



# Lecture 14: Parallel Algorithms

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# Communication algorithms

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- Reduction
- All-to-all

# Types of reduction

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- **Scalar reduction: every process contributes one number**
  - Perform some commutative associate operation
- **Vector reduction: every process contributes an array of numbers**

# Parallelizing reduction

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# Parallelizing reduction

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- Naive algorithm: every process sends to the root

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- Spanning tree: organize processes in a k-ary tree

# Parallelizing reduction

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- Naive algorithm: every process sends to the root
- Spanning tree: organize processes in a k-ary tree
- Start at leaves and send to parents
- Intermediate nodes wait to receive data from all their children

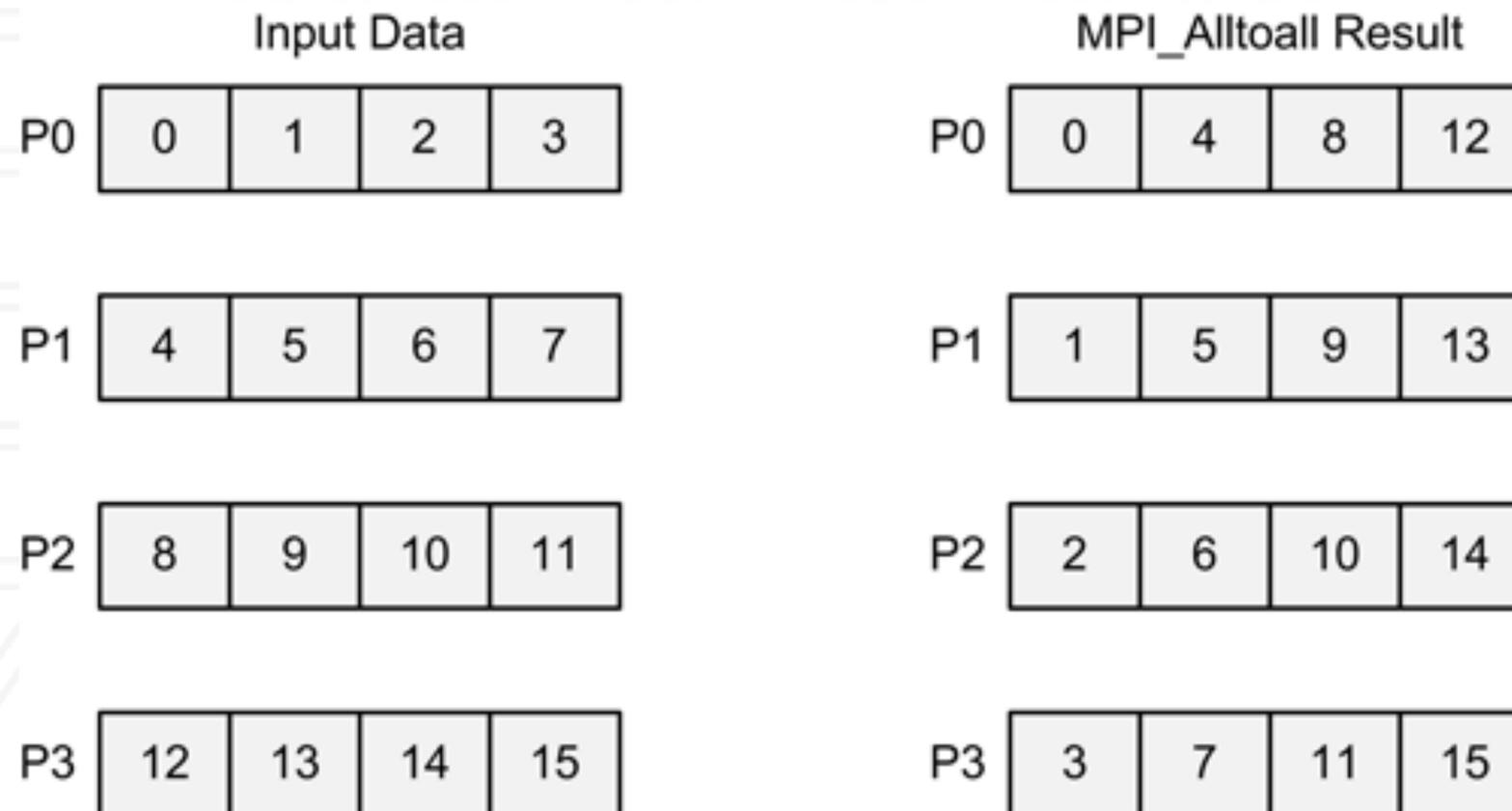
# Parallelizing reduction

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- Naive algorithm: every process sends to the root
- Spanning tree: organize processes in a k-ary tree
- Start at leaves and send to parents
- Intermediate nodes wait to receive data from all their children
- Number of phases:  $\log_k p$

# All-to-all

- Each process sends a distinct message to every other process
- Naive algorithm: every process sends the data pair-wise to all other processes

