

CMSC425 Lecture notes 10/3

Skeletons, rigging and animation

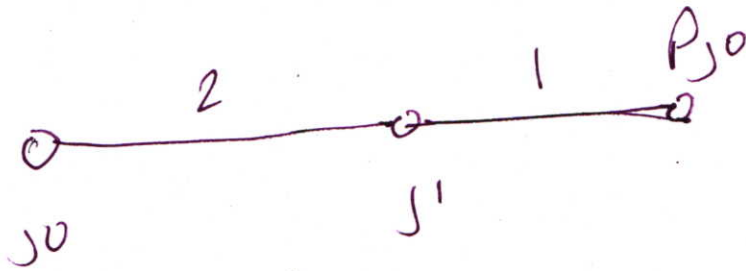
These notes parallel the PowerPoint “Skeletons and Skins”, Day 11.

Pages:

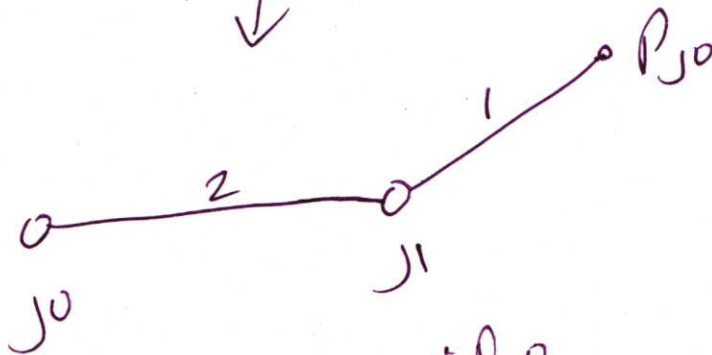
- 1) Three positions of a two joint skeleton with a point P_j0 defined in joint 1 ($j1$) coordinate system. The transform matrix M of the point around the two joints will be in sequence as on the notes.
- 2) Example of an animation file with joint rotations for $J3$, $J4$ and $J5$ over time – the entries in the grid are angles (or I for identify matrix).
- 3) Example of Scene graph for objects on a table – see PowerPoint PDF for example
- 4) Example of joint rotations embedded in larger world coordinate system.

Position

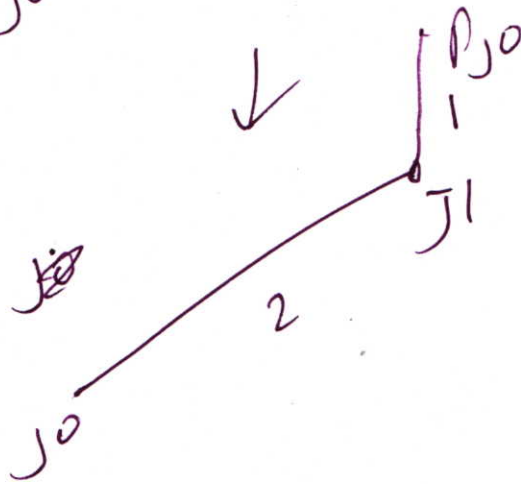
(A)



(B)



(C)



$$P_{j0} = (1, 0)$$

(J1)

