This test is open-book, open-notes, but you may not use any computing device other than your brain and may not communicate with anyone. You have 120 minutes to complete the test.

The phrase “design a program” or “design a function” means follow the steps of the design recipe. Unless specifically asked for, you do not need to provide intermediate products like templates or stubs, though they may be useful to help you construct correct solutions.

You may use any of the data definitions given to you within this exam and do not need to repeat their definitions.

Unless specifically instructed otherwise, you may use any built-in ISL+ functions or data types.

When writing tests, you may use a shorthand for writing check-expects by drawing an arrow between two expressions to mean you expect the first to evaluate to same result as the second. For example, you may write \((\text{add1 3}) \rightarrow 4\) instead of \((\text{check-expect (add1 3) 4})\).
Problem 1 (10 points). For the following program, write out each step of computation. At each step, underline the expression being simplified. Label each step as being “arithmetic” (meaning any built-in operation), “conditional”, “plug” (for plugging in an argument for a function parameter), or “constant” for replacing a constant with its value.

(define S 1)
(define (q z)
  (cond [(< 4 z) (+ z S)]
         [else 9]))
(q 8)
**Problem 2 (10 points).** For the following structure definition, list the names of every function it creates. For each function, classify it as being either a constructor, accessor, or predicate.

```
(define-struct qt (nw ne se sw))
```
Problem 3 (15 points). Consider the following data definition (and examples) for representing sentences:

;; A Sentence is a [NEListof String]

(define sent1 (list "a" "dog" "barked"))
(define sent2 (list "a" "cat" "meowed"))

Recall the following data definition of [NEListof X]:

;; A [NEListof X] is one of:
;; - (cons X '())
;; - (cons X [NEListof X])

Given a Sentence, a bigram is a list of two consecutive elements of the sentence. For example, sent1 has exactly two bigrams:

(list "a" "dog")
(list "dog" "barked")

Using the following data definition,

;; a Bigram is a (list String String)

design a function bigrams which takes a Sentence and returns a list of Bigrams.
**Problem 4 (15 points).** Here is a program that, given a sentence (see problem 3), computes a two element list consisting of the minimal and maximal words according to alphabetic ordering.

```
;;; min-and-max : Sentence -> (list String String)
;;; Produces the min and max words in the sentence.
(check-expect (min-and-max (list "the" "zoo" "has" "aardvarks"))
 (list "aardvarks" "zoo"))
(define (min-and-max s)
  (cond [(empty? (rest s)) (list (first s) (first s))]
         [else
          (local [(define w (first s))
                   (define m+m (min-and-max (rest s)))]
                 (cond [(string<? w (first m+m))
                        (list w (second m+m))]
                       [(string<? (second m+m) w)
                        (list (first m+m) w)]
                       [else m+m))]))))
```

Redesign this program to use an accumulator-based helper function with two accumulators: the minimal and maximal elements of the sentence seen so far.
[Space for problem 4.]
**Problem 5 (15 points).** Design the following program for determining if two sentences (see problem 3) are equal, meaning they are lists of the same length with the same elements (in the same order):

```plaintext
;; sent=? : Sentence Sentence -> Boolean
;; Are the two sentences the same?

(You may not use equal? in the design of this program.)
Problem 6 (15 points). During your internship at the University of Maryland's Center for Bioinformatics and Computational Biology (CBCB), you’re asked to design a program for computing the reverse complement of DNA strands. A DNA strand is an arbitrarily long sequence of bases, which are either: C, G, A, or T. A and T are complements of each other, as are C and G. The reverse complement of a DNA strand is formed by reversing the strand and taking the complement of each symbol. For example, the reverse complement of AAAACCCG GT is ACCG GGT TTTT. Design a program that, given a DNA strand, computes its reverse complement.
Problem 7 (15 points). Design a program that takes two strings and counts how many times the first string occurs within the second. For example,

- "ho" occurs three times in "ho  ho  ho", while
- "ho  ho" occurs once in "ho  ho  ho" (notice that occurrences cannot overlap).

You may assume the first string is non-empty. It may be helpful to use the substring function. Recall: (substring "hello world" 1 5) produces "ello" and (substring "hello world" 4) produces "o world".