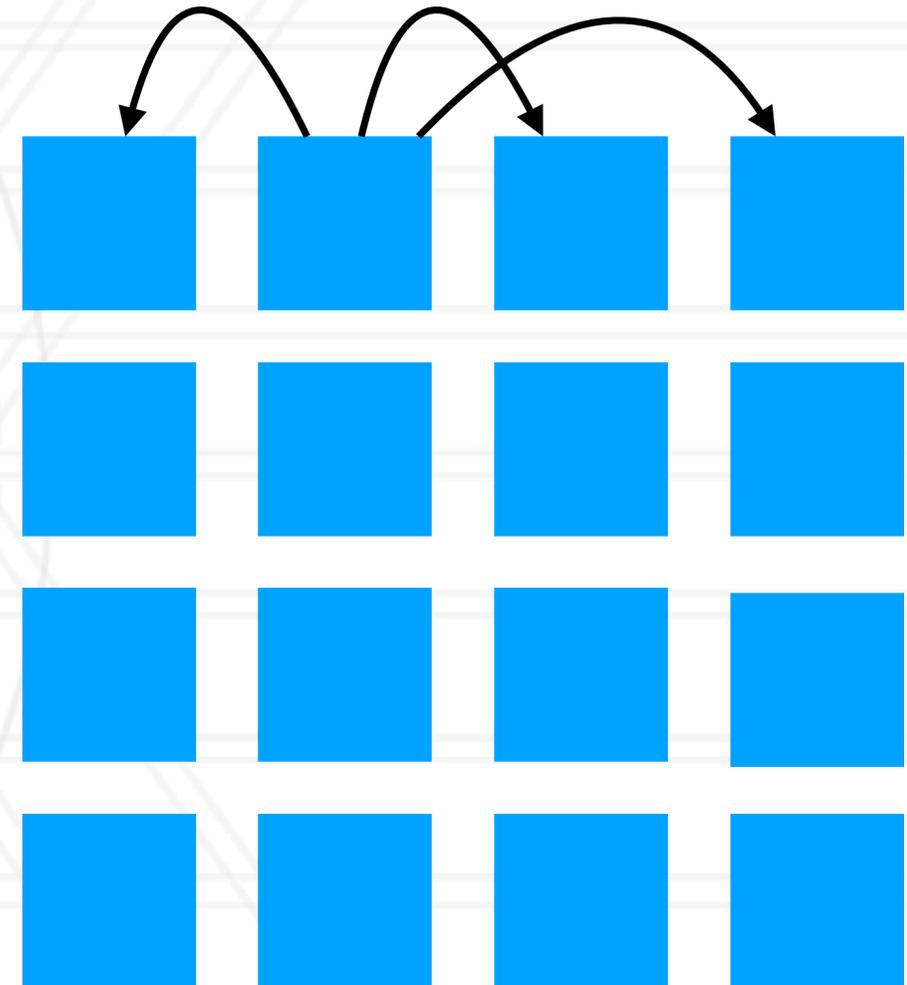


<https://www.codeproject.com/Articles/896437/A-Gentle-Introduction-to-the-Message-Passing-Inter>

# Virtual topology: 2D mesh

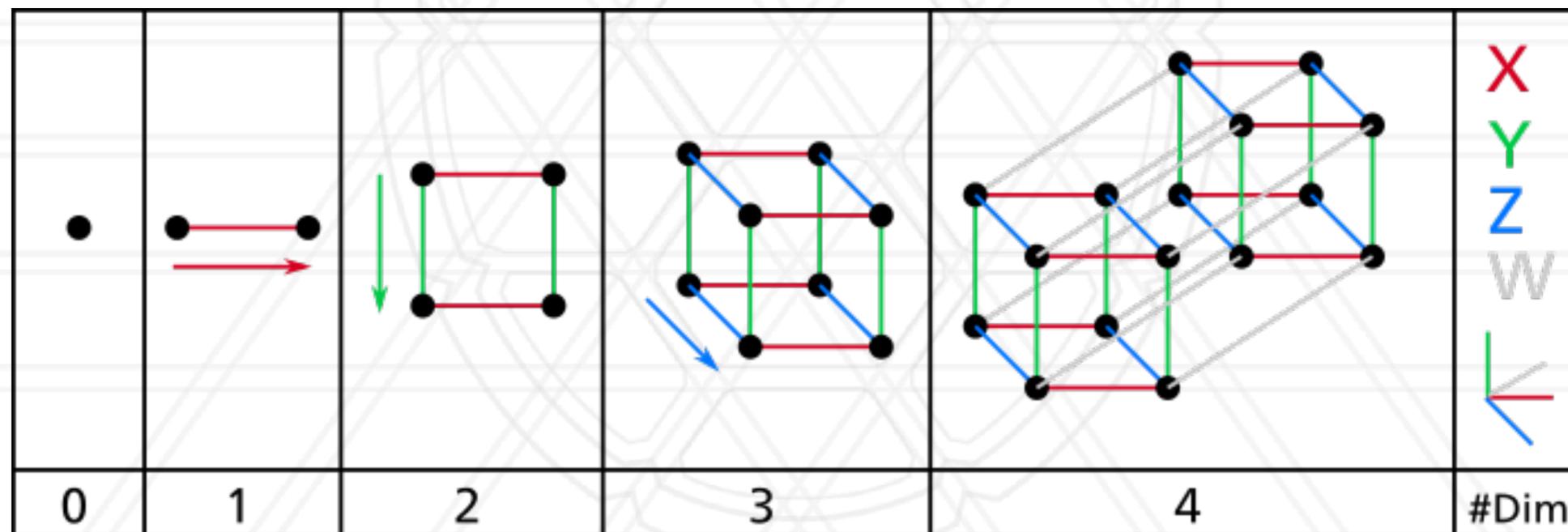
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- Phase 1: every process sends to its row neighbors
- Phase 2: every process sends to column neighbors



# Virtual topology: hypercube

- Hypercube is an n-dimensional analog of a square (n=2) and cube (n=3)
- Special case of k-ary d-dimensional mesh



<https://en.wikipedia.org/wiki/Hypercube>



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