

CMSC 330: Organization of Programming Languages

OCaml 2 Higher Order Functions

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1

Anonymous Functions

- ▶ Passing functions around is very common
 - So often we don't want to bother to give them names
- ▶ Use `fun` to make a function with no name

Parameter  `fun x -> x + 3`  Body

`(fun x -> x + 3) 5` = 8

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2

All Functions Are Anonymous

- ▶ Functions are first-class, so you can bind them to other names as you like

```
let f x = x + 3
let g = f
g 5 = 8
```

- ▶ In fact, `let` for functions is just shorthand

```
let f x = body
```



stands for

```
let f = fun x -> body
```



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3

Examples

- ▶ `let next x = x + 1`
 - Short for `let next = fun x -> x + 1`
- ▶ `let plus (x, y) = x + y`
 - Short for `let plus = fun (x, y) -> x + y`
 - Which is short for
 - ▶ `let plus = fun z ->`
`(match z with (x, y) -> x + y)`
- ▶ `let rec fact n =`
`if n = 0 then 1 else n * fact (n-1)`
 - Short for `let rec fact = fun n ->`
`(if n = 0 then 1 else n * fact (n-1))`

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4

Higher-Order Functions

- In OCaml you can pass functions as arguments, and return functions as results

```
let plus_three x = x + 3
let twice f z = f (f z)
twice plus_three 5
twice : ('a->'a) -> 'a -> 'a

let plus_four x = x + 4
let pick_fn n =
  if n > 0 then plus_three else plus_four
(pick_fn 5) 0
pick_fn : int -> (int->int)
```

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5

Currying

- We just saw a way for a function to take multiple arguments
 - The function consumes one argument at a time, returning a function that takes the rest
- This is called **currying** the function
 - Named after the logician Haskell B. Curry
 - But Schönfinkel and Frege discovered it
 - So it should probably be called Schönfinkelizing or Fregging

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6

Curried Functions In OCaml

- ▶ OCaml has a really simple syntax for currying

```
let add x y = x + y
```

- This is identical to all of the following:

```
let add = (fun x -> (fun y -> x + y))  
let add = (fun x y -> x + y)  
let add x = (fun y -> x+y)
```

- ▶ Thus:

- `add` has type `int -> (int -> int)`
- `add 3` has type `int -> int`
 - `add 3` is a function that adds 3 to its argument
- `(add 3) 4 = 7`

- ▶ This works for any number of arguments

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7

Curried Functions In OCaml (cont.)

- ▶ Because currying is so common, OCaml uses the following conventions:

- `->` associates to the right
 - Thus `int -> int -> int` is the same as
➢ `int -> (int -> int)`
- function application associates to the left
 - Thus `add 3 4` is the same as
➢ `(add 3) 4`

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8

Another Example Of Currying

- ▶ A curried add function with three arguments:

```
let add_th x y z = x + y + z
```

- The same as

```
let add_th x = (fun y -> (fun z -> x+y+z))
```

- ▶ Then...

- `add_th` has type `int -> (int -> (int -> int))`
- `add_th 4` has type `int -> (int -> int)`
- `add_th 4 5` has type `int -> int`
- `add_th 4 5 6` is `15`

Implementing This Is Challenging!

- ▶ Implementing functions that return other functions requires a clever data structure called a **closure**
 - We'll see how these are implemented later
- ▶ In the meantime, we will explore using higher order functions, and then discuss how they are implemented

The Map Function

- ▶ Let's write the `map` function (like Ruby's `collect`)
 - Takes a function and a list, applies the function to each element of the list, and returns a list of the results

```
let rec map f l = match l with
  [] -> []
  | (h::t) -> (f h)::(map f t)
```

```
let add_one x = x + 1
let negate x = -x
map add_one [1; 2; 3]
map negate [9; -5; 0]
```

- ▶ Type of `map`?

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11

The Map Function (cont.)

- ▶ What is the type of the map function?

```
let rec map f l = match l with
  [] -> []
  | (h::t) -> (f h)::(map f t)
```

$$\underbrace{('a \rightarrow 'b)}_f \rightarrow \underbrace{'a \text{ list}}_l \rightarrow 'b \text{ list}$$

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12

Pattern Matching With Fun

- ▶ `match` can be used within `fun`

```
map (fun l -> match l with (h::_) -> h)
    [ [1; 2; 3]; [4; 5; 6; 7]; [8; 9] ]
    = [1; 4; 8]
```

- ▶ But use named functions for complicated matches
- ▶ May use standard pattern matching abbreviations

```
map (fun (x, y) -> x+y) [(1,2); (3,4)]
    = [3; 7]
```

