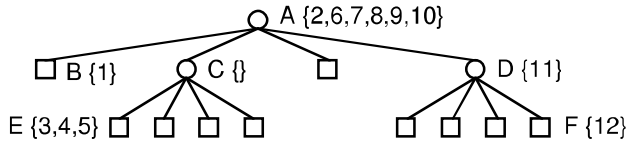
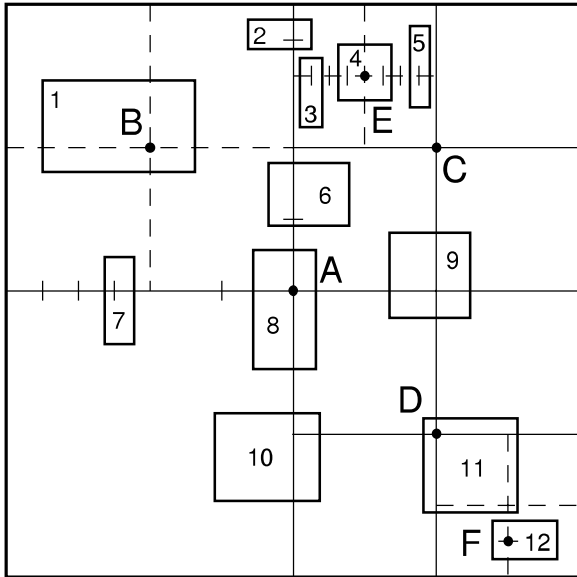


○ MX-CIF QUADTREE (Kedem)

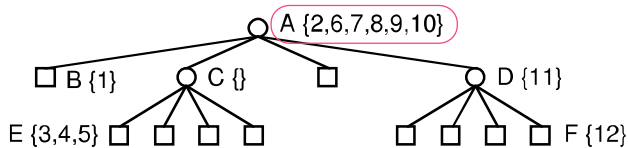
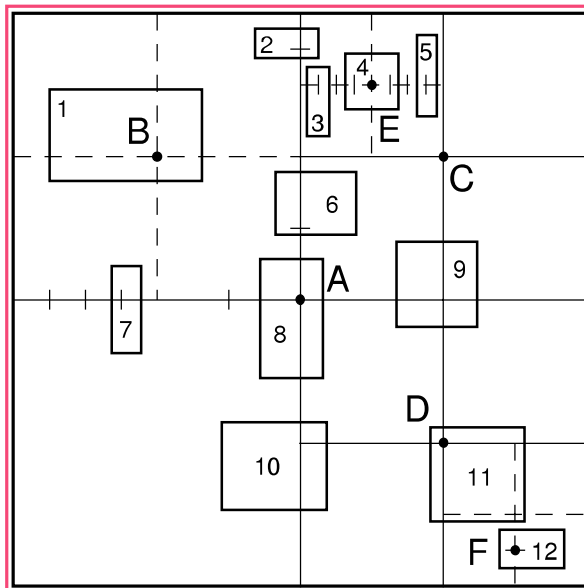
1 hp14 ○
b

1. Collections of small rectangles for VLSI applications
2. Each rectangle is associated with its minimum enclosing quadtree block
3. Like hashing: quadtree blocks serve as hash buckets



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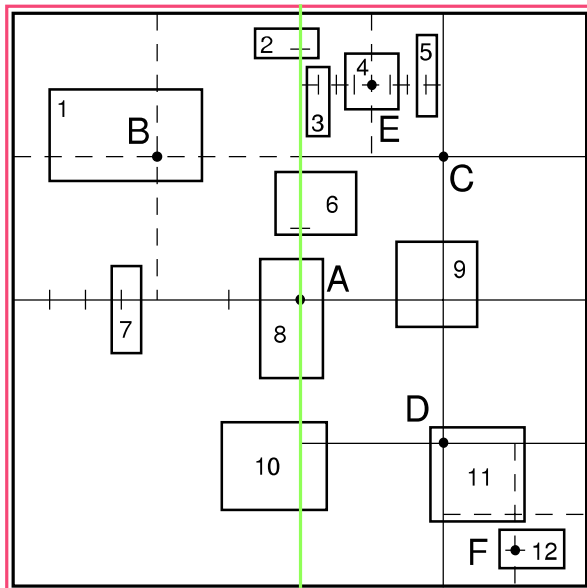