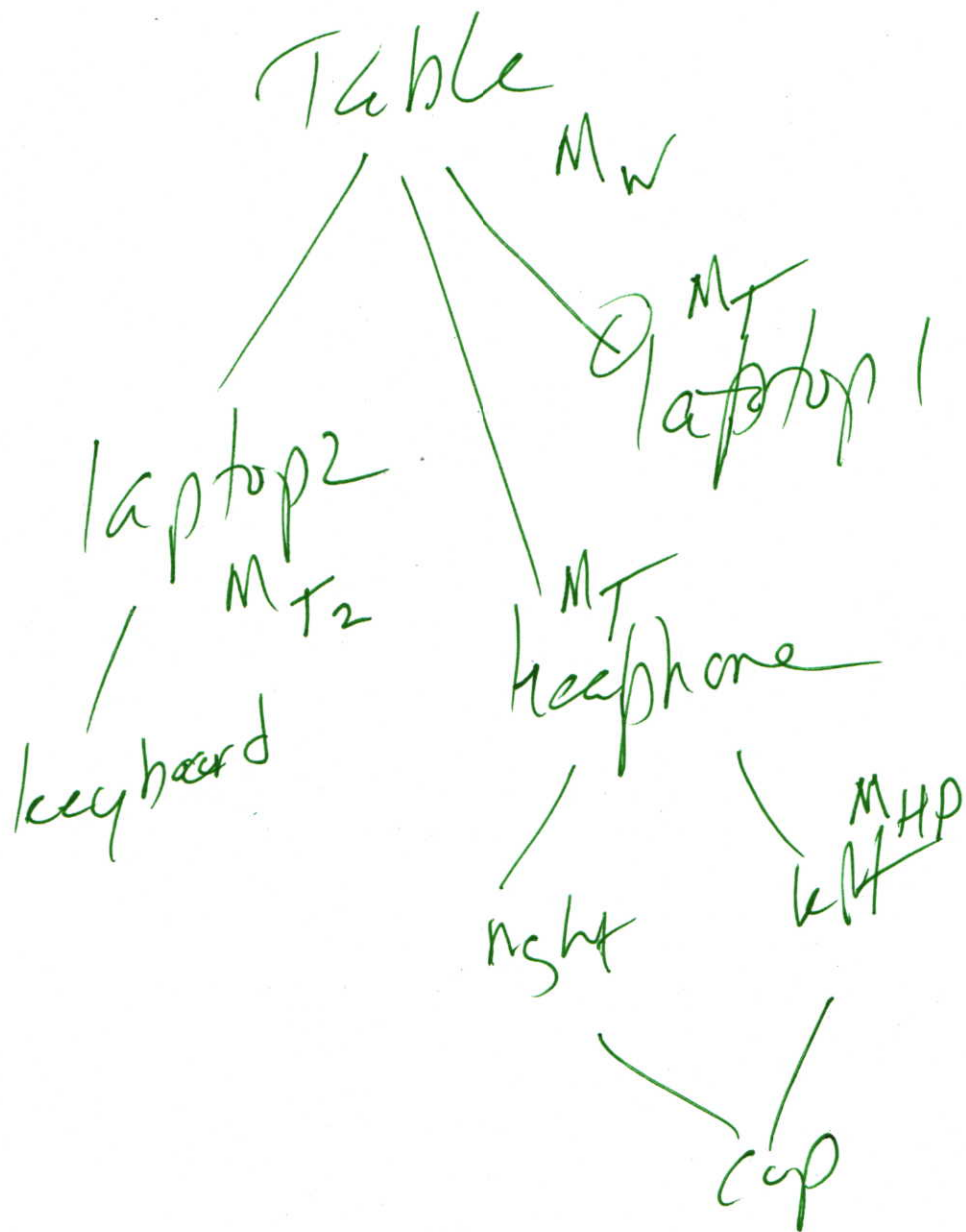
$$M = M_{R(45)} \quad \cancel{M_T(2,0)} \quad M_{R(45)} (P_{j0})$$

