Introduction to Algorithms

CMSC 351

Fall 2019

Administration

General Administration:
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Exam Scheduling: Jamie Matthews <jamiem@cs.umd.edu>

Administration (continued)

- Webpage
 - Get homework assignments
 - Syllabus
 - Other documents
- Piazza
 - Ask questions
 - ★ Do not post solutions.
 - ★ Do **not** ask if your answer or approach is correct.
 - Discuss issues
 - Public versus Private
- ELMS
 - Get homework solutions
 - See final grades
- Gradescope
 - Hand in homework
 - See graded homeworks and exams

Administration (continued)

- Textbook (bookstore/on reserve at McKeldin Library)
 - Cormen, Leiserson, Rivest, and Stein, Introduction to Algorithms (3rd ed., 2009). MIT Press. (Any edition is fine.)

Class attendance

- You are responsible for what is said in class.
- ► Laptops and other devices: Do not share during class.
- Lectures will be posted (mostly).
- Office hours
- Exams
 - ► Two evening midterms: **7:00-9:00pm**.
 - * Thursday, October 17th
 - ★ Thursday, November 14th
 - Final exam: 4:00-6:00pm.
 - ★ Friday, December 13th

Administration (continued)

Homework

- Three types
 - ★ Regular: typically due each Friday. (1% each)
 - ★ NP-completeness: typically due every other Wednesday. (1/2% each)
 - ★ Programming project (likely). (4%)
- Must be in PDF.
- Must be easy to read (your responsibility).
- ▶ Late date: 25% off your actual grade.
 - ★ One get-out-of-jail-free card for each type.
- ► Your neighbor should understand your answers.
- ► Study groups.
- Must write up homework solutions yourself.
 - ★ State who is in your study group at top of homework.
 - ★ State what outside resources you used to solve each problem.
- Do problems from book (and other books).
- Grading

Topics (tentative)

- Introduction, Ch. 1,2
- Quadratic sorting algorithms
- Mergesort, Ch. 2
- Summations, Appendix A
- Recurrences, Ch. 4
- Heapsort, Ch. 6
- Quicksort, Ch. 7
- Sorting in Linear Time, Ch. 8
- Medians and Order Statistics, Ch. 9
- Graphs and Trees, Appendix B
- Minimum Spanning Trees, Ch. 23
- Shortest Paths: Dijkstra's algorithm, Ch. 24.3
- Introduction to NP-completeness, Ch. 34



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What is an algorithm?

Definition

An *algorithm* is a finite list of step-by-step instructions for solving a problem.

Efficiency

- Time
- Space

Example

Tournament assignment. (Think about at home.)

Good Algorithms Are Critical

Example

Two sorting algorithms:

- Slow algorithm (bubble sort): $4n^2$ instructions
- Fast algorithm (merge sort): $80n \lg n$ instructions

Two computers:

- Fast computer: 10 billion instructions/second
- Slow computer: 10 million instructions/second

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- Fast algorithm, slow computer: $\approx \frac{1}{2}$ hour

Example

• Slow algorithm, fast computer:

$$\frac{4 \cdot \left(10^7\right)^2 \text{ instructions}}{10^{10} \text{ instructions/second}} = 40000 \text{ secs } \approx 11 \text{ hrs}$$

Fast algorithm, slow computer:

$$\frac{80\cdot 10^7\,\mathrm{lg}\, \left(10^7
ight)\,\,\mathrm{instructions}}{10^7\,\,\mathrm{instructions/second}}\,pprox\,\,1860\,\,\mathrm{secs}\,\,pprox\,\,31\,\,\mathrm{mins}$$

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