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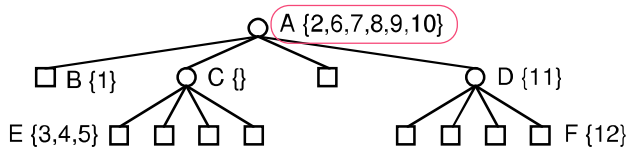
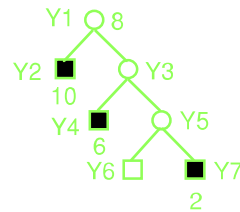
3	2	1
g	r	b

 hp14 ○

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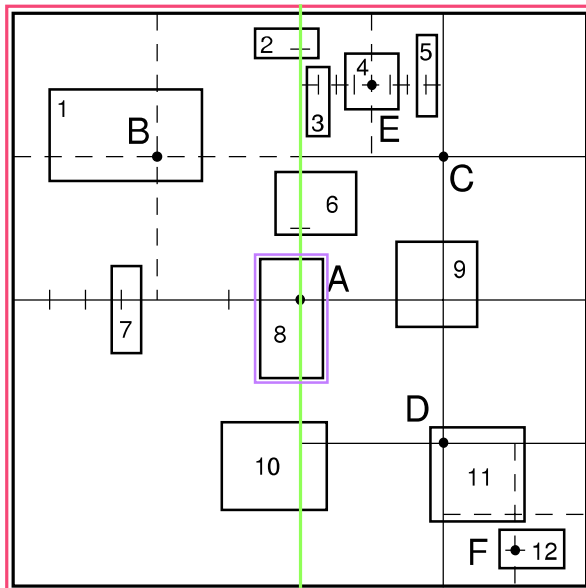
Binary tree for y-axis through A



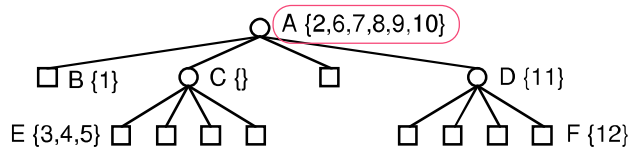
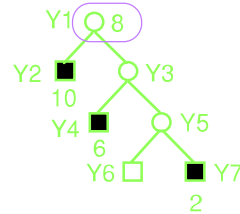
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v g r b

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 - if a rectangle intersects both x and y axes, then associate it with the y axis