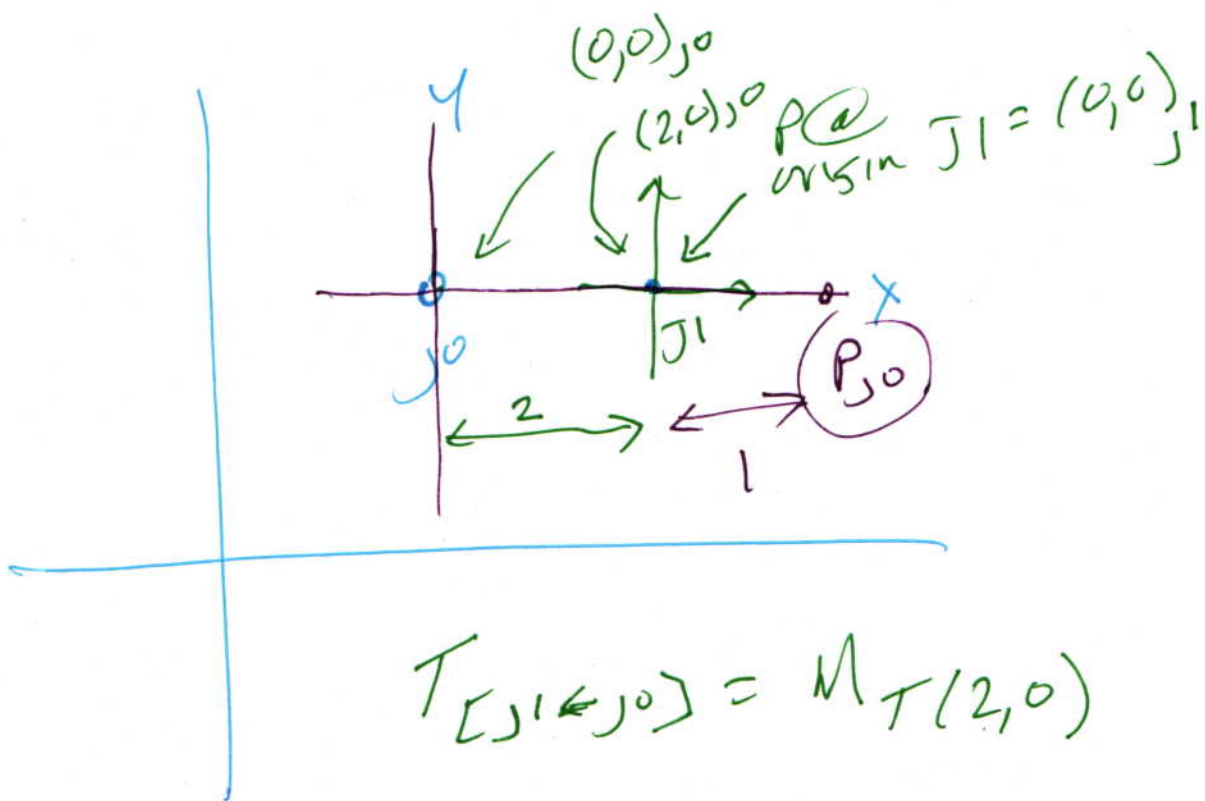
Amirreza
Time

J_3	0	10	20	30	
J_4	0	20	40	20	0
J_5	F	I	I	I	

$$M = M_k \cdot M_{-j_0} * M_{-j_1} * M_{-j_2} \dots$$

$M(P)$





$$T_{[J_1 \leftarrow J_0]} = M_{T(2,0)}$$

$$T_{[J_1 \leftarrow J_0]}(0,0) =$$

$$M_{T(2,0)} \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 2 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix}$$

$$= [2, 0, 1]$$

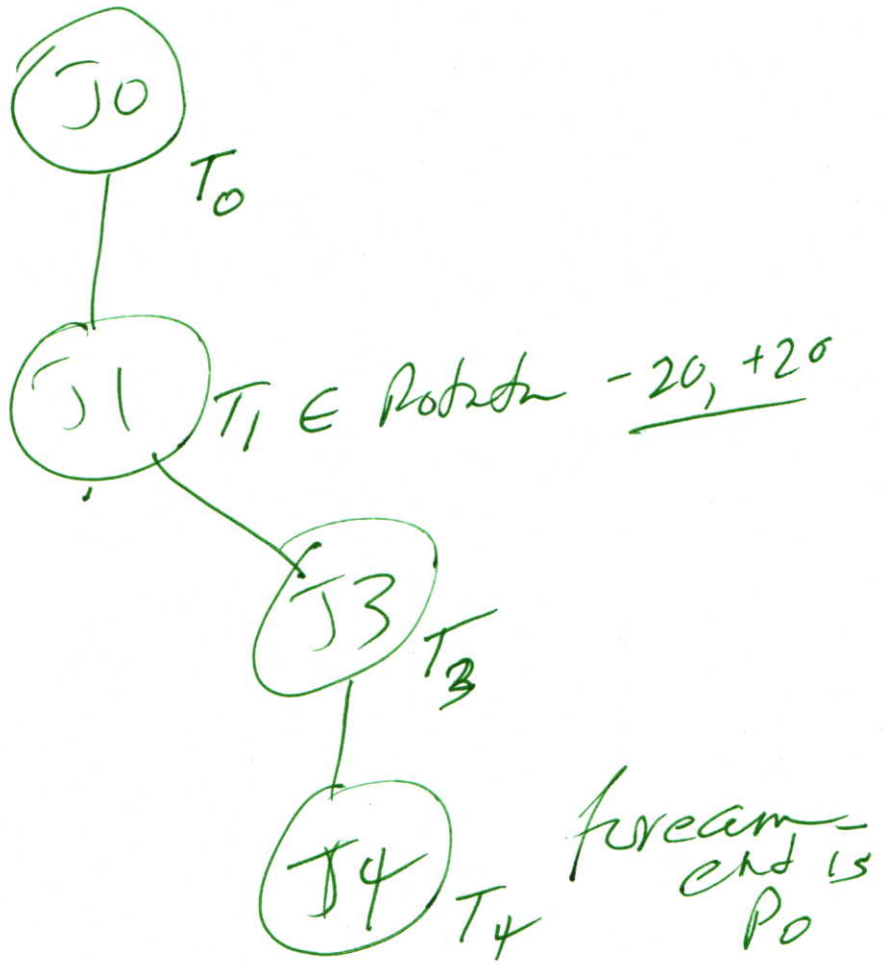
Homogeneous matrices

$$M_{T(\Delta x, \Delta y)} = \begin{bmatrix} 1 & 0 & \Delta x \\ 0 & 1 & \Delta y \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$

$$= \begin{bmatrix} x + \Delta x \\ y + \Delta y \\ 1 \end{bmatrix}$$

$$M_S(\alpha) = \begin{bmatrix} \alpha & 0 & 0 \\ 0 & \alpha & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$M_R(\theta) = \begin{bmatrix} \cos \theta & -\sin \theta & 0 \\ \sin \theta & \cos \theta & 0 \\ 0 & 0 & 1 \end{bmatrix}$$



forearm position =

$$T_4(T_3(T_1(T_0(P_0))))$$

