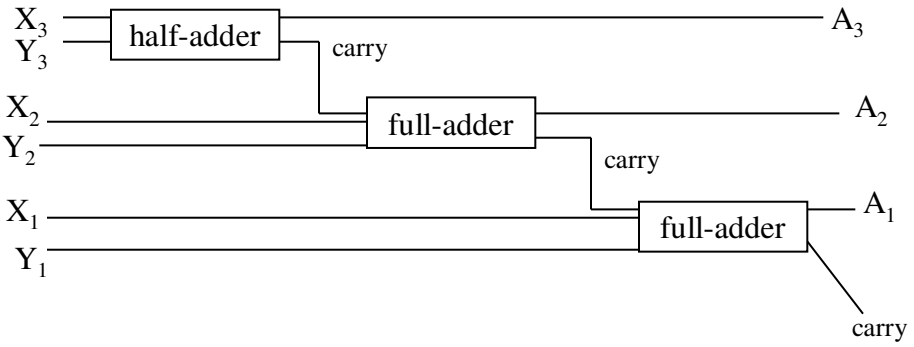
Full Adder



- P Q and R are binary digits
- P + Q + R gives sum value and carry value

Parallel Adders

- Chain these half adders and full adders together for multi-bit addition
- $X_1X_2X_3 + Y_1Y_2Y_3 = CA_1A_2A_3$



2's Compliment

To Represent Negative Values using Binary

1. Find the binary equivalent of the absolute value.
2. Pad on the left to completely fill the bits.
3. Switch all of the 1's to 0's and 0's to 1's.
4. Add 1 to the result.

i.e.: Find the 8-bit 2's compliment representation of -43.

1. $43_{10} = 101011_2$
2. 00101011_2
3. 11010100_2
4. $11010101_2 = -43_{10}$