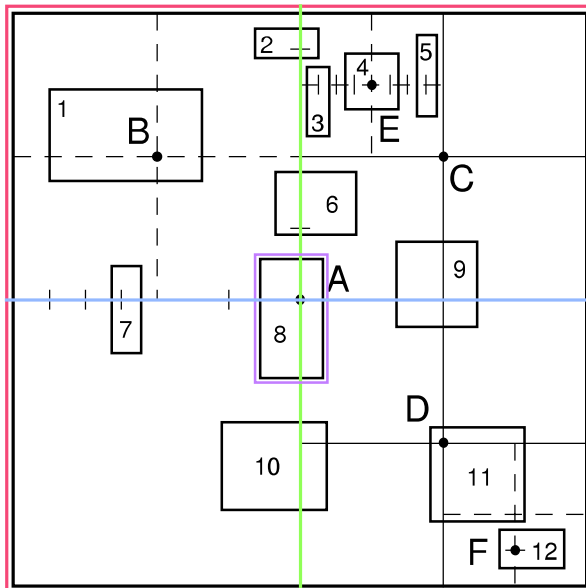


Binary tree for y-axis through A

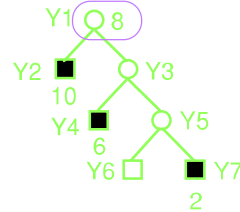


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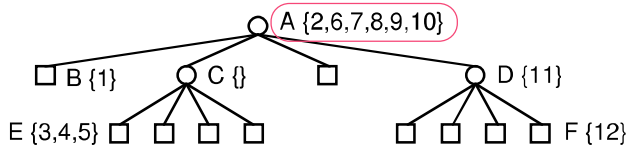
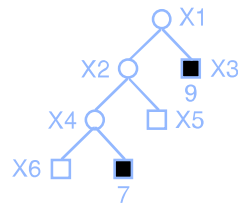
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Binary tree for y-axis through A

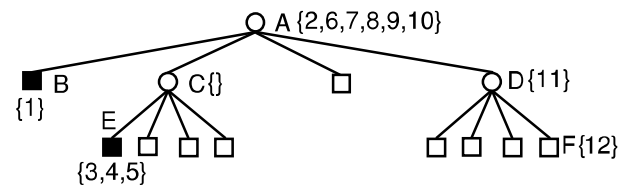
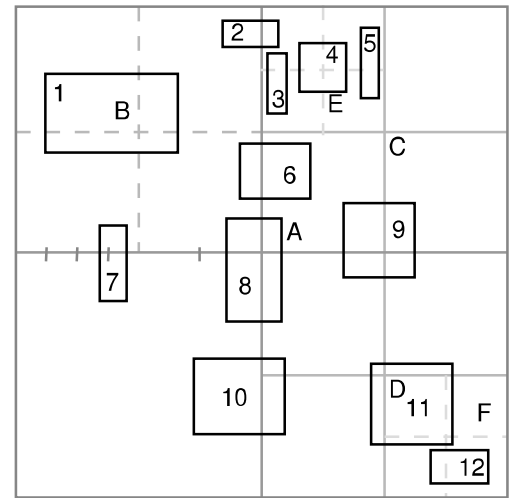


Binary tree for x-axis through A



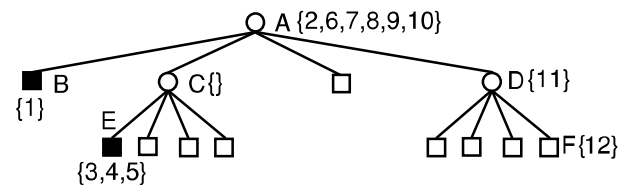
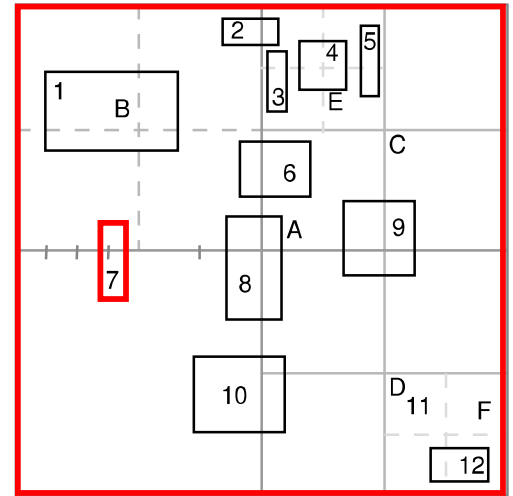
Loose Quadtree (Octree)/Cover Fieldtree

- Overcomes drawback of MX-CIF quadtree that the width w of the minimum enclosing quadtree block of a rectangle o is not a function of the size of o



