

## Effective Random Testing of Concurrent Programs

### What is Concurrency?

- Simplest view
  - Sequential programs: single thread of control
  - Concurrent programs: multiple threads of control

## Concurrency Models

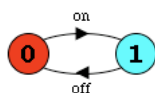
- Many models for studying concurrency
  - These slides use state machines, called Labelled Transition Systems (LTS)
  - Can view and analyze LTS models in using the LTSA analysis tool
- You can download the LTSA tool at:
  - <http://www.doc.ic.ac.uk/~jnm/book/ltsa/download.html>

## Modeling Processes

- Processes - units of sequential execution
  - Model processes as finite state machines
  - Use LTSA to analyse, display and animate behavior

## Modeling Processes (cont'd)

- Finite state machines transit from state to state by executing a sequence of atomic actions
- Example: a light switch LTS



## Examining Process Behaviors

- Sequences of actions or *traces*
  - on->off->on->off ...
- There can be an infinite number of unique traces

## Action Prefix

- If  $x$  is an action and  $P$  is a process then  $(x \rightarrow P)$  means that a process does action  $x$  and then behaves exactly as described by  $P$
- $\text{ONESHOT} = (\text{once} \rightarrow \text{STOP})$ .



- $\text{STOP}$  is a special state in which execution logically ends
- Conventions:
  - actions written in lowercase letters
  - PROCESSES written in uppercase letters

## Action Prefix & Recursion

- Repetitive behaviour uses recursion:  
 $\text{SWITCH} = \text{OFF},$   
 $\text{OFF} = (\text{on} \rightarrow \text{ON}),$   
 $\text{ON} = (\text{off} \rightarrow \text{OFF}).$
- Substituting gives you:  
 $\text{SWITCH} = \text{OFF},$   
 $\text{OFF} = (\text{on} \rightarrow (\text{off} \rightarrow \text{OFF})).$
- And again:  
 $\text{SWITCH} = (\text{on} \rightarrow \text{off} \rightarrow \text{SWITCH}).$

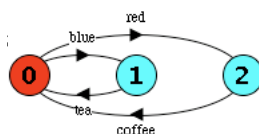
## Choice

- If  $x$  and  $y$  are actions then  $(x \rightarrow P \mid y \rightarrow Q)$  is a process which does action  $x$  and then behaves exactly as described by  $P$ , or which does action  $y$  and then behaves exactly as described by  $Q$

## Choice (cont.)

- FSP model of a drinks machine :  

$$\text{DRINKS} = (\text{red} \rightarrow \text{coffee} \rightarrow \text{DRINKS} \mid \text{blue} \rightarrow \text{tea} \rightarrow \text{DRINKS}).$$
- LTS generated using LTSA:

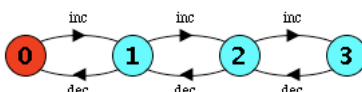


## Guarded Actions

- $(\text{when } B \ x \rightarrow P \mid y \rightarrow Q)$  means that when the guard  $B$  is true the actions  $x$  and  $y$  are both eligible to be chosen, otherwise the action  $x$  cannot be chosen

...

$\text{COUNT}[i:0..N] = (\text{when}(i < N) \text{ inc} \rightarrow \text{COUNT}[i+1] \mid \text{when}(i > 0) \text{ dec} \rightarrow \text{COUNT}[i-1]).$



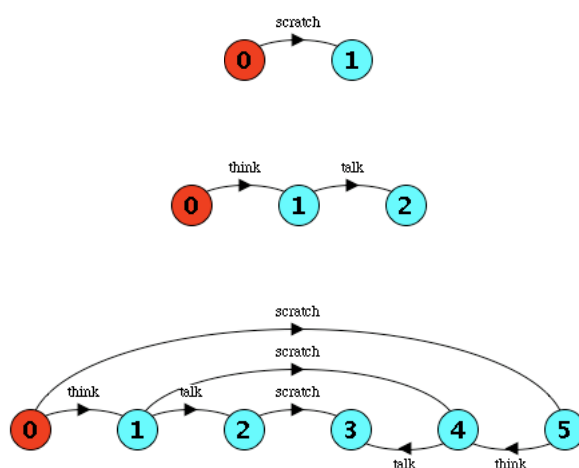
## Modeling Concurrency

- So far we've modeled individual processes. How do we model concurrent processes?
  - Compose processes by arbitrarily interleaving actions from different processes (but preserve within process order)
- Ignores process execution speed
  - assumes arbitrary speed (abstract away time)

## Parallel Composition – Action Interleaving

- If P and Q are processes then  $(P \parallel Q)$  represents the concurrent execution of P and Q
- $\parallel$  is the parallel composition operator  
 $ITCH = (\text{scratch} \rightarrow \text{STOP}).$   
 $\text{CONVERSE} = (\text{think} \rightarrow \text{talk} \rightarrow \text{STOP}).$   
 $\parallel \text{CONVERSE\_ITCH} = (ITCH \parallel \text{CONVERSE}).$

## ITCH $\parallel$ CONVERSE



## Modeling Interaction - Shared Actions

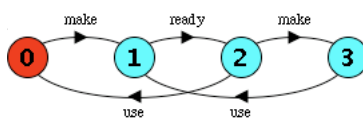
- If processes in a composition have common actions, those actions are said to be shared
- Shared actions are how process interaction is modeled
- While unshared actions may be arbitrarily interleaved, a shared action must be executed at the same time by all processes that participate in the shared action

MAKER = (make->*ready*->MAKER).

