

Name & Section Number: \_\_\_\_\_

1. (a) Describe briefly but clearly how to efficiently merge three sorted lists, of sizes  $m_1 \leq m_2 \leq m_3$ , into a single sorted list. Try to minimize the number of comparisons under the assumption that  $m_1 \approx m_2 \approx m_3$ , but no proof of optimality required.

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- (b) Exactly how many comparisons does your algorithm use in the worst case (as a function of  $m_1, m_2, m_3$ ).

2. Consider a MergeSort-like algorithm in which the list of size  $N$  is split into three equal sized lists, each list is sorted recursively, and the three lists are then merged into a single sorted list.
  - (a) Write pseudo-code for your algorithm. You may assume a three-way merge algorithm is available (as described in Question 1). Your algorithm should work even if  $N$  is not nice.
  - (b) Analyze exactly how many comparisons your algorithm uses by drawing out the tree and summing across the rows (as we did in class for standard mergesort). You may assume  $N$  is nice (i.e.,  $N$  is a power of 3).

- (c) Write a recurrence for exactly how many comparisons your algorithm uses under the assumption that  $N$  is nice (i.e.,  $N$  is a power of 3).

- (d) Write a recurrence for exactly how many comparisons your algorithm uses without assuming  $N$  is nice.