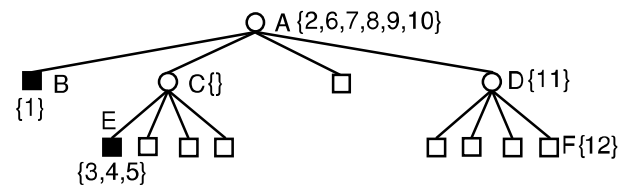
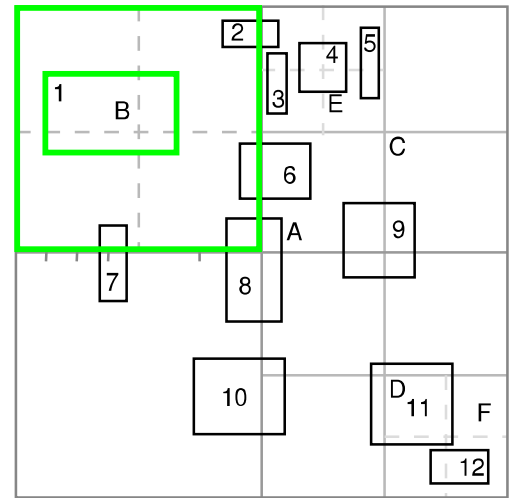
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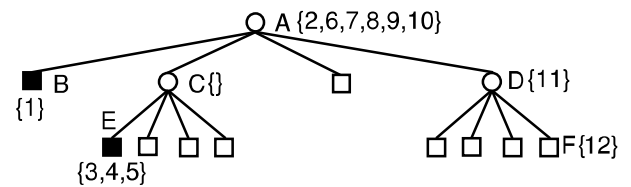
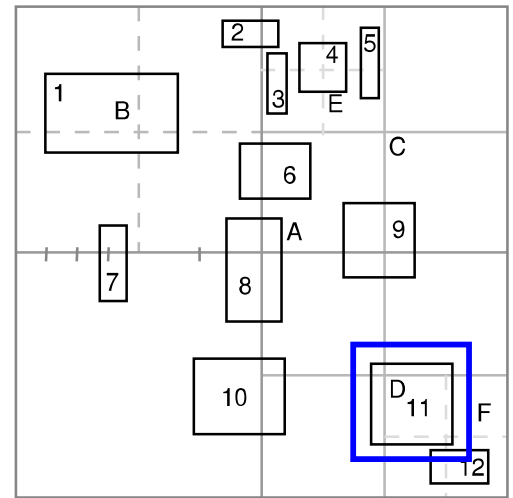
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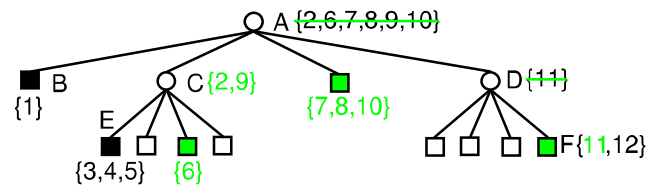
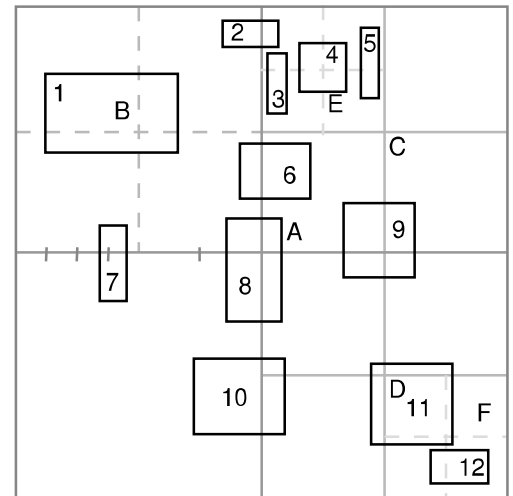