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13

The Fold Function

- ▶ Common pattern

- Iterate through list and apply function to each element, keeping track of partial results computed so far

```
let rec fold f a l = match l with
  [] -> a
  | (h::t) -> fold f (f a h) t
```

- `a` = “accumulator”
 - Usually called **fold left** to remind us that `f` takes the accumulator as its first argument
- ▶ What's the type of `fold`?
`= ('a -> 'b -> 'a) -> 'a -> 'b list -> 'a`

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14

Example

```
let rec fold f a l = match l with  
  [] -> a  
  | (h::t) -> fold f (f a h) t
```

```
let add a x = a + x  
fold add 0 [1; 2; 3; 4] →  
fold add 1 [2; 3; 4] →  
fold add 3 [3; 4] →  
fold add 6 [4] →  
fold add 10 [] →  
10
```

We just built the `sum` function!

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15

Another Example

```
let rec fold f a l = match l with  
  [] -> a  
  | (h::t) -> fold f (f a h) t
```

```
let next a _ = a + 1  
fold next 0 [2; 3; 4; 5] →  
fold next 1 [3; 4; 5] →  
fold next 2 [4; 5] →  
fold next 3 [5] →  
fold next 4 [] →  
4
```

We just built the `length` function!

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16

Using Fold to Build Reverse

```
let rec fold f a l = match l with
  [] -> a
  | (h::t) -> fold f (f a h) t
```

- Can you build the **reverse** function with **fold**?

```
let prepend a x = x::a
fold prepend [] [1; 2; 3; 4] →
fold prepend [1] [2; 3; 4] →
fold prepend [2; 1] [3; 4] →
fold prepend [3; 2; 1] [4] →
fold prepend [4; 3; 2; 1] [] →
[4; 3; 2; 1]
```

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17

Currying Is Standard In OCaml

- Pretty much all functions are curried
 - Like the standard library **map**, **fold**, etc.
 - See </usr/local/ocaml/lib> on linuxlab
 - In particular, look at the file **list.ml** for standard list functions
 - Access these functions using **List.<fn name>**
 - E.g., **List.hd**, **List.length**, **List.map**
- OCaml works hard to make currying efficient
 - Otherwise it would do a lot of useless allocation of closures (which we see later) when all arguments are provided

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18

A Convention

- ▶ Since functions are curried, **function** can often be used instead of **match**

- **function** declares an anonymous function of one argument
- Instead of

```
let rec sum l = match l with  
  [] -> 0  
  | (h::t) -> h + (sum t)
```

- It could be written

```
let rec sum = function  
  [] -> 0  
  | (h::t) -> h + (sum t)
```

A Convention (cont.)

Instead of

```
let rec map f l = match l with  
  [] -> []  
  | (h::t) -> (f h)::(map f t)
```

It could be written

```
let rec map f = function  
  [] -> []  
  | (h::t) -> (f h)::(map f t)
```

Nested Functions

- In OCaml, you can define functions anywhere
 - Even inside of other functions

```
let sum l =  
  fold (fun a x -> a + x) 0 l
```

```
let pick_one n =  
  if n > 0 then (fun x -> x + 1)  
  else (fun x -> x - 1)  
(pick_one -5) 6    (* returns 5 *)
```

Nested Functions (cont.)

- You can also use `let` to define functions inside of other functions

```
let sum l =  
  let add a x = a + x in  
  fold add 0 l
```

```
let pick_one n =  
  let add_one x = x + 1 in  
  let sub_one x = x - 1 in  
  if n > 0 then add_one else sub_one
```

How About This?

```
let addN n l =  
  let add x = n + x in  
  map add l
```

Accessing variable
from outer scope

- (Equivalent to...)

```
let addN n l =  
  map (fun x -> n + x) l
```

Returned Functions

- In OCaml a function can return another function as a result; this is what currying is doing

- Consider the following example

```
let addN n = (fun x -> x + n)  
(addN 3) 4 (* returns 7 *)
```

- When the anonymous function is called, `n` isn't even on the stack any more!
 - We need some way to keep `n` around after `addN` returns

The Call Stack in C/Java/etc.

```
void f(void) {
    int x;
    x = g(3);
}

int g(int x) {
    int y;
    y = h(x);
    return y;
}

int h(int z) {
    return z + 1;
}

int main() {
    f();
    return 0;
}
```

x	4	f
x	3	g
y	4	g
z	3	h

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25

Now Consider Returning Functions

```
let map f n = match n with
[] -> []
| (h::t) -> (f h)::(map f t)

let addN n l =
    let add x = n + x in
    map add l
```

addN 3 [1; 2; 3]

n	3	
l		<list>
f		<add>
n		
x	1	

- Uh oh...how does **add** know the value of **n**?
 - OCaml does **not** read it off the stack
 - The language could do this, but can be confusing (see above)
 - OCaml uses **static scoping** like C, C++, Java, and Ruby