USER = (*ready*->use->USER).

||MAKER\_USER = (MAKER || USER).

## MAKER||USER



## Model Checking Programs

- Situation gets more complicated, but the general ideas are still applicable
- Can model concurrent program executions as interleavings of individual program executions

## Example Program & Execution Traces

Initially  $x = 0$  and  $y = 0$

| Thread 1:           | Thread 2:                             |
|---------------------|---------------------------------------|
| <code>y = 1;</code> | <code>if (x==4) assert(false);</code> |
| <code>y = 2;</code> |                                       |
| <code>y = 3;</code> |                                       |
| <code>x = 4;</code> |                                       |

Figure 1: Simple Example

```
if (x==4) assert(false); y=1; y=2; y=3; x=4;
y=1; if (x==4) assert(false); y=2; y=3; x=4;
y=1; y=2; if (x==4) assert(false); y=3; x=4;
y=1; y=2; y=3; if (x==4) assert(false); x=4;
y=1; y=2; y=3; x=4; if (x==4) assert(false);
```

Figure 2: Five Interleavings Exhibited by the Simple Example

## Observation

- Only variable  $x$  is shared between the two threads
- Many of the interleaved executions are therefore equivalent. Only 2 sets of distinct traces:
  - “ $x=4$ ” in Thread 1 then “if ( $x==4$ ) ...” in Thread 2
  - “if ( $x==4$ ) ...” in Thread 2 then “ $x=4$ ” in Thread 1
- Creates lots of extra, useless work
- Random exploration oversamples equiv. traces

## Partial Order Traces

- If two transitions do not interact with each other then they are independent. All other transitions are dependent. Some examples:
  - Transitions in same thread are dependent
  - Two threads acquiring the same lock is dependent
- Intuitively, we can reorder some independent transitions without affecting the program's behavior

## Partial Order Traces (cont.)

- The happens-before relation  $\prec$  for a transition sequence  $\tau = t_1 t_2 \dots t_n$  is defined as the smallest relation such that
  - If  $t_i$  and  $t_j$  are dependent and  $1 \leq i \leq j \leq n$ , then  $t_i \prec t_j$ , and
  - $\prec$  is transitively closed
- All transition sequences that are linearizations of the same partial order are equivalent

## RAPOS: Random Partial Order Sampling Algorithm

- Uses two sets of transitions
  - **Schedulable**: a subset of the transitions that are ready to execute
  - **Scheduled**: random subset of Schedulable in which all transitions are mutually independent

## RAPOS (cont.)

```

RAPOS() {
  s := s0;
  schedulable := Enabled(s);
  while (Enabled(s) ≠ ∅) {
    scheduled := RandIndependentSubset(schedulable);
    for each t ∈ scheduled
      s := Execute(s, t);
    schedulable := {t' ∈ Enabled(s) | ∃t ∈ scheduled
      such that t and t' are dependent };
    if (schedulable = ∅)
      add a random element from Enabled(s) to schedulable
  }

  if (Alive(s) ≠ ∅) {
    print "Deadlock Detected";
  }
}

```

Figure 4: Random Partial Order Sampling Algorithm (RAPOS)

## RAPOS Application

y=1  
y=2  
y=3  
x=4

if (x==4) assert false

schedulable: {y=1} | {if (x==4) assert false} | {y=1, if (x==4) assert false}

## RAPOS Application (1<sup>st</sup> trace)

y=1  
y=2  
y=3  
x=4

if (x==4) assert false

schedulable: {y=1, if (x==4) assert false}

scheduled: {if (x==4) assert false}

## RAPOS Application (1<sup>st</sup> trace)

y=1  
y=2  
y=3  
x=4

if (x==4) assert false

schedulable: {y=1, if (x==4) assert false}

scheduled: {if (x==4) assert false}

## RAPOS Application (1<sup>st</sup> trace)

y=1  
y=2  
y=3  
x=4

if (x==4) assert false

schedulable: {}  
scheduled: {if (x==4) assert false}

## RAPOS Application (1<sup>st</sup> trace)

y=1  
y=2  
y=3  
x=4

if (x==4) assert false

schedulable: {y=1}  
scheduled: {if (x==4) assert false}

## RAPOS Application (1<sup>st</sup> trace)

y=1  
y=2  
y=3  
x=4

if (x==4) assert false

schedulable: {y=1}  
scheduled: {y=1}

## RAPOS Application (1<sup>st</sup> trace)

y=1  
y=2  
y=3  
x=4

if (x==4) assert false

schedulable: {y=1}  
scheduled: {y=1}

## RAPOS Application (2<sup>nd</sup> trace)

y=1  
y=2  
y=3  
x=4

if (x==4) assert false

schedulable: {y=1, if (x==4) assert false}  
scheduled: {y=1}

## RAPOS Application (2<sup>nd</sup> trace)

y=1  
y=2  
y=3  
x=4

if (x==4) assert false

schedulable: {y=1, if (x==4) assert false}  
scheduled: {y=1}

## RAPOS Application (2<sup>nd</sup> trace)

y=1  
y=2  
y=3  
x=4

if (x==4) assert false

schedulable: {y=2}  
scheduled: {y=1}

## RAPOS Application (2<sup>nd</sup> trace)

y=1  
y=2  
y=3  
x=4

if (x==4) assert false

schedulable: {y=2}  
scheduled: {y=2}