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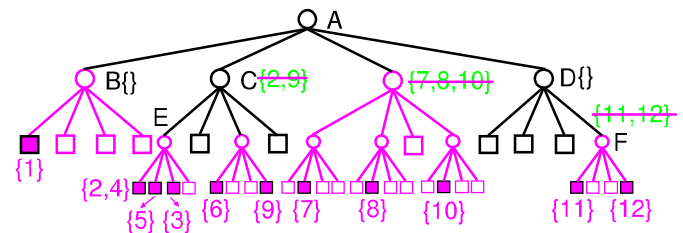
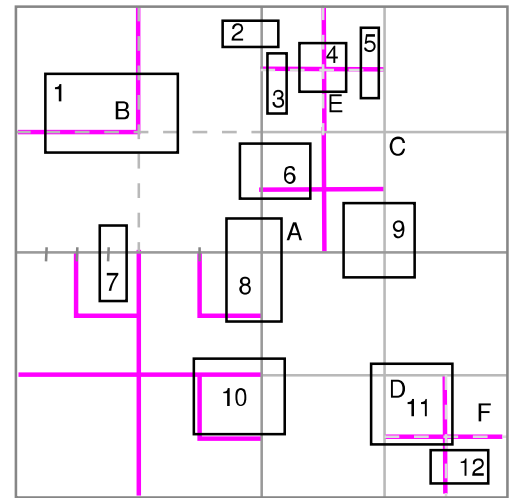
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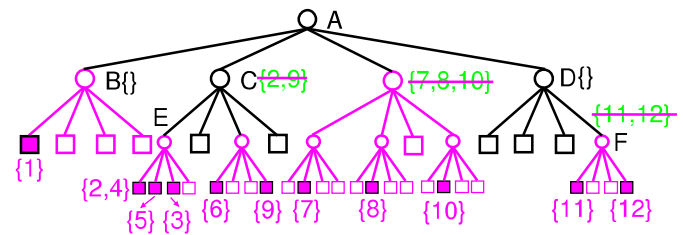
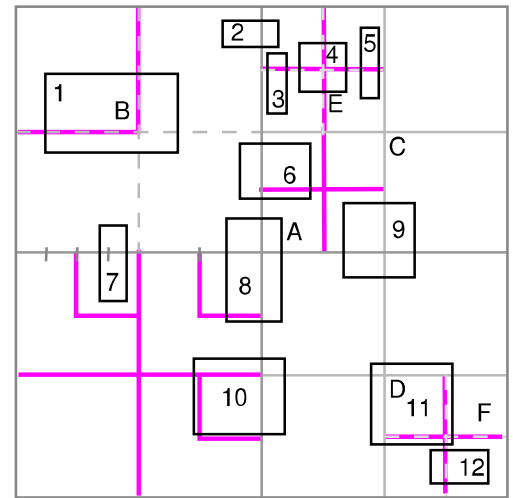
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- $p = 0.3$
- $p = 1.0$