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26

Static Scoping (AKA Lexical Scoping)

- ▶ In **static** or **lexical scoping**, (nonlocal) names refer to their nearest binding in the program text
 - Going from inner to outer scope
 - In our example, **add** refers to **addN**'s **n**
 - C example:

Refers to the **x** at file scope – that's the nearest **x** going from inner scope to outer scope in the source code

```
int x;  
void f() { x = 3; }  
void g() { char *x = "hello"; f(); }
```

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27

Closures Implement Static Scoping

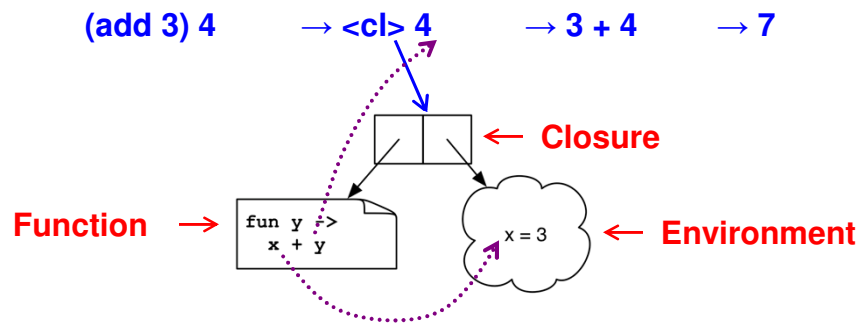
- ▶ An **environment** is a mapping from variable names to values
 - Just like a stack frame
- ▶ A **closure** is a pair (**f**, **e**) consisting of function code **f** and an environment **e**
- ▶ When you invoke a closure, **f** is evaluated using **e** to look up variable bindings

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28

Example – Closure 1

```
let add x = (fun y -> x + y)
```

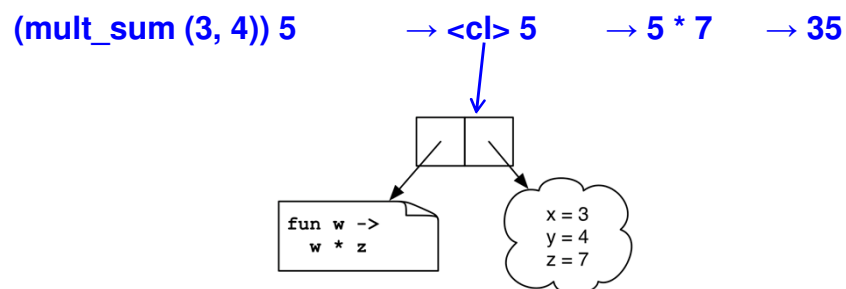


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29

Example – Closure 2

```
let mult_sum (x, y) =  
  let z = x + y in  
  fun w -> w * z
```