- Maximum w (i.e., minimum depth of minimum enclosing quadtree block) is a function of p and radius r of o and independent of position of centroid of o

- Range of possible ratios $w/2r$: $1/(1 + p) \cdot w/2r < 2/p$
- For $p \geq 1$, restricting w and r to powers of 2, $w/2r$ takes on at most 2 values and usually just 1



Partition Fieldtree

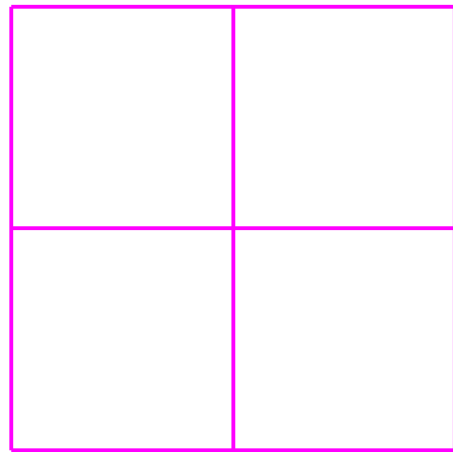
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- Achieves similar result by shifting positions of the centroid of quadtree blocks at successive levels of the subdivision by one half of the width of the block that is being subdivided

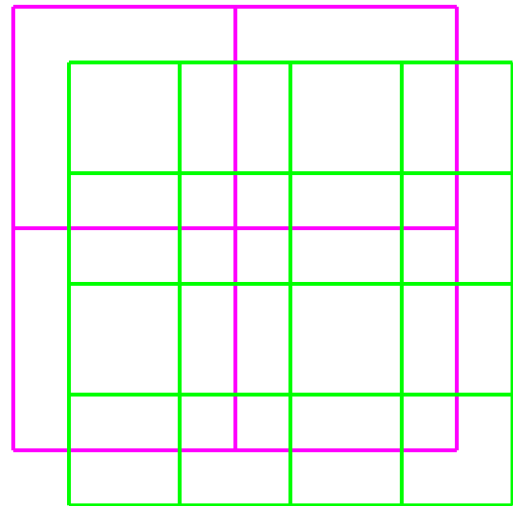
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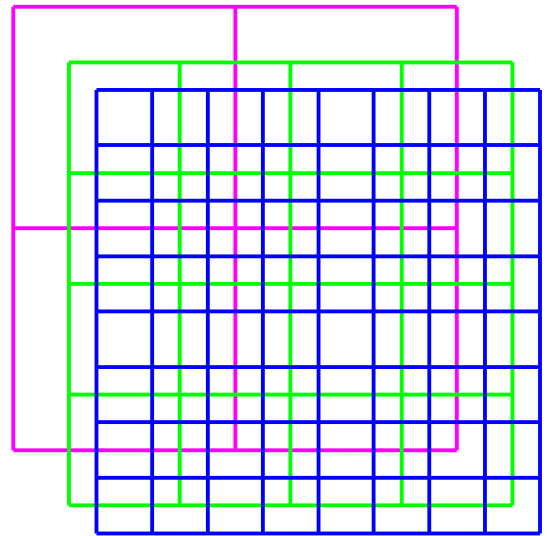
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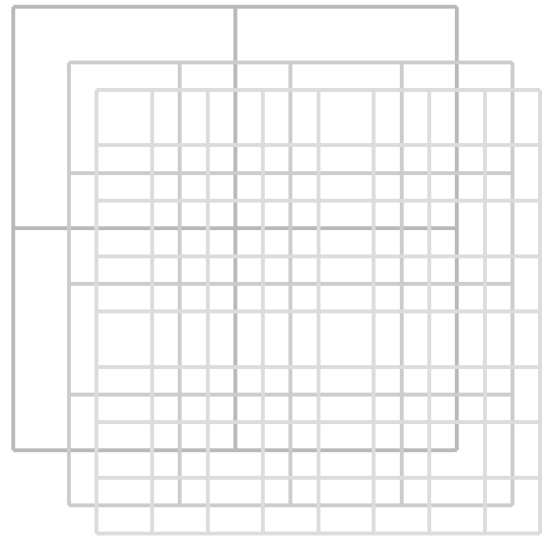
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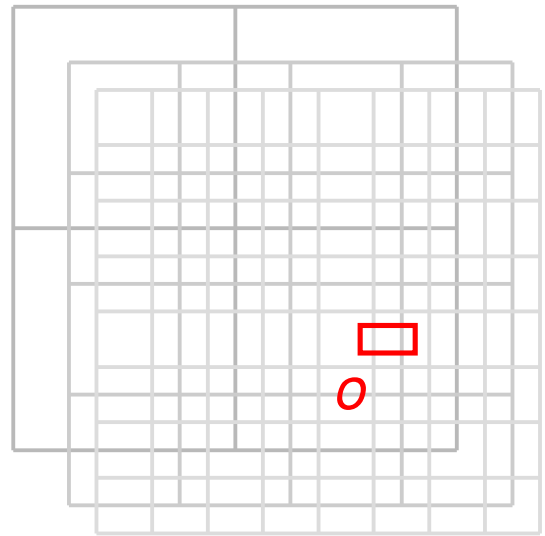