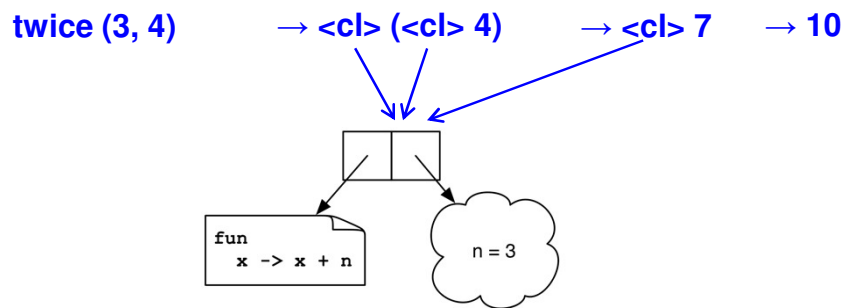


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30

Example – Closure 3

```
let twice (n, y) =
  let f x = x + n in
  f (f y)
```

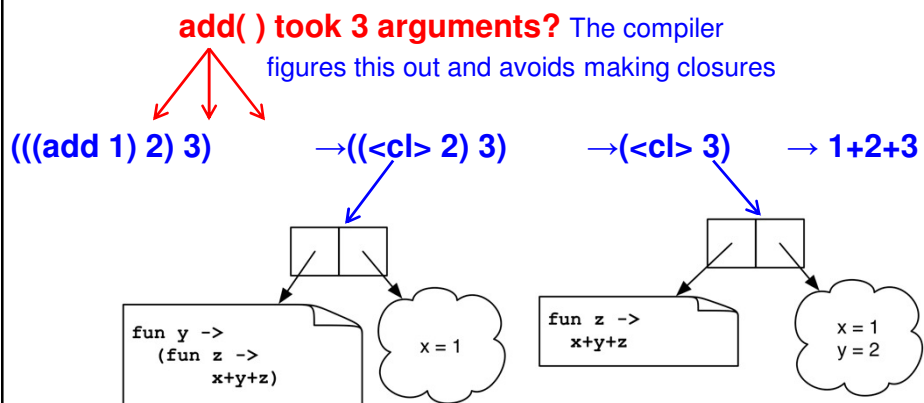


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31

Example – Closure 4

```
let add x = (fun y -> (fun z -> x + y + z))
```



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32

Higher-Order Functions in C

- C supports **function pointers**

```
typedef int (*int_func)(int);
void app(int_func f, int *a, int n) {
    for (int i = 0; i < n; i++)
        a[i] = f(a[i]);
}
int add_one(int x) { return x + 1; }
int main() {
    int a[] = {5, 6, 7};
    app(add_one, a, 3);
}
```

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33

Higher-Order Functions in C (cont.)

- C does not support closures
 - Since no nested functions allowed
 - Unbound symbols always in global scope

```
int y = 1;
void app(int (*f)(int), n) {
    return f(n);
}
int add_y(int x) {
    return x + y;
}
int main() {
    app(add_y, 2);
}
```

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34

Higher-Order Functions in C (cont.)

- ▶ Cannot access non-local variables in C
- ▶ OCaml code

```
let add x y = x + y
```

- ▶ Equivalent code in C is illegal

```
int (* add(int x))(int) {  
    return add_y;  
}  
int add_y(int y) {  
    return x + y; // x undefined  
}
```

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35

Higher-Order Functions in C (cont.)

- ▶ OCaml code

```
let add x y = x + y
```

- ▶ Works if C supports nested functions
 - Not in ISO C, but in gcc; but not allowed to return them

```
int (* add(int x))(int) {  
    int add_y(int y) {  
        return x + y;  
    }  
    return add_y; }  
}
```

- Does not allocate closure, so x popped from stack and add_y will get garbage (potentially) when called

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36

Higher-Order Functions in Ruby

- Ruby supports higher-order functions
 - Use **yield** within method to call **code block** argument

```
def my_collect(a)
  b = Array.new(a.length)
  0.upto(a.length-1) { |i|
    b[i] = yield(a[i])
  }
  return b
end
b = my_collect([5, 6, 7]) { |x| x+1 }
```

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37

Higher-Order Functions in Ruby (cont.)

- Ruby supports closures
 - Code blocks can access non-local variables
 - Binding determined by lexical scoping

```
def twice
  yield
  yield
end
x = 1
twice {x += 1}
puts x # 3
```

```
def twice
  x = 0 #dynamic
  yield
  yield
end
x = 1 #lexical
twice {x += 1}
puts x # 3 not 1
```

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38

Higher-Order Functions in Ruby (cont.)

- Ruby code blocks are actual variables

```
def twice      # implicit block
  yield       # invoked with yield
  yield
end
twice { x += 1 } # same as x += 2
↓
def quad (&block) # explicit block
  twice (&block) # used as argument
  twice (&block)
end
quad { x += 1 } # same as x += 4
```

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39

Higher-Order Functions in Ruby (cont.)

- Code blocks may be saved

```
def quad (&block) # explicit block
  c = block      # no ampersand!
  twice (c)      # used as argument
  twice (c)
end
↓
def twice c      # arg = explicit closure
  c.call         # invoke with .call
  c.call
end
quad { x += 1 } # same as x += 4
```

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40

Higher-Order Functions in Ruby (cont.)

► Ruby supports creating closures directly

- Proc.new
- proc
- lambda
- method

```
c1 = Proc.new { x+=1 }  
c2 = proc      { x+=1 }  
c3 = lambda    { x+=1 }  
def foo  
  x+=1  
end  
c4 = method    { :foo }  
  
↓  
c.call         # x+=1
```

Higher-Order Functions in Java/C++

- An object in Java or C++ is kind of like a closure
- It has some data (like an environment)
 - Along with some methods (i.e., function code)
 - So objects can be used to simulate closures
- So is an anonymous Java inner class
- Inner class methods can access fields of outer class
- Back in CMSC 132 (OOP II)
- We studied how to implement some functional patterns in OO languages