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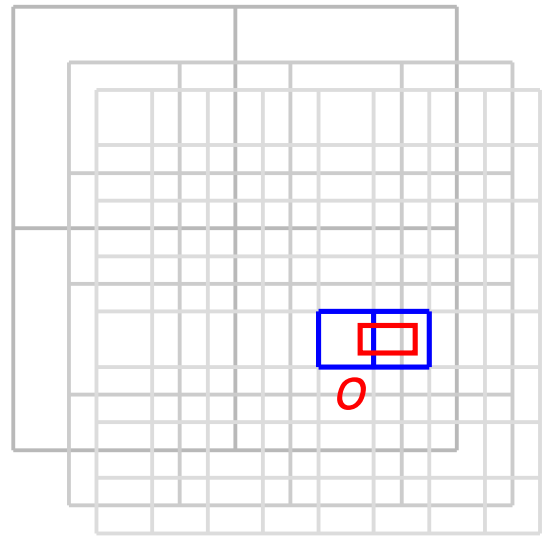
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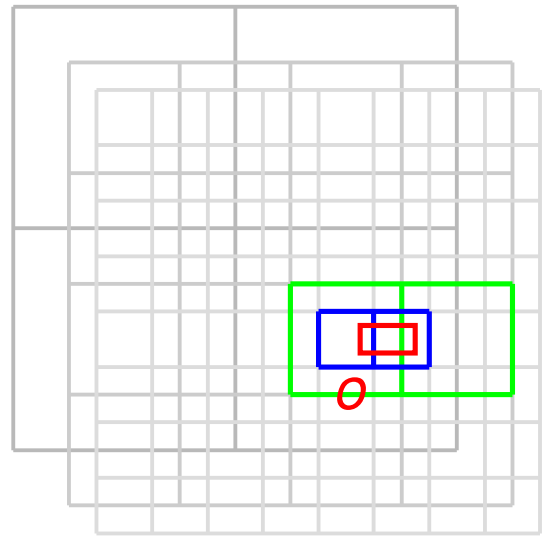
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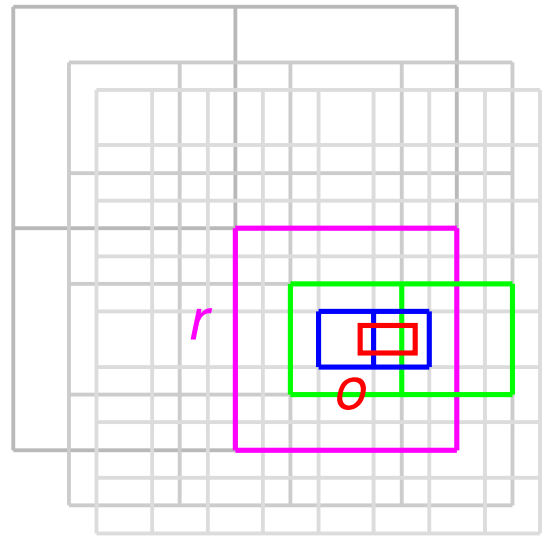
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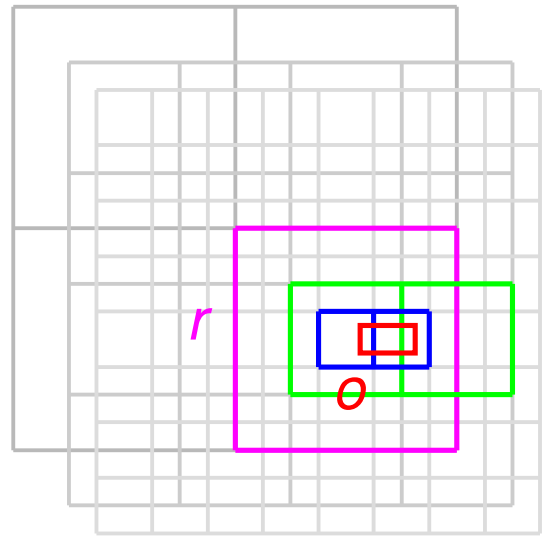
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- Same ratio is obtained for the loose quadtree (octree)/cover fieldtree when $p = 1/4$, and thus partition fieldtree is superior to the cover fieldtree when $p < 1/4$



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- Same ratio is obtained for the loose quadtree (octree)/cover fieldtree when $p = 1/4$, and thus partition fieldtree is superior to the cover fieldtree when $p < 1/4$
- Summary: cover fieldtree expands the width of the quadtree blocks while the partition fieldtree shifts the positions of their centroids

